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A COMPUTER MODEL PREDICTING THE THERMAL RESPONSE TO MICROWAVE RADIATION

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NOTICES

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This report has been reviewed and is approved for publication.

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20. ABSTRACT (Continued)

publication which appeared in Vol. BME-27, Nov. 8, of the IEEE Transactions on Biomedical Engineering. The results of these measurements are discussed in this report.

We describe a shooting method for solving the eigenvalue and eigenfunction determination problem for a multilayered, penetrable, spherically symmetric, autothermally regulated, simulated biostructure when there is heat removal by blood flow in some but possibly not all of the layers. This requires study of a new type of special function.

While originally our computer program experienced difficulty when the frequency of the incoming radiation was as high as 10 GHz or when the radius of the sphere bounding the ball of biotissue was as large as 48 cm, we have overcome this problem with a hybrid scheme for computing spherical Bessel functions.

Our computer program 'lso permits the computation of temperature excursions that would be experienced by the simulated biostructure when the source of radiation is pulsed in a complex way. We develop exact formulas which enable us to express the expansion coefficients of the temperature in terms of integrals with respect to the spatial coordinates only. To save computing time, the points that will be used in the Gaussian quadrature are determined in advance and care is taken to make certain that no calculation is needlessly repeated.

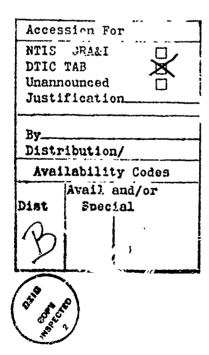


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COMPUTER MODEL PREDICTING THE THERMAL RESPONSE TO MICROWAVE RADIATION OF A SIMULATED BIOLOGICAL STRUCTURE

1. INTRODUCTION

autothermally regulated body such as a biological body to a source of microwave radiation. The description of this method is divided into five parts. It includes (1) a discussion of the symbols (and their units) used in developing the solution, (2) the induced electromagnetic field distribution and the power density distribution that represents the source term for the heat transfer problem, (3) the modified heat operator eigenvalues and eigenfunctions associated with a Newton cooling law boundary condition, (4) the computation of temperature excursions induced by microwave radiation including complex pulse heating schemes, and (5) a discussion of the spreading of temperature distributions with time in three types of simulated biological structures. These are discussed in Sections 3.1-3.5 respectively.

In [2] we developed a computer model to determine the temperature distribution in a penetrable, homogeneous, and spherically symmetric body that has been irradiated by microwave radiation. Heat removal by blood flow could be considered, provided that only one layer was used in the model. In the present paper a shooting method for solving the eigenvalue and eigenfunction determination problem for a multilayered, penetrable, but spherically symmetric scatterer is solved when the heat equation describing the microwave heating includes the possibility of blood-flow-heat-removal terms in some, but not necessarily all layers. This innovation is described in Section 3.

Also, originally our program in [2] experienced some difficulty in computing expansion coefficients used in determining the induced electric field when the frequency of the incoming radiation was high (>10 GHz) or when the radius of the outer sphere was as large as 48 cm; the procedure by which we overcame this difficulty is described in Section 2. Some experimental microwave bioenvironmentalists look for a nonthermal microwave effect and consequently attempt to control temperature in their microwave exposure systems by using a complex microwave pulse heating scheme with a low duty factor. therefore contains a description of a formula which permits one to express the expansion coefficients associated with a complex temporal heating pattern in terms of integrals with respect to only the spatial variables. note that several people--including MacLatchy and Clements [9] and Washisu and [11] have proposed microwave-induced temperature excursions as a nonperturbing method of measuring or estimating field Consequently, in Section 3.5 of this paper we have included a discussion of the potential and limitations of this method of field measurement. because microwave heating may be used to treat tumors in humans (c.f. Zimmer et al. [12]), we give in Section 3.5 some new computer calculations showing possible thermal effects on simulated biological structures.

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2. RESULTS AND DISCUSSION

In this paper the authors extend the computer model which generated the results of [2]. We consider as before that a plane wave irradiates a spherically symmetric structure in the manner indicated in Figure 2.1. We allow, however, time profiles similar to that of the PAVE PAWS radar so that heating from any radar emission can be estimated directly. We note that with this capability and the possibility of estimating temperature derivatives that one can, by solving the equations of thermoelasticity, describe radar acoustic effects in a quantitative way. This is important in view of large efforts by other branches of the armed services to study this effect. We can also, by going to more general geometries and using an integral equation method, describe quantitatively the effect of microwave radiation on biochemical processes and fetal development which are strictly thermal in nature.

Figures 2.2-2.10 compare computer model predictions with measurements made by John G. Burr at Brooks AFB and give a comparison of our ability to predict spatial variations in temperature for two radiofrequencies (RF), 1.2 GHz and 2.5 GHz, and for a short 30-s and for a longer 3-min exposure. The capability of predicting the thermal response to pulsed radiation is demonstrated in Figure 2.11.

We now discuss the effect of blood flow in removing heat from a living system subjected to microwave-radiation-induced thermal excursions. John Burr and Jerome Krupp of the Radiation Sciences Division of the USAF School of Aerospace Medicine reported in [3] the results of Figure 2.12 showing temperature measurements in the head of a living and dead Macaca mulatta. In Figure 2.13 we use blood flow rates supplied in [9] to estimate the effect of the blood flow term in giving a lower predicted value of a radiation-induced temperature increase.

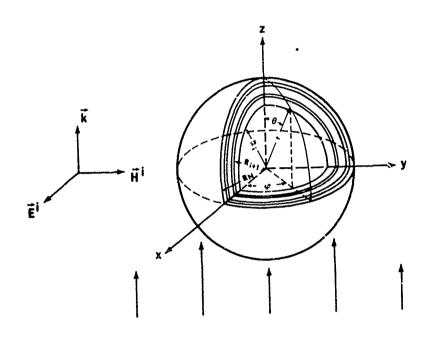


Figure 2.1. Electromagnetic plane wave impinging on a cranial model composed of an inner core sphere and N concentric spherical shells.

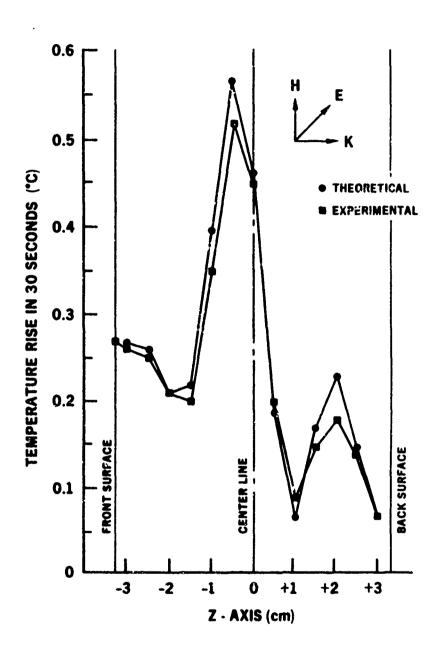


Figure 2.2. Temperature rise along the z-axis of a 3.3-cm radius homogeneous muscle-equivalent sphere exposed to 1.2 GHz, continuous wave (CW), 70 mW/cm^2 , RF in the far field for 30 s.

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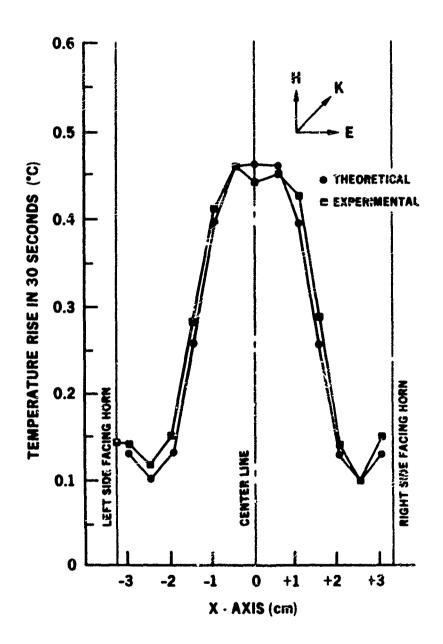


Figure 2.3. Temperature rise along the x-axis of a 3.3-cm radius homogeneous muscle-equivalent sphere exposed to 1.2 GHz, CW, 70 mW/cm 2 , RF in the far field for 30 s.

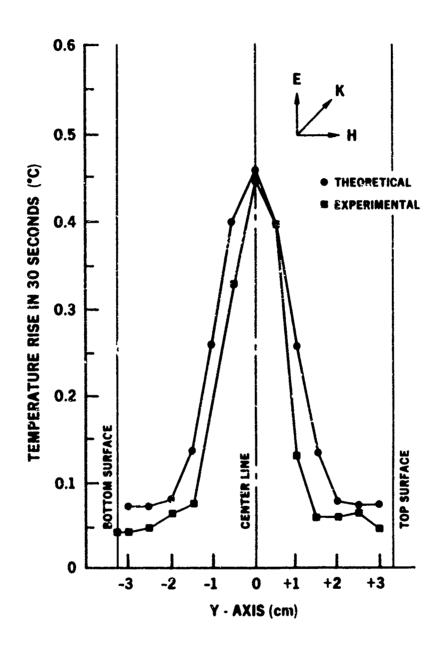


Figure 2.4. Temperature rise along the y-axis of a 3.3-cm radius homogeneous muscle-equivalent sphere exposed to 1.2 GHz, CW, 70 mW/cm 2 , RF in the far field for 30 s.

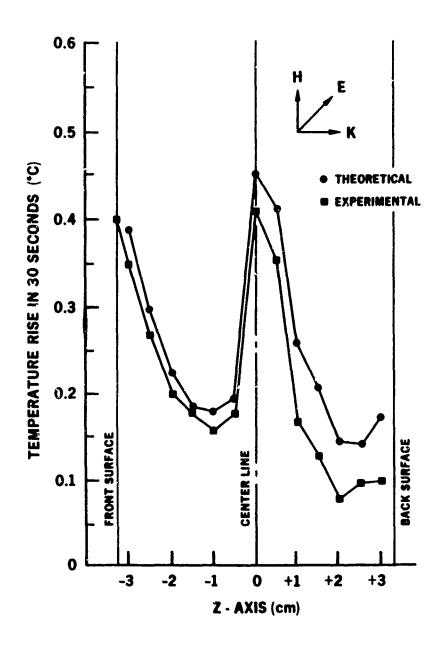


Figure 2.5. Temperature rise along the z-axis of a 3.3-cm radius homogeneous muscle-equivalent sphere exposed to 2.5 GHz, CW, $100~\text{mW/cm}^2$, RF in the far field for 30 s.

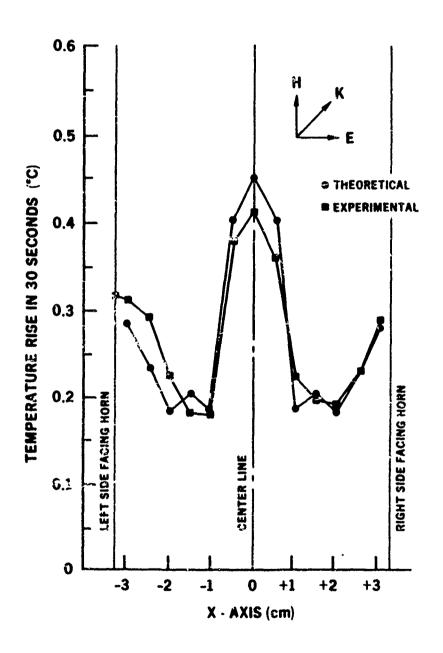


Figure 2.6. Temperature rise along the x-axis of a 3.3-cm radius homogeneous muscle-equivalent sphere exposed to 2.5 GHz, CW, $100~\text{mW/cm}^2$, RF in the far field for 30 s.

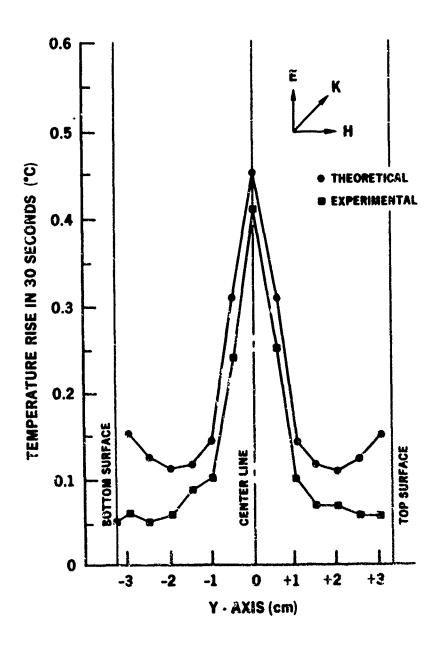


Figure 2.7. Temperature rise along the y-axis of a 3.3-cm radius homogeneous muscle-equivalent sphere exposed to 2.5 GHz, CW, 100 mW/cm², RF in the far field for 30 s.

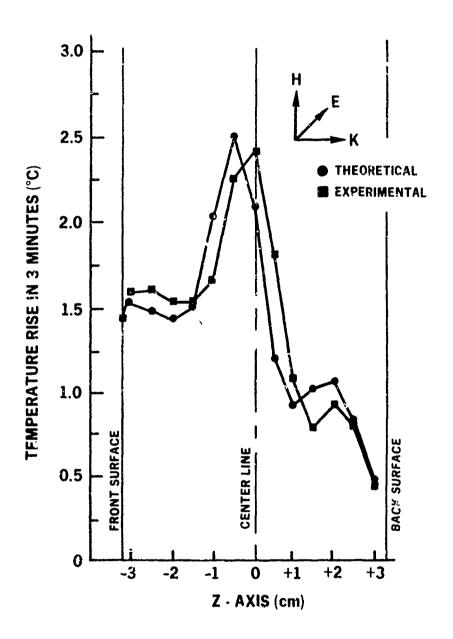


Figure 2.8. Temperature rise along the z-axis of a 3.3-cm radius homogeneous muscle-equivalent sphere exposed to 1.2 GHz, CW, 70 mW/cm^2 , RF in the far field for 3 min.

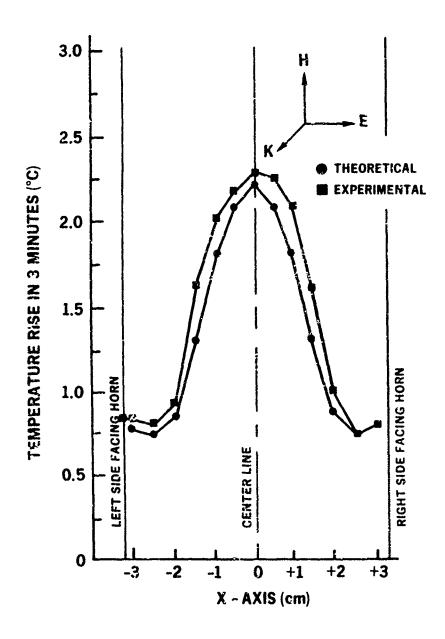


Figure 2.9. Temperature rise along the x-axis of a 3.3-cm radius homogeneous muscle-equivalent sphere exposed to 1.2 GHz, CW, 70 mW/cm 2 , RF in the far field for 3 min.

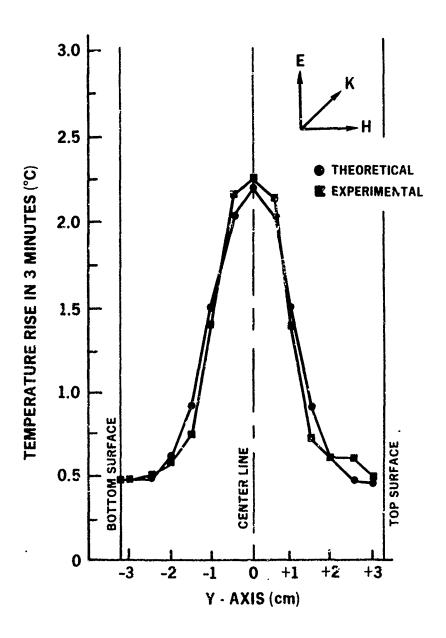


Figure 2.10. Temperature rise along the y-axis of a 3.3-cm radius homogeneous muscle-equivalent sphere exposed to 1.2 GHz, CW, 70 mW/cm^2 , RF in the far field for 3 min.

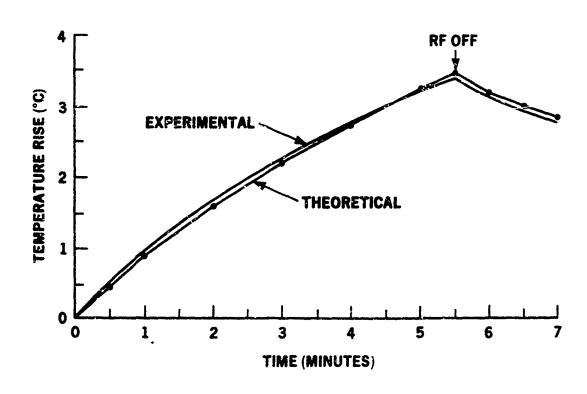


Figure 2.11. The predicted and measured temperature excursion versus time at the center of a 3.3-cm radius homogeneous muscle-equivalent sphere at 1.2 GHz, CW, 70 mW/cm².

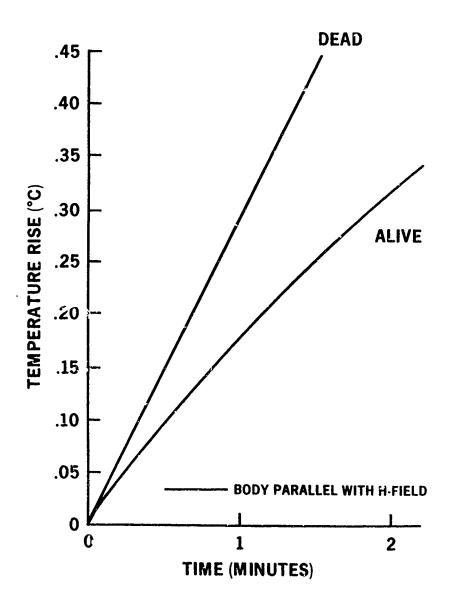


Figure 2.12. Temperature excursion in the midbrain of a living (blood flow case) and dead (no blood flow case) Macaca mulatta (rhesus monkey) head exposed to 70 mW/cm², CW, RFR in the far field, 1.2 GHz [3].

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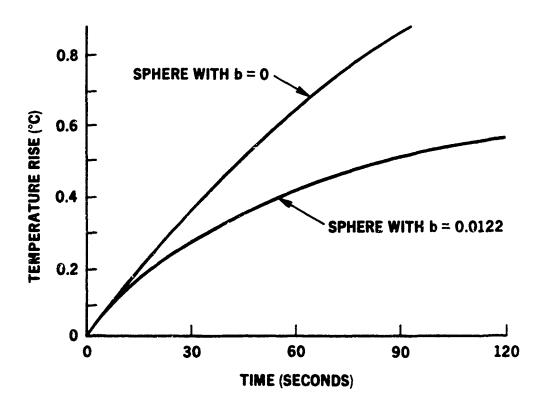


Figure 2.13. Effect of the blood flow term (b) on the temperature excursion in the center of a 4.5-cm radius homogeneous muscle-equivalent sphere.

We see that there are qualitative differences in the curvature of the temperature versus time curves in Figures 2.12 and 2.13 that are at this point unexplained although the measured and predicted values seem to be reasonably close.

Finally we give a comparison between our computer model and the simpler model developed by Kritikos and Schwan [5]. This comparison is given in Figures 2.14 and 2.15.

We note that consideration of the thought experiment depicted in Figure 2.16 makes it obvious that there is such a thing as a nonthermal effect. We consider a structure that will not drift in a microwave field but which will necessarily respond differently to a microwave field and to an equivalent amount of thermal energy. We consider a simple molecule with three charges in a row connected by two chemical bonds that we approximate by two linear springs with identical spring constants. The outside two moieties have charge q and the middle moiety has charge -2q.

Since all three masses are the same, the thermal energy of the solvent will act in the same way on all three moieties, but the electric field will exert twice as much force on the inner moiety.

COMPARISON OF KRITIKOS-SCHWAN AND MIE SOLUTION GENERATED SOURCE TERM

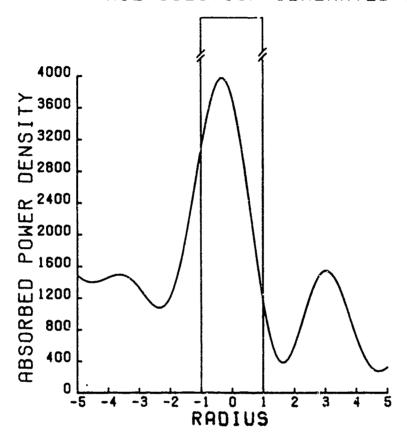


Figure 2.14. Comparison of the Kritikos and Schwan source term used in [5] and the Mie solution generated source term used in this paper. The magnitude of the Kritikos and Schwan source term is $10,000~\text{W/m}^3$. The Mie solution assumes that the incident power is $10~\text{mW/cm}^2$ (field strength = 194.09~V/m), that the frequency is 1000~MHz, that the real part of the relative permittivity is 34.4, that the ionic plus polarization current conductivity = σ' + $\omega \epsilon_0 \epsilon''$ = 0.8~mhos/m, and that the outer boundary of this scattering body is a sphere whose radius is 5 cm.

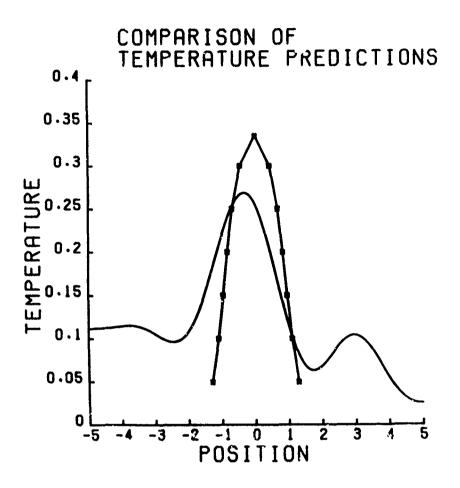


Figure 2.15. Comparison of the Kritikos-Schwan predictions in [5] (marked with an *) and our solution (smooth curve). We assumed, following Kritikos and Schwan, that the blood flow was normal (b = 0.00186 cal/cm³/s) and that the exposure time was 200 s; we used the parameters K = 0.001 cal/cm/°C, $\rho = 1.0$ g/cm³, and c = 1.0 cal/g • °C that were used in [5].

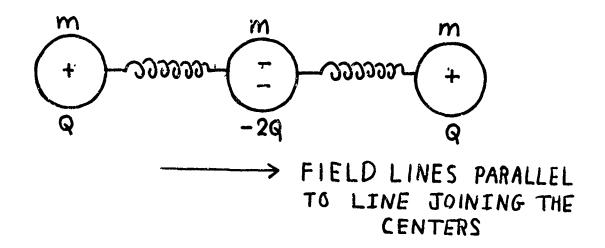


Figure 2.16. Electromagnetic field interaction model for which there would be a nonthermal effect.

3. MATHEMATICAL PRELIMINARIES

3.1. Notation

The variables used in this paper are

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- A_{ij} = dimensionless, coefficient of the radial eigenfunction that is regular at the origin,
- $a_{(\ell,p)}$ = expansion coefficient for the odd regular vector wave functions,
- $a_k^{(m,n)}(t)$ = the temperature decay factor of the solution u associated with the radial eigenvalue $\lambda_{(n,k)}$ and the Legendre transform \mathcal{L}_n^m ,
 - b(r) = the product of the number of grams of blood per gram of tissue per second, the tissue density in grams of tissue per cubic centimeter of tissue, and the specific heat of the blood (typically b = .0122),
 - B_{i} = dimensionless coefficient of the radial eigenfunction that is singular at the origin.
 - $b_{(2,p)}$ = expansion coefficient for the even regular vector wave functions.
- $b_k^{(m,n)}(t)$ = the temperature decay factor of the source term S (associated with the radial eigenvalue $\lambda_{(n,k)}$ and the Legendre transform L_n^m ,

- c(r) = tissue specific heat in calories per gram degree centigrade (typically c = .84),
 - the electric field intensity in volts per meter (10 milliwatts per square centimeter corresponds to 194.087 volts per meter),
 - f = frequency in Hertz,
 - H = Newton cooling constant in calories per square centimeter per degree per second (typically H = .0000572),
 - \vec{H} = magnetic field intensity in Henrys per meter (10 milliwatts per square centimeter corresponds to .5151 Henrys per meter)
 - h_n = spherical Hankel function = j_n iy_n that is used in expanding the electromagnetic fields in Tesseral harmonics,
- $\underline{J}(\underline{S}(\lambda,r),r,n)$ = the radial eigenfunction, used in expanding the temperature, that is nonsingular at the origin,
 - $j_n =$ the spherical Bessel function of order n,
 - K = thermal conductivity in calories per centimeter per degree centigrade per second (typically K = .0012),

- n = the index of the Legendre polynomial used in expanding the field,
- $P_n^m(\cos(\theta))$ = the associated Legendre polynomial,
 - r = the distance from the center of the scatterer in centimeters,
 - R_i = the radius of the ith bounding sphere in centimeters,
 - S = the source term for the heat equation in calories per cubic centimeter per second,
 - $\underline{S}(\lambda,r) = (\lambda \rho(r)c(r) b(r))/K(r),$
 - $\underline{S_{i}}(\lambda) = a \text{ constant value of } \underline{S}(\lambda,r) \text{ occurring when } R_{i-1} < r < R_{i}$
 - t = time in seconds,
 - u = temperature excursion above the ambient temperature,
 - y_n = spherical Bessel function of the second kind,
 - $Y_{n+1/2}$ = half order Bessel function of the second kind (Weber function of order n+1/2),
- $\underline{Y}(\underline{S}(\lambda,r),r,n)$ = the radial eigenfunction, used in expanding the temperature, that is singular at the origin,
 - $Z_{(n,k)}(r)$ = the radial eigenfunction associated with the eigenvalue $\lambda_{(n,k)}$,

 $\alpha_{(\ell,p)}$ = expansion coefficient for the odd singular vector wave functions,

$$\alpha_{i}(\lambda,R,n) = \underline{J}(\underline{S}_{i}(\lambda),r,n),$$

$$\tilde{\alpha}_{i}(\lambda,R,n) = K_{i}[(\partial/\partial r)\underline{J}(S_{i}(\lambda),r,n)]$$
 evaluated at $r = R$,

 $\beta(\ell,p)$ = expansion coefficient for the even singular vector wave functions,

$$\beta_{i}(\lambda,R,n) = \underline{Y}(\underline{S}_{i}(\lambda),R,n),$$

$$\tilde{\beta}_{i}(\lambda,R,n) = K_{i+1}[(\partial/\partial r)\underline{Y}(\underline{S}_{i}(\lambda),r,n)]$$
 evaluated at $r = R$,

$$\Delta_{\mathbf{i}}(\lambda, R_{\mathbf{i}}, \mathbf{n}) = \alpha_{\mathbf{i}+1}(\lambda, R_{\mathbf{i}}, \mathbf{n})\tilde{\beta}_{\mathbf{i}+1}(\lambda, R_{\mathbf{i}}, \mathbf{n}) - \tilde{\alpha}_{\mathbf{i}+1}(\lambda, R_{\mathbf{i}}, \mathbf{n})\beta_{\mathbf{i}+1}(\lambda, R_{\mathbf{i}}, \mathbf{n}),$$

- ε = permittivity in farads per meter,
- θ = spherical coordinate--angle of ray to a point with the positive z-axis,
- λ = eigenvalue associated with radial harmonics,
- ρ = density in grams per cubic centimeter,
- σ = conductivity in ohms per meter,
- τ = dummy variable of integration used in expressing temperature decay factors as a convolution integral,
- ϕ = spherical coordinate of the x-y plane,
- ω = frequency in radians per second,

and

 $x(N_p,T,T_p,T_p)$ = a cutoff function for the temporal envelope of the pulse heating scheme.

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a = partial derivative symbol

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 $B(T_d, T_p, N_p, T_p, T_R, t)$ = the pulse heating scheme temporal envelope function,

 $C_{\rm m}$ = the finite cosine transform,

 L_n^{m} = the Legendre transform,

 $S(T_p, T_p, N_p, T_d, T) = part of a temperature decay factor associated with a heating pattern defined by equation (3.4.14),$

 $T(T_p, T_p, N_p, T_d, T)$ = part of a temperature decay factor associated with a complex pulse heating scheme defined by equation (3.4.15),

and

T(n,k) = the radial transform used in getting expansion coefficients to express a function of r in terms of radial eigenfunctions that satisfy the Newton cooling law boundary condition.

Other notation that is introduced in the text of the paper is defined and used locally.

3.2. Induced Electromagnetic Field Distribution

A new practical method of developing Tesseral harmonic expansion coefficients for the electromagnetic field induced in a penetrable scatterer with spherical symmetry is described here. Our numerical technique will permit us to use the Mie-solution method to determine the response of a body with a large size to a higher frequency radiation than we could with the standard methods described in the references of [1].

The electric field induced in the pth interior region by a wave of the form

$$\dot{E}^{\dagger} = E_0 \exp(-i\omega_0(t-\frac{x}{c})) \qquad (3.2.1)$$

is given in the pth region by

$$\overset{\diamond}{E}_{p} = E_{0} \sum_{\ell=1}^{\infty} i^{\ell} \frac{2\ell+1}{\ell(\ell+1)} \left[\underbrace{a_{\ell,p}}^{\diamond(0,1)} - ib_{\ell,p} \underbrace{a_{\ell,p}}^{\diamond(0,1)} + \alpha_{\ell,p} \underbrace{a_{\ell,p}}^{\diamond(0,3)} \right]$$

$$-i\beta (\ell,p) \stackrel{+(e,3)}{N} (1,\ell)$$
 (3.2.2)

where

$$\overset{+}{M}\overset{(e,j)}{(1,n)} = -\frac{1}{\sin(\theta)} z_n^j (k_p r) P_n^j (\cos(\theta)) \sin(\phi) \dot{\vec{e}}_{\theta}
- z_n^j (k_p r) (d/d\theta) (P_n^j (\cos(\theta))) \cos(\phi) \dot{\vec{e}}_{\phi},$$
(3.2.3)

$$\frac{1}{k_{p}r} = \frac{n(n+1)}{k_{p}r} z_{n}^{j}(k_{p}r) P_{n}^{1}(\cos(\theta))\cos(\phi) \vec{e}_{r}
+ (\frac{1}{k_{p}r})(\partial/\partial r)(rz_{n}^{2}(k_{p}r))(d/d\theta)(P_{n}^{1}(\cos(\theta)))\cos(\phi) \vec{e}_{\theta}
- \frac{1}{((k_{p}r)\sin(\theta))} (\partial/\partial r)(rz_{n}^{j}(k_{p}r)) P_{n}^{1}(\cos(\theta))\sin(\phi) \vec{e}_{\phi}$$
(3.2.5)

and

where

$$k_p = sign(\omega) \sqrt{\frac{\mu \epsilon \omega^2 + \sqrt{\mu^2 \epsilon^2 \omega^4 + \mu^2 \sigma^2 \omega^2}}{2}} + i(\sqrt{\frac{-\mu \epsilon \omega^2 + \sqrt{\mu^2 \epsilon^2 \omega^4 + \mu^2 \sigma^2 \omega^2}}{2}})$$
 (3.2.7)

In (3.2.3) - (3.2.6) functions P_n^1 are the associated Legendre polynomials and

$$h_n^1(z) = (j_n + iy_n)(z)$$
 if $j = 3$ $z_n^j(z) = j_n(z)$ if $j = 0$ (3.2.8)

where j_n and y_n are respectively the spherical Bessel functions of the first and second kind. Part of the difficulty is that we cannot use (3.2.7) to compute h_n^1 even if we know j_n and y_n exactly. For example, z = u + iv implies that

$$h_0^1(z) = (1/z)[\sin(u)(\cosh(v) - \sinh(v))$$

+ $i \cos(u)(\sinh(v) - \cosh(v))]$ (3.2.9)

which is uncomputable on a digital computer if v is large enough so that $\cosh(v)$ and $\sinh(v)$ are indistinguishable.

A better way is the use of the formula

$$h_n^1(z) = i^{-n-1}z^{-1}\exp(iz)\sum_{k=0}^{n}(n+1/2,k)(-2iz)^k,$$
 (3.2.10)

coupled with the Hankel symbol formula,

$$(n+1/2,k) = \frac{(n+k)!}{k!(n-k)!} = \frac{(n+k)(n+k-1)\cdots(n+1)n(n-1)\cdots(n-(k-1))}{k!}$$

$$= \prod_{i=1}^{k} \left(\frac{(n-(k-2i))(n-(k-(2i-1)))}{i} \right),$$
(3.2.11)

when the complex number z is such that $(n+1/2,k)(-2iz)^k$ are of such a size that round-off error is not encountered in the computation of (3.2.10).

The reader can verify (3.2.10) by induction using the three-term recursion formula

$$h_{n+1}^1 = \frac{(2n+1)}{z} h_n^1 - h_{n-1}^1$$
 (3.2.12)

is satisfied and by showing that (3.2.10) is true for n = 0 and n = 1

since from (3.2.8) we know that

$$h_0^1(z) = \frac{\sin(z)}{z} + i(-\frac{\cos(z)}{z}),$$
 (3.2.13)

and

$$h_1^1(z) = \left(\frac{\sin(z)}{z^2} - \frac{\cos(z)}{z}\right) + i\left(\frac{\cos(z)}{z^2} - \frac{\sin(z)}{z}\right).$$
 (3.2.14)

For intermediate values of z, another method must be sed to compute $h_n^1(z)$. We observe that equation (3.2.12) implies that

$$\frac{h_{n-2}^{1}(z)}{h_{n-1}^{1}(z)} = \frac{2n-1}{z} - \frac{h_{n}^{1}(z)}{h_{n-1}^{1}(z)}.$$
 (3.2.15)

The basic idea is to write

$$a_{n+1/2} = \frac{h_{n-1}^{1}(z)}{h_{n}^{1}(z)} = \frac{H_{(n-1+1/2)}^{1}(z)}{H_{(n+1/2)}^{1}(z)}$$
(3.2.16)

and then observe that equations (3.2.15) and (3.2.16) imply that

$$a_{(n+1/2)} = \frac{2(n+1)-1}{7} - \frac{1}{a_{(n+1+1/2)}}$$
 (3.2.17)

Hence, v = n + 1/2 and n = v - 1/2 and equation (3.2.17) imply that

$$a_{v} = \frac{2v}{z} - \frac{1}{a_{v+1}}$$
 (3.2.18)

Thus, from (3.2.16) we get immediately a continued fraction expansion

$$a_v = \frac{2v}{z} - \frac{1}{\frac{2(v+1)}{z} + \frac{1}{a_{v+2}}}$$
 (3.2.19)

et cetera, which by the following Lemma is always convergent.

Lemma (Wall [10], p. 50). We have uniform convergence of the continued fraction,

$$c = b_0 + \frac{a_1}{b_1 + \frac{a_2}{b_2 + \frac{a_3}{b_4 + \cdots}}}$$

$$b_2 + \frac{a_3}{b_4 + \cdots},$$
(3.2.20)

if there exists constants $g_p \epsilon(0,1)$ such that

$$\left| \frac{a_{p+1}}{b_p b_{p+1}} \right| \le (1 - g_p) g_{p+1}. \tag{3.2.21}$$

In our situation

$$b_0 = \frac{2v}{7}$$
 (3.2.22)

$$b_p = \frac{2(v+p)}{z}$$
 $p = 1,2,...$ (3.2.23)

and

$$a_p = 1$$
 $p = 1, 2, ...$ (3.2.24)

Thus, for every z there is an $N_z > 0$ such that if $p > N_z$ then

$$\left| \frac{a_{p+1}}{b_p b_{p+1}} \right| \leq \frac{|z|^2}{4(\nu+p)(\nu+p+1)} \leq (1-g_p)g_{p+1}$$
 (3.2.25)

provided that N_z is such that $(N_z+v) \ge |z|$ and $g_p = 1/2$ for all p. Thus in view of the Lemma the continued fraction expansion theoretically converges for all $z \ne 0$.

The idea then is not to compute the spherical Bessel functions of the second kind y_n at all, but rather use a direct method for obtaining the h_n^1 . Observe that

$$h_{n}^{1} = \left(\frac{h_{n}^{1}}{h_{n-1}^{1}}\right) \left(\frac{h_{n-1}^{1}}{h_{n-2}^{1}}\right) \cdots \left(\frac{h_{1}^{1}}{h_{0}^{1}}\right) \frac{(-i)\exp(iz)}{z}$$
(3.2.26)

The functions $\xi_n(z)$ used in the expansion are successfully computed by the methods of Lentz [8].

- 3.3. Heat Operator Eigenvalues and Eigenfunctions for a Newton Cooling Law Boundary Condition
- 3.3.1. The Radiative Heat Transfer Problem. From the E field determination of the preceding section, we develop an expression for a source

$$S = div(E \times H)/(10^6 \times 4.184)$$
 (3.3.1)

of internal energy generation which is used as a term in the heat equation,

$$\rho c \frac{\partial u}{\partial t} - \operatorname{div}(K \operatorname{grad}(u)) + bu = S, \qquad (3.3.2)$$

where ec is the product of density and specific heat, b is a blood-flow cooling term, and K is the thermal conductivity. Assume that the scattering body is a union of material regions bounded by spheres $r = R_j$ for i in $\{1, \ldots, N\}$ (with $N \le 6$ in our computer program) and

$$0 = R_0 < R_1 < ... < R_N$$
 (3.3.3)

Assume that $\rho(r)$, c(r), and K(r) have the constant values ρ_i , c_i , K_i respectively for $R_{i-1} < r < R_i$. Then for $R_{i-1} < r < R_i$ equation (3.2) may be written

$$\rho_{i}c_{i}(\partial/\partial t)u = K_{i}\left[\frac{1}{r^{2}}\frac{\partial}{\partial r}\left(r^{2}\frac{\partial u}{\partial r}\right)\right] + \frac{1}{r^{2}\sin(\theta)}\left[\frac{\partial}{\partial \theta}\left(\sin(\theta)\frac{\partial u}{\partial \theta}\right)\right] + \frac{1}{\sin(\theta)}\frac{\partial^{2}u}{\partial \phi^{2}} - b_{i}u + S, \qquad (3.3.4)$$

where the initial condition is that

$$u(r,\theta,\phi,0) = 0,$$
 (3.3.5)

continuity of temperature and heat flux implies

$$\lim_{\varepsilon \to 0} u(R_{i} - \varepsilon, \theta, \phi, t) = \lim_{\varepsilon \to 0} u(R_{i} + \varepsilon, \theta, \phi, t), \qquad (3.3.6)$$

and

$$\lim_{\varepsilon \to 0} K_{i}(\partial/\partial r)u(R_{i}-\varepsilon,\theta,\phi,t) = \lim_{\varepsilon \to 0} K_{i+1}(\partial/\partial r)u(R_{i}+\varepsilon,\theta,\phi,t), \quad (3.3.7)$$

and the Newton cooling law implies that

$$K_N(\partial/\partial r)u(R_N, \partial, \phi, t) + Hu(R_N, \partial, \phi, t) = 0.$$
 (3.3.8)

We define the finite cosine transform of the temperature excursion $u(r,\theta,\phi,t)$ by the rule,

$$(C_{\mathsf{m}}\mathsf{u})(\mathsf{r},\theta,\mathsf{t}) = (1/\pi) \int_{-\pi}^{\pi} \mathsf{u}(\mathsf{r},\theta,\phi,\mathsf{t}) \cos(\mathsf{m}\phi) \mathsf{d}\phi, \qquad (3.3.9)$$

for positive integers m and

$$(C_0 u)(r,\theta,t) = (1/2\pi) \int_{-\pi}^{\pi} u(r,\theta,\phi,t) d\phi.$$
 (3.3.10)

We define the Legendre transform operator E_{n}^{m} on the temperature excursion $u(r,\theta,\phi,t)$ by the rules,

$$(L_{n}^{m}u)(r,\phi,t) =$$

$$\left(\frac{2n+1}{1}\right)\left(\frac{(n-m)!}{(n+m)!}\right)\int_{0}^{\pi}u(r,\theta,\phi,t)P_{n}^{m}(\cos(\theta))\sin(\theta)d\theta \tag{3.3.11}$$

and

$$L_{n}^{0}u(r,\phi,t) = \left(\frac{2n+1}{1}\right)\int_{0}^{\pi}u(r,\theta,\phi,t)P_{n}(\cos(\theta))\sin(\theta)d\theta. \qquad (3.3.12)$$

Thus, if we combine (3.3.9), (3.3.10), (3.3.11), (3.3.12), and (3.3.4) we see that if ρ , c, and K are simply functions of r, then

$$(\partial/\partial t) L_{n}^{m} C_{m} u = (\frac{1}{\rho cr}) \{ (\partial/\partial r) (r^{2} K(r)) (\partial/\partial r) L_{n}^{m} C_{m} u$$

$$- K(r) n (n+1) L_{n}^{m} C_{m} u \} - (b/(\rho)) L_{n}^{m} C_{m} u + L_{n}^{m} C_{m} (S/\rho c)$$

$$(3.3.13)$$

Let us attempt to write

$$(L_{n}^{m}C_{m}u)(r,t) = \sum_{k=1}^{\infty} a_{k}^{(m,n)}(t)Z_{(n,k)}(r),$$
 (3.3.14)

and

$$L_n^m c_m(S/pc)(r,t) = \sum_{k=1}^{\infty} b_k^{(m,n)}(t) Z_{(n,k)}(r),$$
 (3.3.15)

where

$$(d/dr)(K(r)r^{2}(d/dr))Z_{(n,k)}(r) +$$

$$\{\lambda_{(n,k)}r^{2}\rho c - Kn(n+1) - br^{2}\}Z_{(n,k)}(r) = 0,$$
(3.3.16)

$$\lim_{\epsilon \to 0} Z_{(n,k)}(R_i^{+\epsilon}) = \lim_{\epsilon \to 0} Z_{(n,k)}(R_i^{-\epsilon})$$
 (3.3.17)

$$\lim_{\epsilon \to 0} K(R_i + \epsilon)(Z_{(n,k)})'(R_i + \epsilon) = \lim_{\epsilon \to 0} K(R_i - \epsilon)(Z_{(n,k)})'(R_i - \epsilon) \qquad (3.3.18)$$

for

$$i = 1, ..., N-1$$

where the $\lambda_{(n,k)}$ are positive numbers for which

$$(Z_{(n,k)})'(R_N) + (H/K_N)Z_{(n,k)}(R_N) = 0.$$
 (3.3.19)

Thus, we conclude that

$$a_k^{(m,n)'}(t) + \lambda_{(n,k)} a_k^{(m,n)}(t) = b_k^{(m,n)}(t)$$
 (3.3.20)

and consequently that

$$a_k^{(m,n)}(t) = \int_0^t \exp(-\lambda_{(n,k)}(t-\tau))b_k^{(m,n)}(\tau)d\tau.$$
 (3.3.21)

By defining for every function g(r)

$$T_{(n,k)}(g) = \frac{\int_{0}^{R_{N}} g(r)Z_{(n,k)}(r)(\rho c)(r)r^{2}dr}{\int_{0}^{R_{N}} |Z_{(n,k)}(r)|^{2}(\rho c)(r)r^{2}dr}$$
(3.3.22)

we see that

$$b_k^{(m,n)}(t) = T_{(n,k)} L_h^m C_m(\frac{S}{\rho c}).$$
 (3.3.23)

3.3.2. <u>Eigenvalue Determination</u>. We wish to describe here a computer algorithm for computing the $\lambda_{(n,k)}$ and the $Z_{(n,k)}(r)$ when ρ , c, b, and K are nonnegative piecewise constant functions. While this is trivial when b(r) is a constant function, the problem becomes interesting when b(r) is positive in some intervals (R_{i-1},R_i) and is identically zero in others.

To begin with we define

$$\underline{S}(\lambda,r) = \frac{\lambda \rho(r)c(r) - b(r)}{K(r)}$$
 (3.3.24)

and we obtain in each interval (R_{i-1},R_i) one of three different classes of solutions of the problem (3.3.16) - (3.3.19) depending on whether or not $\underline{S}(\lambda_{(n,k)},r)$ is uniformly positive, zero, or negative in this interval. We, therefore, write

$$Z(r,\lambda) = A_{i}\underline{J}(\underline{S}(\lambda,r),r,n) + B_{i}\underline{Y}(\underline{S}(\lambda,r),r,n)$$
 (3.3.25)

and require that

$$\lim_{r \to 0} \frac{A_1 J(S(\lambda, r), r, n)}{r^n} = 1$$
 (3.3.26)

and

$$B_1 = 0$$
 (3.3.27)

In general for $\underline{S}(\lambda,r) > 0$ we have setting

$$z = r \sqrt{\frac{\lambda \rho c - b}{K}} = r \sqrt{\frac{S(\lambda, r)}{N}}$$
 (3.3.28)

the fact that (3.3.16) is equivalent to

$$r^{2}(d/dr)^{2}Z_{n} + 2r(d/dr)Z_{n} + r^{2}\underline{S}(\lambda,r)Z_{n} - n(n+1)Z_{n} = 0$$
 (3.3.29)

and if we change variables by the rule

$$z = \sqrt{S(\lambda, r)r}$$
 (3.3.30)

and observe that

$$\frac{d}{dr} = \frac{dz}{dr} \frac{d}{dz} , \qquad (3.3.31)$$

we see that if

$$Z_{(n,k)}(r) = W(z),$$
 (3.3.32)

then

$$z^2W'' + 2zW' + (z^2 - (n(n+1)W = 0, (3.3.33))$$

which implies that in (R_{i-1}, R_i) we have

$$W(z) = A_{ij}_{n}(z) + B_{iy}_{n}(z),$$
 (3.3.34)

where

$$j_{n}(z) = \begin{bmatrix} \frac{z^{n}}{\prod_{k=1}^{n} (2k-1)} \end{bmatrix} \sum_{m=0}^{\infty} \frac{(-1)^{m} (z^{2}/2)m}{\prod_{k=0}^{m} (2k+1+2n)}.$$
 (3.3.35)

Thus, to make (3.3.34) consistent with (3.3.26) when i = 1, we must have

$$A_{1} = 1/\{ \begin{pmatrix} n+1 \\ \pi \\ k=1 \end{pmatrix} (2k-1) (\sqrt{\underline{S}(\lambda,r)})^{n} \}.$$
 (3.3.36)

If $\underline{S}(\lambda,r) = 0$ we have

$$\underline{J(S(\lambda,r),r,n)} = r^n \qquad (3.3.37)$$

and

$$\underline{Y}(\underline{S}(\lambda,r),r,n) = r^{-n-1} \tag{3.3.38}$$

If $\underline{S}(\lambda,r) = \underline{S}_{i}(\lambda) < 0$ in (R_{i-1},R_{i}) we have in this interval

$$\underline{J}(\underline{S}(\lambda,r),r,n) = \underline{J}(\underline{S}_{i}(\lambda),r,n)$$

$$= \sum_{m=0}^{\infty} \frac{(\left|\underline{S}_{i}(\lambda)\right| r^{2/2})^{m} (\sqrt{\left|\underline{S}_{i}(\lambda)\right| r})^{n}}{m! \left[\prod_{k=1}^{m} (2k+1) + 2n\right] \left[\prod_{k=0}^{n} (2k+1)\right]},$$
 (3.3.39)

and

$$\underline{Y}(\underline{S}(\lambda,r),r,n) = \underline{Y}(\underline{S}_{i}(\lambda),r,n)$$

$$= \left(\sum_{m=0}^{\infty} \frac{(\left| \underline{S}_{i}(\lambda) \right| r^{2}/2)^{m}}{\sum_{k=1}^{m} (2k-1-2n)} \left[\frac{\prod_{k=0}^{n} (2k-1)}{\left(\sqrt{\left| \underline{S}_{i}(\lambda) \right| r}\right)^{n+1}} \right]. \tag{3.3.40}$$

The functions defined by (3.3.39) and (3.3.40) do not satisfy Bessel's differential equation, but they may be expressed in terms of Bessel functions of a purely imaginary argument. This is the way they are developed in our computer program.

We begin our search for eigenvalues by finding the unique solution $Z_n(r,\lambda)$ of equation (3.3.29) which satisfies the condition

$$\lim_{r \to 0} \frac{Z_n(r,\lambda)}{r^n} = 1$$
 (3.3.41)

and the requirement that $Z_n(r,\lambda)$ and $K(r)(\partial/\partial r)Z_n(r,\lambda)$ be continuous on $[0,R_N)$. We then define a function of λ by the rule,

$$F_{n}(\rho,c,K,\lambda) = \lim_{r \to R_{N}} \{K_{N}(\partial/\partial r)Z_{n}(r,\lambda) + HZ_{n}(r,\lambda)\}.$$
 (3.3.42)

where R_N is the radius of the bounding sphere of the scattering body. We then use a root-finding routine to find for each n an ascending sequence,

$$k \rightarrow \lambda (n,k)$$
 (3.3.43)

of positive real numbers such that $\lambda = \lambda_{(n,k)}$ implies that

$$F_n(\rho,c,K,\lambda) = 0.$$
 (3.3.44)

These numbers $\lambda_{(n,k)}$ are the eigenvalues associated with the rest transfer problem and have the units of reciprocal seconds. The numbers $t_{(n,k)} = 1/\lambda_{(n,k)}$ estimate the time needed for the (n,k)th mode of the temperature solution to decay to (1/e) times its original value.

3.3.3. <u>Eigenfunction Computation</u>. We assume here that the eigenvalue $\lambda = \lambda_{(n,k)}$ that we are using to develop the radial eigenfunction is known and use the initial condition (3.3.26) and the regularity conditions (3.3.17) and (3.3.18) to uniquely determine the eigenfunction $Z_{(n,k)}$.

A first step in carrying this out is the determination of the eigenfunction coefficients A_i and B_i used in expressing the eigenfunction $Z(r,\lambda)$ by the relation (3.3.25). We observe that A_i and B_i are given by equations (3.3.26) and (3.3.27) and that if A_i and B_i are known, then

$$A_{i+1} = \frac{\det \begin{bmatrix} A_{i}\alpha_{i}(\lambda, R_{i}, n) + B_{i}\beta_{i}(\lambda, R_{i}, n) & \beta_{i+1}(\lambda, R_{i}, n) \\ A_{i}\tilde{\alpha}_{i}(\lambda, R_{i}, n) + B_{i}\tilde{\beta}_{i}(\lambda, R_{i}, n) & \tilde{\beta}_{i+1}(\lambda, R_{i}, n) \end{bmatrix}}{\Delta_{i}(\lambda, R_{i}, n)}$$
(3.3.45)

$$B_{i+1} = \frac{\det \begin{bmatrix} \alpha_{i+1}(\lambda, R_i, n) & A_i \alpha_i(\lambda, R_i, n) + B_i \beta_i(\lambda, R_i, n) \\ \tilde{\alpha}_{i+1}(\lambda, R_i, n) & A_i \tilde{\alpha}_i(\lambda, R_i, n) + B_i \tilde{\beta}_i(\lambda, R_i, n) \end{bmatrix}}{\Delta_i(\lambda, R_i, n)}$$
(3.3.46)

where

$$\alpha_{i}(\lambda,r,n) = \underline{J}(\underline{S}_{i}(\lambda),r,n), \qquad (3.3.47)$$

$$\tilde{\alpha}_{i}(\lambda,r,n) = K_{i}(\partial/\partial r)J(S_{i}(\lambda),r,n), \qquad (3.3.48)$$

$$\beta_{i}(\lambda,r,n) = \underline{Y}(S_{i}(\lambda),r,n), \qquad (3.3.49)$$

and

$$\tilde{\beta}_{i}(\lambda,r,n) = K_{i}(\partial/\partial r)\underline{Y}(\underline{S}_{i}(\lambda),r,n), \qquad (3.3.50)$$

defines the entries in the numerators of (3.3.45) and (3.3.46) and where

$$\Delta_{\mathbf{i}}(\lambda, R_{\mathbf{i}}, \mathbf{n}) = \alpha_{\mathbf{i}+1}(\lambda, R_{\mathbf{i}}, \mathbf{n})\tilde{\beta}_{\mathbf{i}+1}(\lambda, R_{\mathbf{i}}, \mathbf{n})$$

$$-\tilde{\alpha}_{\mathbf{i}+1}(\lambda, R_{\mathbf{i}}, \mathbf{n})\beta_{\mathbf{i}+1}(\lambda, R_{\mathbf{i}}, \mathbf{n})$$
(3.3.51)

defines the determinant of the matrix multiplying the column vector whose entries are A_{i+1} and B_{i+1} . Thus, the relations (3.3.45) and (3.3.46) determine A_i and B_i for all i $\in \{1,\ldots,N\}$. Consequently, if $\lambda = \lambda_{(n,k)}$ the eigenfunction $Z_{(n,k)}(r)$ has for r in (R_{i-1},R_i) the explicit representation

$$Z_{(n,k)}(r) = A_{i}\underline{J}(\underline{S}_{i}(\lambda),r,n) + B_{i}\underline{Y}(\underline{S}_{i}(\lambda),r,n)$$
 (3.3.52)

where the form of the functions \underline{J} and \underline{Y} depend on whether or not

$$\underline{S}_{i}(\lambda) = \frac{\lambda \rho(r)c(r) - b(r)}{K(r)} (R_{i-1} < r < R_{i})$$
 (3.3.53)

is positive, zero, or negative in the manner indicated in Section 3.2.

3.4. Details of the Temperature Computation Including Complex Pulse Heating Schemes

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3.4.1. Series Expansion of the Temperature. In this section we describe the computational procedure for determining the solution u of equation (3.3.2) under the assumption that we know the eigenvalues $\lambda_{(n,k)}$ and eigenfunctions $Z_{(n,k)}$ described in Section (3.3.1). Now that this is done we express the solution $u(r,\theta,\phi,t)$ by the series

$$u(r,\theta,\phi,t) = \frac{\sum_{k=1}^{\infty} \sum_{n=0}^{\infty} \sum_{m=0}^{n} a_{k}^{(m,n)}(t) P_{n}^{m}(\cos(\theta)) \cos(m\phi) Z_{(n,k)}(r)}{(s,k)^{(n,k)}}$$

where $a_k^{(m,n)}(t)$ is defined by equation (3.21) and

$$a_{k}^{(m,n)}(t) = (T_{(n,k)}L_{n,m}^{m}U)(t)$$

$$= \int_{0}^{t}b_{k}^{(m,n)}(\tau)\exp(-\lambda_{(n,k)}(t-\tau))d\tau$$
(3.4.2)

with the operators $T_{(n,k)}$, L_n^m , and C_m being defined by equations (3.3.22), (3.3.11) - (3.3.12), and (3.3.9) - (3.3.10) respectively. Almost all of the computing time is taken up in the computation of the coefficients $b_k^{(m,n)}(t)$, defined by equation (3.3.23), that are used in expanding the source function (S/pc). While each of these represents the result of a triple integration, the total running time is still only between 3 and 4 min on an IBM 360 for results which are good to within the capabilities of experimental measurement.

3.4.2. <u>Complex Pulse Heating Scheme</u>. We wish to consider a pulse heating scheme (e.g., Figure 3.4.1) in which a group of pulses with a duty time and period followed by a period of quiescence defines a function that is periodic with respect to the total duty time of the pulse group plus the length of time of the quiescent period.

More precisely the time profiles we consider include time harmonic radiation whose basic frequency is that of a radar transmitter multiplied by a function of time $(T_d, T_p, N_p, T_p, T_R, t)$ defined for $0 < T_d < T_p \le N_p T_p \le T_p$ and $T_R > 0$ by the initialization rule

$$B(T_{d},T_{p},N_{p},T_{\underline{p}},T_{R},t) = \begin{cases} 1 & 0 \leq t \leq T_{d} \text{ and } t \leq T_{R}, \\ 0 & T_{d} < t < T_{p}, \end{cases}$$

$$0 & N_{p}T_{p} < t < T_{\underline{p}}, \end{cases}$$

$$(3.4.3)$$

and the periodicity rules,

$$B(T_d, T_p, N_p, T_p, T_R, t+T_p) = B(T_d, T_p, N_p, T_p, T_R, t)$$
 (3.4.4)

if $t + \overline{r}_p \leq T_R$ and $t + T_p \leq N_p \overline{r}_p$ and

$$B(T_d,T_p,N_p,T_{\underline{p}},T_R,t+T_{\underline{p}}) = B(T_d,T_p,N_p,T_{\underline{p}},T_R,t)$$
 (3.4.5)

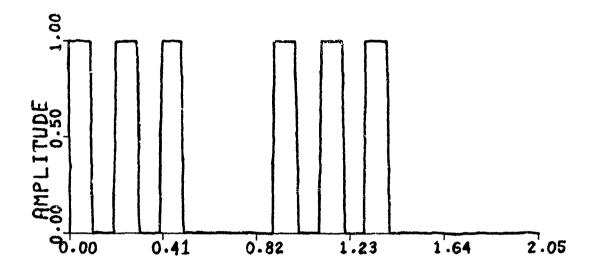
if $t + T_p \leq T_R$, where

 T_d = the pulse duration,

 T_p = the intrapulse group period,

 $N_{\rm p}$ = the number of pulses per group,

OVERALL PICTURE



AMPLIFIED PICTURE

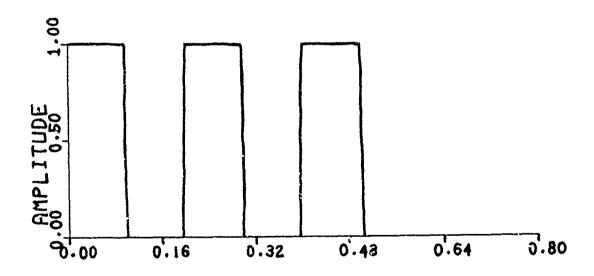


Figure 3.4.1. Complex pulse heating pattern typical of radar emissions with a burst of three pulses followed by a quiet period and with the pattern being repeated periodically. In the above figure we have N $_p$ = 3 pulses per group, T $_d$ = .1 millisecond (ms), T $_p$ = .2 ms, T $_p$ = .9 ms, T $_R$ = 1.6 ms, and t = 2.05 ms.

 T_p = the period,

 T_R = the time that the source has been on,

and

t = the time of observation of the radiation effect.

The basic idea is to assume that T_d is large enough that the continuous-wave solution accurately predicts the electromagnetic field distribution and consequently the source term of the heat transfer equation. That is to say, if

$$b_k^{(m,n)}(t) = \underline{b}_k^{(m,n)} B(T_d, T_p, N_p, T_p, T_R, t),$$
 (3.4.6)

then $T = T_R$ implies that

$$a_{k}^{(m,n)}(t) = \underline{b}_{k}^{(m,n)} \begin{cases} [T/T_{\underline{p}}] & N_{\underline{p}} \\ \sum_{k=1}^{T} \sum_{j=1}^{T} \int_{j=1}^{(j-1)T_{\underline{p}} + (k-1)T_{\underline{p}}} + T_{\underline{d}} \\ \exp(-\lambda(t-\tau))d\tau \\ (j-1)T_{\underline{p}} + (k-1)T_{\underline{p}} \end{cases}$$

$$+ \sum_{\substack{j=1 \\ j=1}}^{\min([(T - [T/T_{\underline{p}}]T_{\underline{p}})/T_{\underline{p}}], N_{\underline{p}})} \begin{bmatrix} [T/T_{\underline{p}}]T_{\underline{p}} + (j-1)T_{\underline{p}} + T_{\underline{d}} \\ \exp(-\lambda(t-\tau)d\tau \\ [T/T_{\underline{p}}]T_{\underline{p}} + (j-1)T_{\underline{p}} \end{bmatrix}$$

where min is an abbreviation for the minimum function and [] denotes the greatest integer function([x] denotes the largest integer not exceeding x).

Some changes of variables and introduction of notation will make it easier to develop computer code to evaluate the preceding three integrals. We therefore define

$$r(k,j) = (j-1)T_p + (k-1)T_p$$
, (3.4.8)

$$s(j) = [T/T_{\underline{p}}]T_{\underline{p}} + (j-1)T_{\underline{p}},$$
 (3.4.9)

$$M(T,N_p) = \min(([T-[T/T_p]T_p]/T_p],N_p), \qquad (3.4.10)$$

$$\underline{t}(T,N_p,T_p,T_{\underline{p}}) = M(T,N_p)T_p + [T/T_{\underline{p}}]T_{\underline{p}}, \qquad (3.4.11)$$

$$\chi = \chi(N_p, T, T_p, T_p) = \{ \begin{cases} 0 & \text{if } \left[\left(T - \left[T / T_p \right] T_p \right) / T_p \right] \ge N_p, \\ 1 & \text{otherwise} \end{cases}$$
 (3.4.12)

$$\overline{t}(T,N_p,T_p,T_{\underline{p}}) = \min (T,\underline{t}(T,N_p,T_p,T_{\underline{p}})) + T_dx(N_p,T,T_{\underline{p}},T_p), \quad (3.4.13)$$

$$S(T_p,T_p,N_p,T_d,T) = \sum_{k=1}^{\lfloor T/T_p \rfloor} \sum_{j=1}^{N_p} \exp(\lambda r(k,j)) =$$

$$\left\{\frac{\exp(\lambda N_{p}T_{p})-1}{\exp(\lambda T_{p})-1}\right\}\left\{\frac{\exp(\lambda [T/T_{p}]T_{p}]-1}{\exp(\lambda T_{p})-1}\right\},$$
(3.4.14)

and

$$T(T_p,T_p,N_p,T_d,T) = \sum_{j=1}^{M(T,N_p)} \exp(\lambda s(j)) =$$

$$\exp(\lambda([T/T_{\underline{p}}]T_{\underline{p}}))(\frac{\exp(\lambda M(T,N_{\underline{p}})T_{\underline{p}})-1}{\exp(\lambda T_{\underline{p}})-1}). \tag{3.4.15}$$

Putting all this together we find that

$$a_{k}^{(\pi,n)}(t) = \underline{b}_{k}^{(m,n)} \left\{ \exp(-\lambda t) \frac{\exp(\lambda T_{d})^{-1}}{\lambda} \left\{ S\left(T_{p}, T_{\underline{p}}, N_{p}, T_{d}, T\right) + T\left(T_{p}, T_{\underline{p}}, N_{p}, T_{d}, T\right) \right\}$$

$$+ \exp(\lambda \overline{t}(T, N_{p}, T_{p}, T_{\underline{p}})) - \exp(\lambda \underline{t}(T, N_{p}, T_{p}, T_{\underline{p}})) + \exp(-\lambda t) \frac{\exp(\lambda \overline{t}(T, N_{p}, T_{p}, T_{\underline{p}})) - \exp(\lambda \underline{t}(T, N_{p}, T_{p}, T_{\underline{p}}))}{\lambda} \right\}.$$

This completes the discussion of our temperature computation method.

3.5. Simulated Biostructures

3.5.1. Description of Structures to be Studied. In a previous paper [2], the authors made a study of the thermal response of a ball of muscle-equivalent material; this study is extended in this paper to multi-layer simulated biological structures. In [2] analytical results were compared with measurements made with Vitek-Model 101 Electrothermia monitor; in this paper we compare the shape of the thermal response curve with the electromagnetic power density curve which serves as a source term for the heat equation. • We study a one-layer structure with blood flow at a higher frequency (4.5 GHz) than was considered in [2], three-layer simulated fetal structures with and without blood flow, and six-layer simulated cranial structure with blood flow.

For one-layer structures Figures 2.2.2-2.2.4 show the agreement between theory and experimental measurement; from the results described in Figure 3.5.1 we see that there are striking resonance effects in a simply one-layer structure exposed to 4.5-GHz radiation; we demonstrate by the results shown in Figures 3.5.2 and 3.5.3 that the temperature distribution curve has a shape very similar to that of a power density distribution—particularly when the exposure time is short.

Next we treat simulated fetal structures. N. J. Edwards [4] observation that microwave heating of rat embryos can cause teratogenic effects suggests that a quantitative analysis of a simulated fetal structure's response to microwave radiation may assist in the assessment of the potential hazard of a source of microwave radiation. We use a three-layer model whose layers consist of fetal tissue, amniotic fluid, and maternal tissue is simulating the response of the fetus to microwave radiation. Figure 3.5.4 shows the power density across the diameter of the three-layer structure; this diameter coincides with the z-axis of a coordinate system whose origin is the center of

sphere; the wave is assumed to propagate in the direction of the positive z-axis. The temperature distributions across the parts of the x, y, and z-axes of the structure within its interior after a 1-hr exposure are given in Figures 3.5.5-3.5.7 where we include blood flow. Figures 3.5.8-3.5.15 show how this temperature distribution changes as exposure time increases when we don't assume removal of heat by blood flow.

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Finally we consider a six-layer simulated cranial structure exposed to microwave radiation. Figure 3.5.16 shows the power density across a six-layer simulated structure exposed to 800-MHz radiation. Figures 3.5.17 and 3.5.18 show the thermal response of the structure to 800-MHz microwave radiation for 30-s and 1-min exposures.

3.5.2. Microwave Heating of a Muscle-Equivalent Sphere. In this section we study the manner in which a microwave-induced temperature profile is smoothed as exposure time increases. We conclude that short-time temperature measurements would serve as an adequate means of validating computer predictions of internal field distributions even when there are resonance effects which cause the power density profile (e.g., Figure 3.5.1) to have many relative maximums and minimums; this particular assertion is valid for continuous-wave exposure, but is not established for a general pulse exposure scenario. The thermal response for 5-s and 1-min exposures is shown in Figures 3.5.2 and 3.5.3. The electromagnetic field strength for the results portrayed in Figures 3.5.1-3.5.3 was 194.09 V/m or 10 mW/cm².

Table 3.5.1 defines the parameters used in making the computer runs.

TABLE 3.5.1. PARAMETERS FOR ONE-LAYER MUSCLE EQUIVALENT SPHERE EXPOSED TO 4500-MHZ RADIATION

ELECTRICAL PROPERTIES

Tissue type	Radius of bounding sphere (cm) Relative permittivity		ittivity	Conductivity (mhos/meter)	
Muscle	3.3	48.25		2.75	
Tissue type	Blood flow cooling				
Muscle	.00126	1.050	.883	.00186	

3.5.3. Microwave Heating of a Simulated Fetal Structure. To estimate the potential hazard of a source of microwave radiation, we have made a simulated fetal structure comprised of three tissue regions delimited by concentric spheres. The parameters used in the computer runs are given in Table 3.5.2. The field strength used in the runs was 194.09 v/m, which is equivalent to 10 mW/cm^2 .

TABLE 3.5.2. PARAMETERS DEFINING A SIMULATED FETAL STRUCTURE EXPOSED TO 1000-MHz RADIATION

ELECTRICAL PROPERTIES

Tissue type	Radius of bounding sphere (cm)	Relative permittivity	Conductivity (mhos/meter)	
Fetal	1.6	50.5	1.65	
Amniotic fluid	2.8	72.0	2.90	
Maternal	3.3	50.5	1.65	

THERMAL PROPERTIES (centimeter-gram-second units)

Tissue type	Thermal conductivity	Density	Specific heat	Blood flow cooling
Fetal	.00126	1.050	.883	.00186
Amniotic fluid	.00124	1.007	.998	.00000
Maternal	.00126	1.050	.883	.00186

We get some qualitative information (e.g., the shielding effect of the amniotic fluid) about the vulnerability of the fetus to microwave exposure from the computer results for the simple model given in this paper. Since Edwards [4] suggests that thermal pulses can affect cell cycles and that there are teratogenic effects associated with elevated fetal temperatures, it would probably be valuable to carry out this analysis for a whole-body model and use (1) the smallest fetal temperature known to cause abnormal fetal development and (2) the computer model for predicting fetal temperature excursions as a definitive way of stating that a particular source of microwave radiation is a potential health hazard.

Figure 3.5.4 shows the power density across a simulated fetal structure when the exposure was carried out in the manner described in Figure 2.1. Figures 3.5.5-3.5.7 show the thermal response of the simulated fetal structure after a 1-hr exposure, and Figures 3.5.8-3.5.15 show how the temperature distribution across the structure changes with time when there is no removal of heat by an autothermal regulatory process. While our autothermal regulatory process model is based on actual physiological parameters relating to blood flow, it can at best be considered phenomenological since we have not modeled the details of the flow of blood through vessels in the tissue and have in essence only added a dissipative term to the heat equation. However, Figures 3.1.5-3.5.7 suggest that there is in the blood flow case a net heating of the amniotic fluid due to the absence of autothermal regulation.

3.5.4. Microwave Heating of a Simulated Cranial Structure. In this section we study the response of a simulated cranial structure to microwave radiation. The manner in which the structure is exposed is described in Figure 2.1. The power density in the simulated cranial structure is shown in Figure 3.5.16. The observed thermal response after 30-s and 1-mir exposures to 800-MHz radiation is described in Figures 3.5.17 and 3.5.13.

The parameters used in carrying out these computations are described in Table 3.5.3.

TABLE 3.5.3. PARAMETERS DEFINING A SIX-LAYER SIMULATED CRANIAL STRUCTURE EXPOSED TO 800-MHz RADIATION

Tissue type	Radius of bounding sphere (cm)	Relative permittivity	Conductivity (mhos/meter)
Brain	2.68	33.76	0.960
CSF	2.88	79.47	1.740
Dura	2.93	45.64	1.230
Fat	3.13	5.61	0.096
Bone	3.20	5.61	0.096
Skin	3,30	45.64	1.230

ELECTRICAL PROPERTIES

THERMAL PROPERTIES (centimeter-gram-second units)

Tissue type	Thermal conductivity	Density	Sr rillic heat	Blood flow cooling
Skin	.0012300	1.0000	.900	.001002242
Fat	.0003822	.8500	.600	.000000000
Bone	.0027780	1.5000	.380	.000000000
Dura	.001230	1.0000	•900	.000000000
CSF	.001240	1.0069	.998	4.498x10 ⁻⁶
Brain	.001260	1.0500	.883	.00743742

We see from the results described in Figures 3.5.17 and 3.5.18 that there is fairly rapid smoothing of the temperature distributions. Indeed, we have assumed mathematically that both the temperature excursion u and K(x,y,z)grad(u), where K=K(x,y,z) is the thermal conductivity, are continuous. Thus, since in our calculation K is constant, we see that u and its derivatives are continuous. The electrical properties of the six tissue types are given in [7]. The model is capable of predicting the microwave-induceutemperature excursion when there is blood flow in some of the layers, and typical values of these blood flow parameters can be obtained from [6].

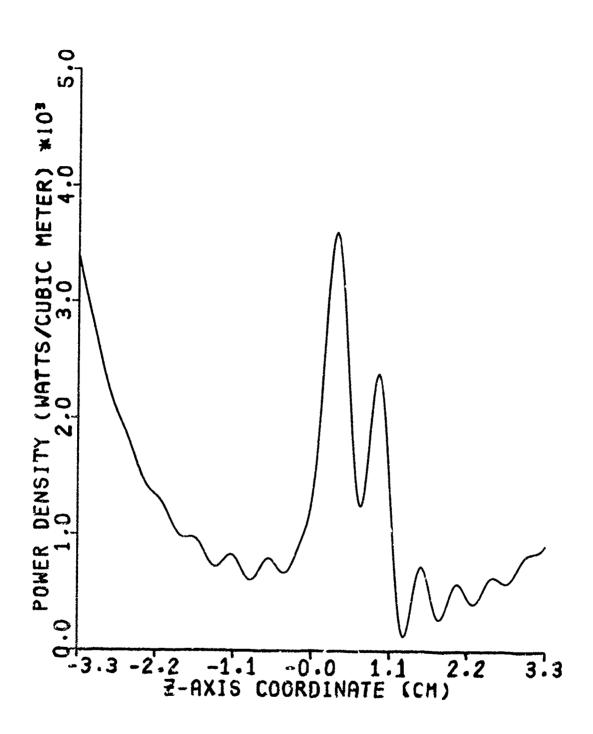


Figure 3.5.1. Power density induced in a muscle-equivalent sphere by 4.5-GHz continuous-wave radiation with a power of $10~\text{mW/cm}^2$.

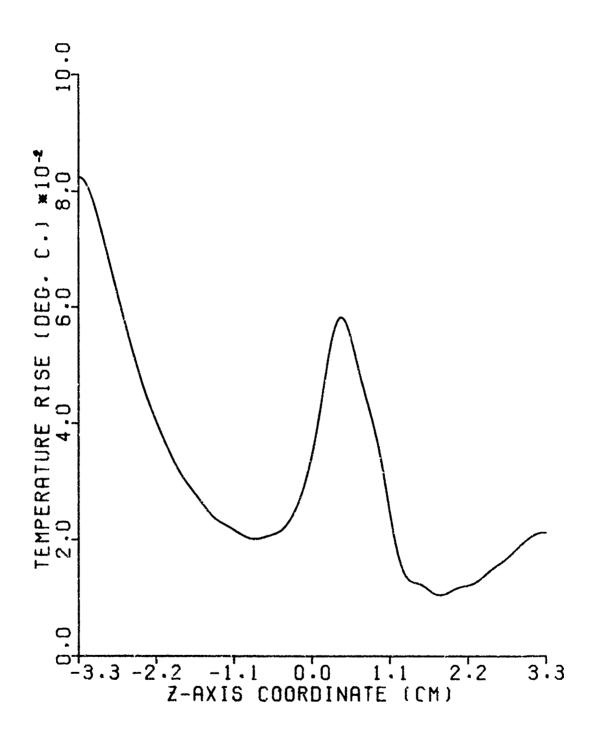


Figure 3.5.2. Thermal response of a muscle-equivalent sphere to a 1-min exposure to 4.5-GHz continuous-wave radiation with a power of 10 $\,$ mW/cm 2 . Parameters defining the problem are given in Table 3.5.1.

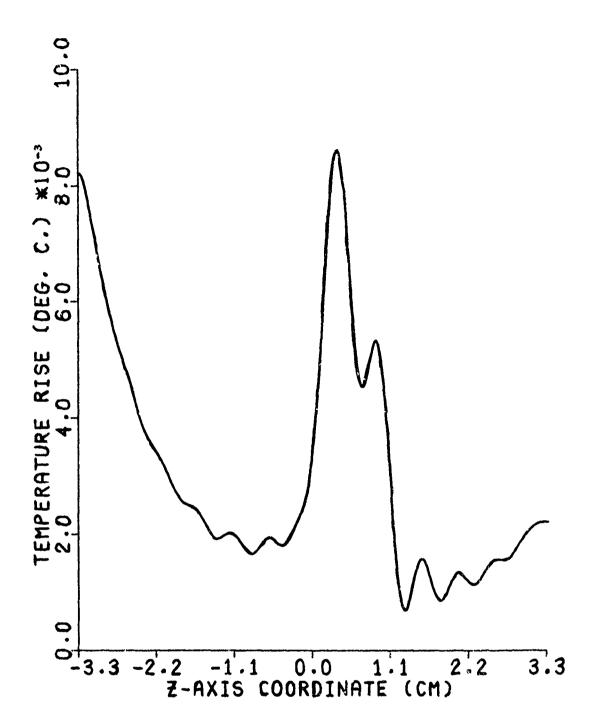


Figure 3.5.3. Thermal response of a muscle-equivalent sphere to a 5-s exposure of 4.5-GHz continuous-wave radiation with a power of $10~\text{mW/cm}^2$. Parameters defining the problem are given in Table 3.5.1.

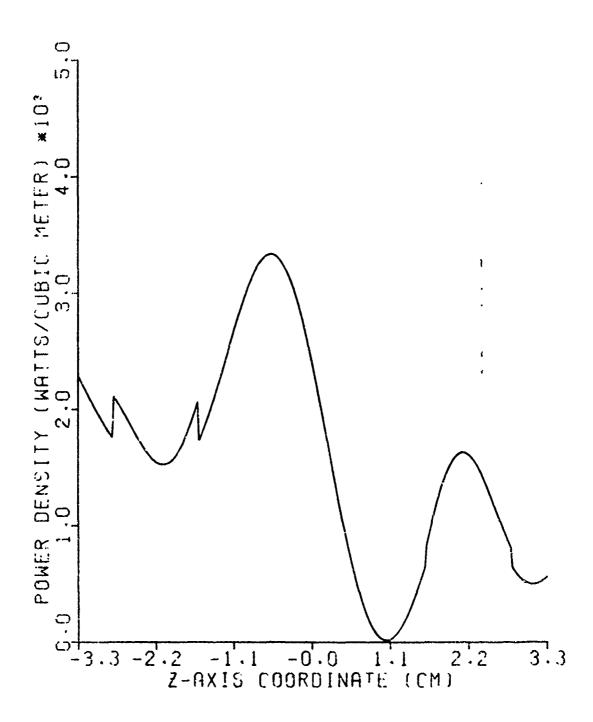


Figure 3.5,4. Power density across the z-axis of a simulated fetal structure exposed to 1-GHz continuous-wave microwave radiation with a power of 10 mW/cm 2 . Parameters defining the problem are given in Table 3.5.2.

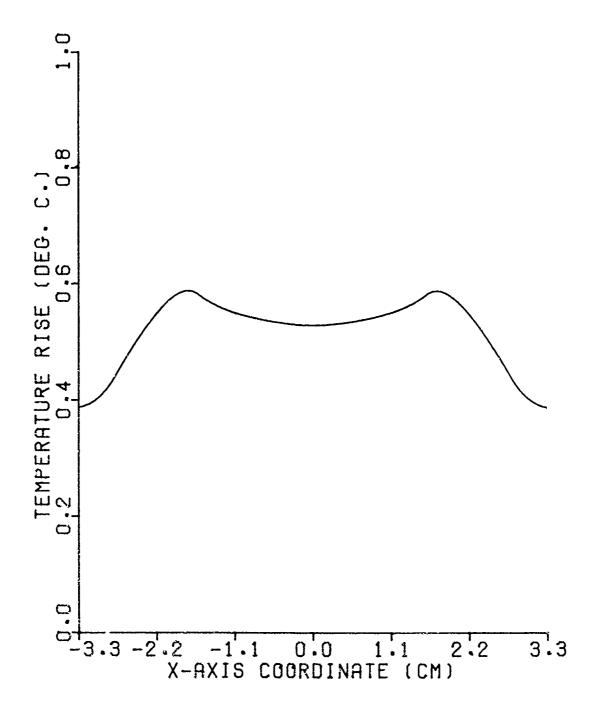


Figure 3.5.5. Thermal response of a simulated fetal structure to a 1-hr exposure to 1-GHz radiation with a power of 10 mW/cm². The temperature is computed across the x-axis. The orientation of the axes is given in Figure 2.1. The parameters defining the problem are given in Table 3.5.2.

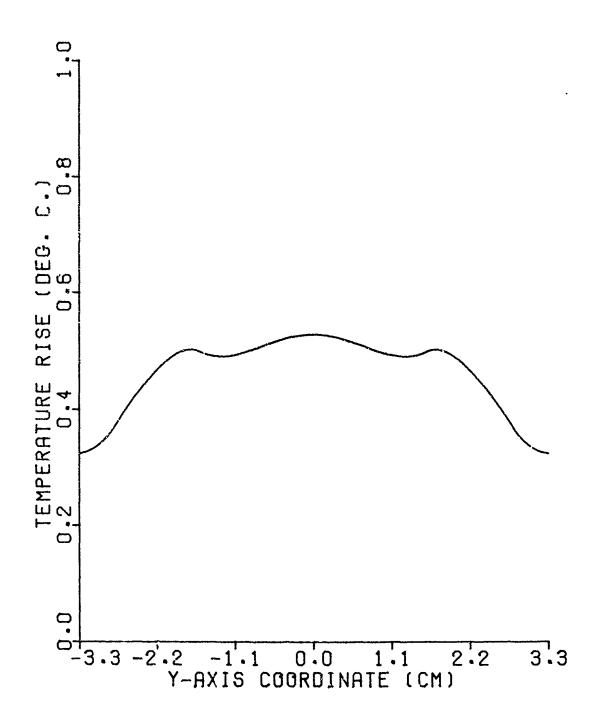


Figure 3.5.6. This is the same as Figure 3.5.5 except that the temperature is computed along the y-axis.

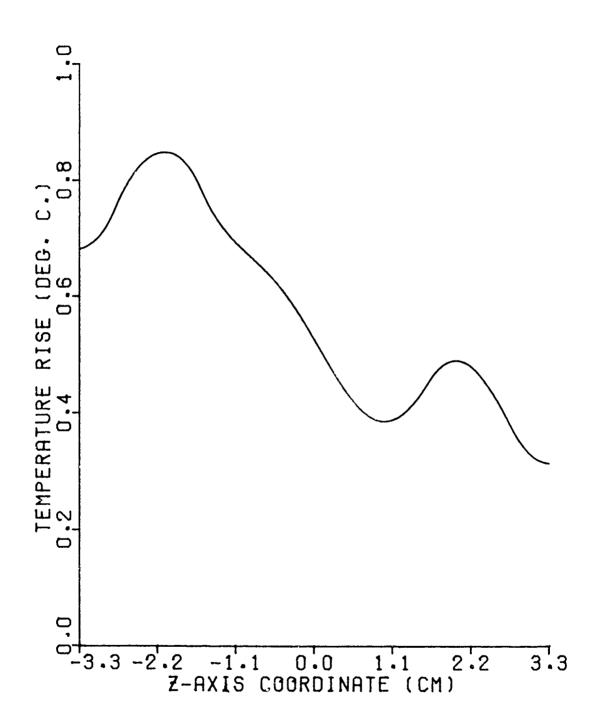


Figure 3.5.7. This is the same as Figure 3.5.5 except that the temperature is computed along the z-axis.

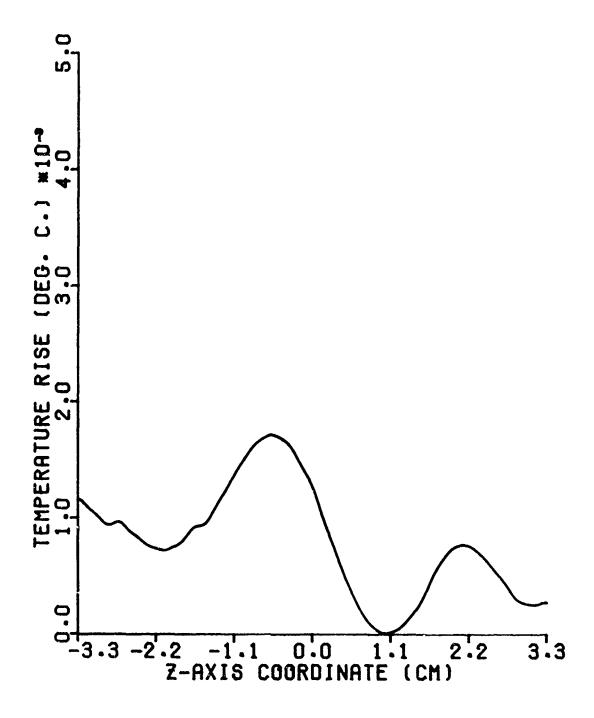


Figure 3.5.8. Temperature distribution along the z-axis for a simulated fetal structure exposed to 1-GHz (10 mW/cm 2) radiation for 1 s. The parameters defining the problem are given in Table 3.5.2, except that all blood flow terms are set to zero.

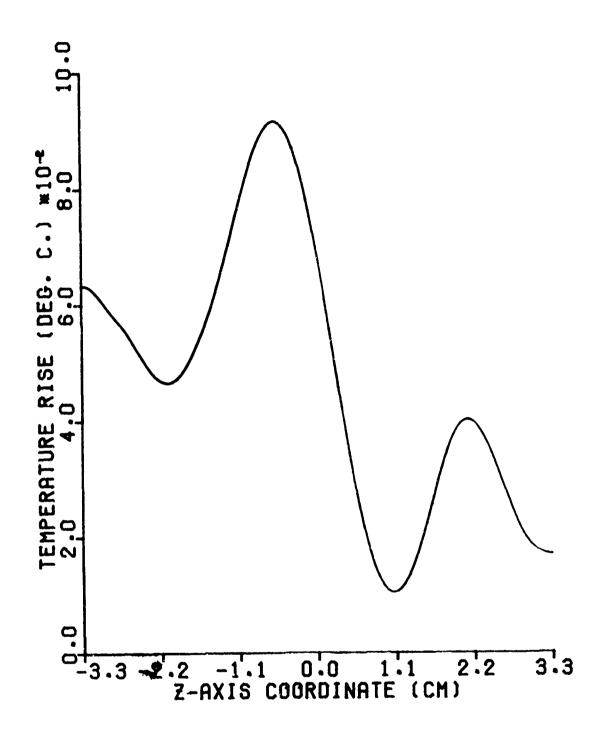


Figure 3.5.9. Temperature distribution along the z-axis of a simulated fetal structure exposed to 1-GHz ($10~\text{mW/cm}^2$) radiation for 1 min. The parameters defining the problem are given in Table 3.5.2, except that all blood flow terms are set to zero.

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Figure 3.5.10. Temperature rise along the z-axis of a simulated fetal structure exposed to 1-GHz (10 mW/cm²) radiation for 15 min. The parameters defining the problem are given in Table 3.5.2, except that all blood flow terms are set to zero.

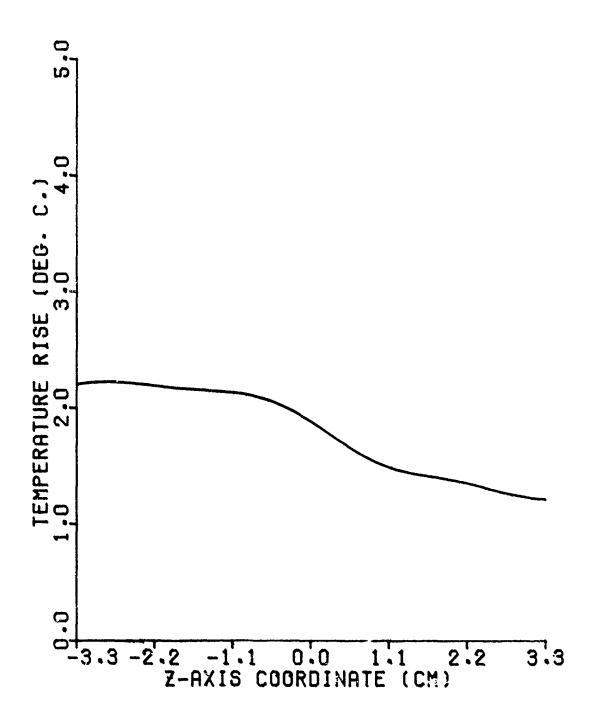


Figure 3.5.11. Temperature rise along the z-axis of a simulated fetal structure exposed to 1-GHz (10 mW/cm²) radiation for 1 hr. The parameters defining this problem are given in Table 3.5.2, except that all blood flow terms are set to zero.

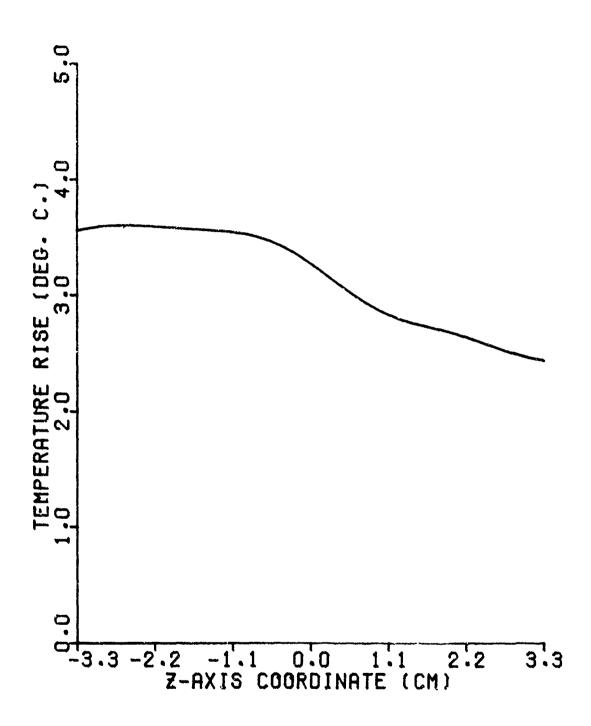


Figure 3.5.12. Temperature rise along the z-axis of a simulated fetal structure exposed to 1-GHz (10 mW/cm²) radiation for 2 hr. The parameters defining this problem are given in Table 3.5.2, except that all blood flow terms are set to zero.

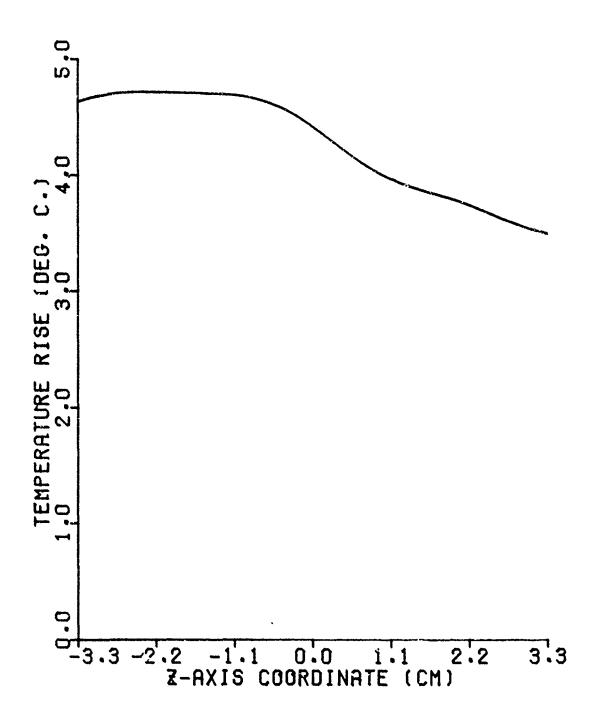


Figure 3.5.13. Temperature rise along the z-axis of a simulated fetal structure exposed to 1-GHz (10 mW/cm^2) radiation for 3 hr. The parameters defining this problem are given in Table 3.5.2, except that all blood flow terms are set to zero.

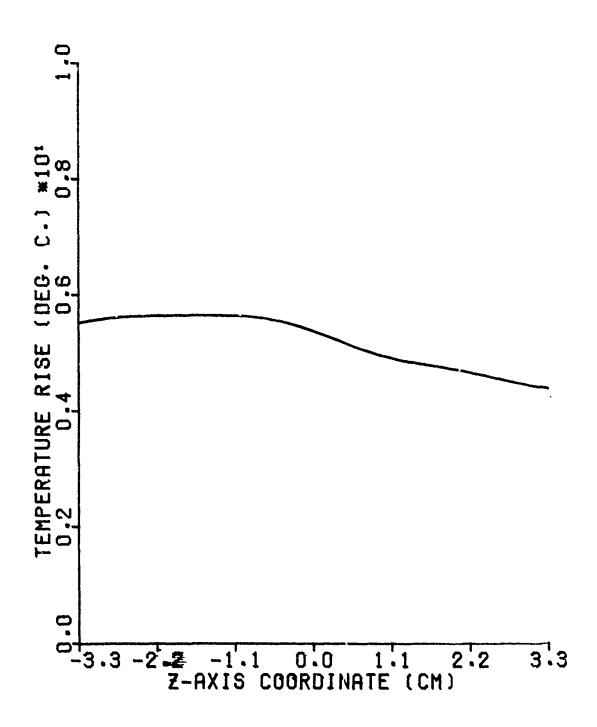


Figure 3.5.14. Temperature rise along the z-axis of a simulated fetal structure exposed to 1-GHz (10 mW/cm^2) radiation for 4 hr. The parameters defining this problem are given in Table 3.5.2, except that all blood flow terms are set to zero.

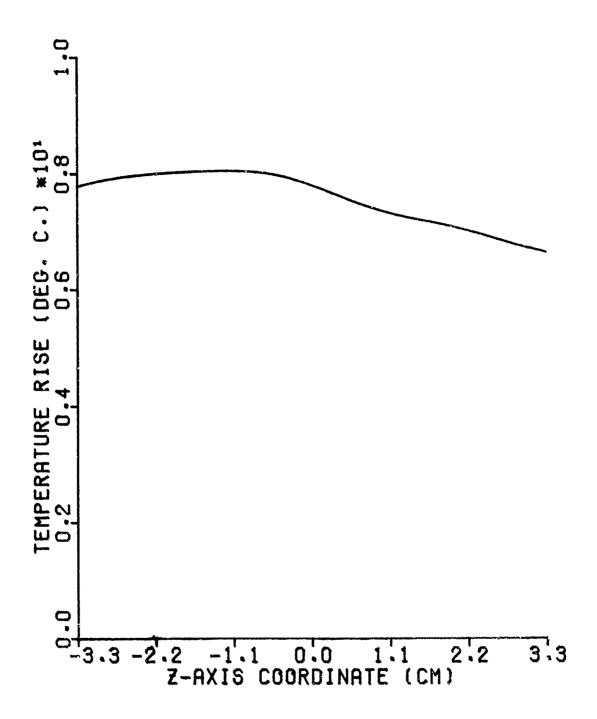


Figure 3.5.15. Temperature rise along the z-axis of a simulated fetal structure exposed to 1-GHz ($10~\text{mW/cm}^2$) radiation for 8 hr. The parameters defining this problem are given in Table 3.5.2, except that all blood flow terms are set to zero.

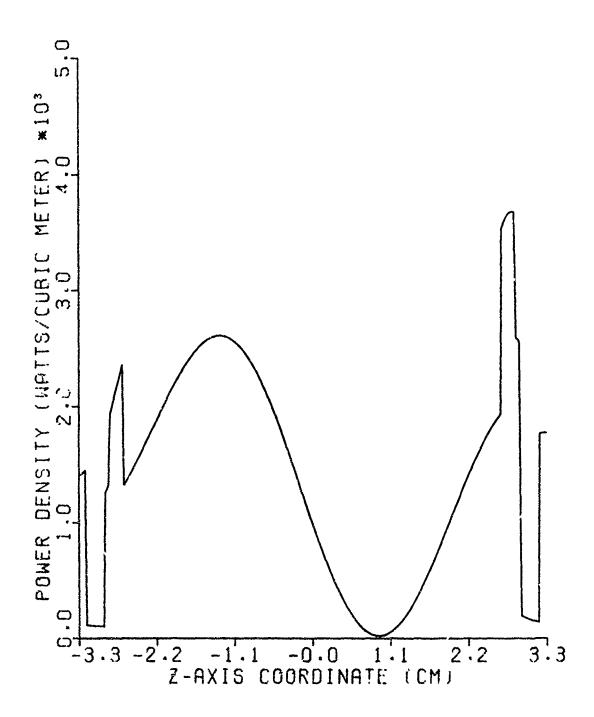


Figure 3.5.16. Power density along the z-axis of a six-layer simulated cranial structure exposed to 800-MHz radiation with a power of $10 \,$ mW/cm 2 . The parameters defining this problem are given in Table 3.5.3.

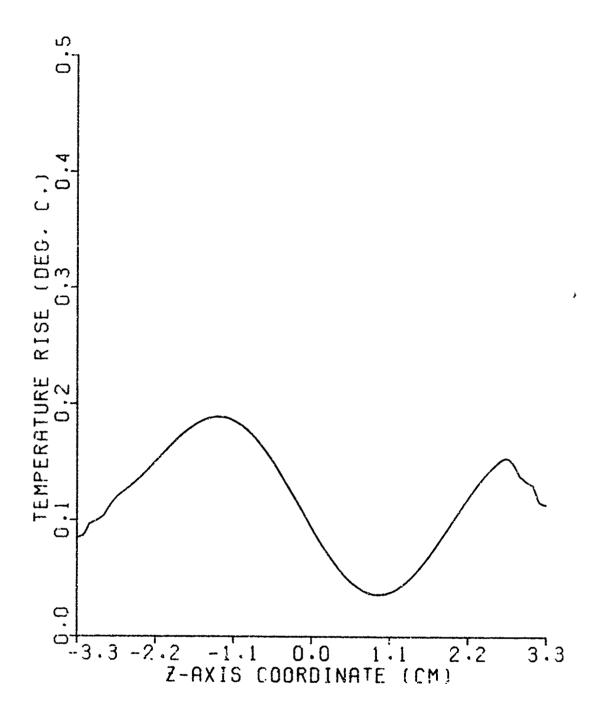


Figure 3.5.17. Thermal response of a six-layer simulated cranial structure exposed to 800-MHz radiation for 3 min. The parameters defining this problem are given in Table 3.5.3.

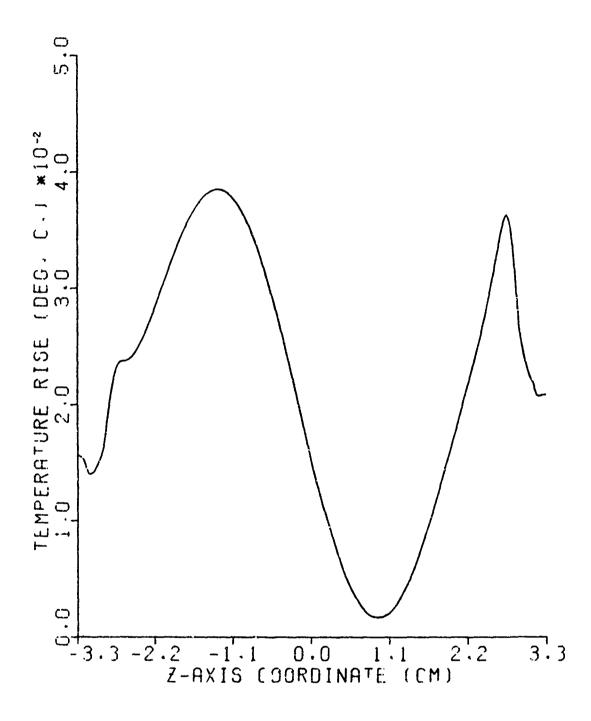


Figure 3.5.18. Thermal response of a six-layer simulated cranial structure exposed to 800-MHz radiation for 30 s. The parameters defining this problem are given in Table 3.5.3.

4. PROGRAM DESCRIPTION

4.1. Purpose of the Program

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The computer program described in this report will predict the thermal response of an autothermally regulated, spherically symmetric, dielectric body with a finite microwave conductivity to a time-harmonic source of microwave radiation. The calculation can be carried out at any point in the interior of this body at any positive time. We also allow the source to be pulsed in the sense that the source of time harmonic radiation may be turned on and off in a complex manner such as that described in Figure 3.4.1. The scattering body consists of from one to six homogeneous regions bounded on the outside by a sphere of finite but positive radius; a description of a six-layer body is shown in Figure 3.5.1. The radiation source is given by an amplitude $\rm E_0$ in volts per meter and a frequency FREQ in megahertz. The calculation is carried out by the evaluation of an analytical expression involving an infinite linear combination of spherical harmonics. The coefficients in this infinite linear combination are functions of time computed from a set of eigenvalues and a knowledge of the manner in which the microwave source has been turned on and off. We also permit a nonzero heat removal term BFRP in one or more of the layers.

4.2. Accessing the Program from the Library

The Job Control Language reeded to access the program from the library is shown in Figure 4.2.1. The data deck, whose preparation will be explained in Section 4.2, goes between the card marked

//GO.SYSIN DD *

/*

The space requirement specified by the expression

REGION.GO=252K

will not change but if one desires temperature information at more points one needs to increase the running time parameter,

TIME.GO=4

and the effective time parameter,

EFFTIME=10

which represents elapsed time in our timesharing computing system. The parameter values listed in Figure 4.2.1 were adequate to determine the temperature excursions for a single fixed time at 13 different locations in space.

Figure 4.2.1. Job control language for calling the microwave thermal response program from the library.

4.3. Glossary of Variables and Their Meaning

All FORTRAN variables used for input and output and important internal FORTRAN variables are listed here in alphabetical order. We, with each variable, give an explanation of its meaning. These variables are:

ALPNP(NNN) = the ALPHA SUB (L,P) coefficient used in formula (3.2.2) to expand the electromagnetic field with NNN = (NREG-1)*NMIN+NN

and

ALPNP(NNN) = ALPHA SUB (NN, NREG) where NN is the spherical Bessel function order and NREG is the layer number.

ANP = the A SUB (L,P) coefficient used in expanding the electric field and which appears in formula (3.2.2) which is stored in a single array with ANP((NREG-1)*NMIN+NN) corresponding to the coefficient A SUB (NN,NREG) where NN indexes the spherical Bessel functions used in the expansion.

and

BETNP(NNN) = BETA SUB (NN, NREG) where NN is the spherical Bessel function order and NREG is the layer number.

BFRP(I) = the blood flow radial perviousness term or the number of grams of blood per gram of tissue per second, with a typical value for brain tissue being .0122

BNP = the B SUB (L,P) coefficient used in formula (3.2.2) to expand the electromagnetic field and which is stored in a single array with BNP((NRTG-1)*NMIN+NN) corresponding to the coefficient B SUB (NN,NREG) where NN indexes the spherical Bessel functions used in the expansion.

BP(!) = the product of BFRP(I), the number of grams of blood per gram of tissue per second, CBP = .98 = the specific heat of blood in calories per gram degree Centigrade, and the density RHOBP = 1.06 = the number of grams of tissue per cubic centimeter of tissue.

CALL BJYH(BJNP,BHNP,Q,NC,STOPR,MAX) = a call to a subroutine which determines the values of spherical Bessel functions of the first kind BJNP and spherical Hankel functions BHNP at the complex argument Q. We attempt to generate up to MAX such functions as we are limited by STOPR and we end up putting only NC such functions in the array.

CALL COEF = a call to a subroutine which produces the expansion coefficients
A SUB(L,P), ALPHA SUB(L,P),
B SUB(L,P) and BETA SUB(L,P)

used in expanding the electromagnetic field using equation (3.2.2)

CALL DRTMI(X,F,FNCAL,SL,SR,W,V,E,NITR) = the call to the bisection routine DRTMI which returns a value X such that FNCAL(X) = F = 0 to within an accuracy of E with less than NITR iterations where FNCAL(SL)=W, FNCAL(SR)=V and W and V are on opposite sides of 0 on the real line.

CALL EPROP(FREQ,ITIS(I),EP,SIG) = a call to a subroutine which determines the relative permittivity EP and microwave conductivity SIG of tissue type ITIS(I) at the microwave frequency FREQ.

CALL PL = a call to a subroutine which computes the array P of associated Legendre polynomials of the first kind and order 1 and an array DP of their derivatives.

CALL TERM(NCK,T,KEY) = a call to a subroutine which computes the I**L multiplied by T appearing in formula (3.2.2) based on its preceding value, where the value of NCK ranges from 1 to 4 since I**1, I**2, I**3, I**4 ranges over all possible values of the square root of (-1) raised to a power, and where KEY takes on the value 1 or 0 depending on where in the process of summing the series we are computing I**L multiplied by the complex term T appearing in equation (3.2.2).

CP(I) = the tissue specific heat in calories per gram per degree centigrade.

DEN(MSBF,M2,NRT) = the integral of the square of the radial eigenfunction multiplied by the square of the radial coordinate, the density, and the specific heat from zero to the outer radius of the scatterer.

E0 = the strength of the incident electric field vector which may be read in a certain number of milliwatts per square centimeter if IE0 = 1 but must be expressed in volts per meter if IE0 = 0, where we understand that if IE0 = 1, then E0 will be converted internally into volts per meter.

EPHI = the phi component of the electric field vector when the electric field is expressed in spherical coordinates and which consequently represents a tangential field component when the point at which the field is being computed is on a sphere defining a boundary of the body being heated by microwaves.

EPS = the relative error associated with the expansion of the electromagnetic field.

EPSP(1) = the relative dielectric constant of the Ith tissue layer at the frequency FREQ of the incoming radiation.

ERAD = the radial component of the electric vector in volts per meter where we assume that we have expressed the field vectors in the spherical coordinate system and which consequently represents the component of electric vector that is perpendicular to a boundary layer when the point at which the electric field is being computed is on a sphere defining a boundary of the body being heated.

ETHETA = the theta responent of the electric field vector when the electric field is expressed in spherical coordinates and which consequently represents a tangential field component when the point at which the field is being computed is on a sphere defining a boundary of the body being heated by microwaves.

ETIME(NRT) = the time profile function, defined by dividing the right side of equation (3.4.7) by b-SUB-BAR-SUB-K-SUB-(M,N) or $b_k^{(m,n)}$, which describes the radar pulse emission patterns.

F = the factor in front of the integral on the right side of equation (3.3.11) in general equal to (2n+1)((n-m)!)/((n+m)!) multiplied by the factor in front of the integrals on the right side of equation (3.3.9) or (3.3.10) whichever is appropriate.

FKP(NREG) = the complex electromagnetic propagation constant associated with layer NREG which is defined by equation (3.2.7).

FREQ = the frequency of the incoming radiation in megahertz or millions of cycles per second.

FUNCTION ALP(N,M,X) = a function subroutine computing the associated Legendre function of the first kind of degree N and order M at the point X with the restriction that N and M are nonnegative integers and M does not exceed N_{\bullet}

FUNCTION FNCAL(EIGV) = a function subroutine whose output is the value of the Newton cooling function defined by equation (3.3.42) when LAMDA = EIGV.

IEO = a parameter for determining the way the input data EO is interpreted with IEO = 0 meaning that EO is a certain number of volts per meter and IEO = 1 meaning that EO is a certain number of milliwatts per square centimeter.

II = in the last print statement an index describing the number of the data card containing the point at which the temperature is being computed with II = 1 for the point on the first card and II = NOCR for the point on the last card.

ISAR = a parameter determining the way that the output data is expressed with ISAR = 0 if the predicted power density that is printed next to the predicted temperature is to be expressed in milliwatts per kilogram, and ISAR = 1 if it is to be expressed in watts per cubic meter.

ITIS(I) = the tissue type of the Ith tissue layer equal to 1,2,3,4,5,6, or 7 if the tissue type is (i) cerebrospinal fluid, (ii) blood, (iii) muscle, (iv) skin or dura, (v) brain, (vi) fat or bone, or (vii) yellow bone marrow, respectively.

KMAX = the number of radial eigenfunctions associated with a given order of Bessel function with the greatest accuracy being achieved by setting KMAX equal to its maximum value of 25.

MP = the number of points to be used in the Gauss quadrature integration scheme that executes the radial transform defined by equation (3.3.22) with this number being one of 32, 48, 64, or 80 and with the larger numbers giving the more accurate results.

MP1 = the number of points used in the Gauss quadrature scheme that performs the Legendre transform defined by equation (3.3.1) with the number being 32 or 48 and where the latter number gives the most accurate results.

NC = the maximum number of Bessel functions available based on the value of the particular point at which the field is being computed and the microwave electrical properties of the layer in which the point is located.

NMAX = the number of orders of spherical Bessel functions that will be used to describe the radial variation of the microwave radiation-induced temperature excursion with the greatest accuracy being achieved by setting NMAX equal to its maximum value of 12.

NMIN = the number of expansion coefficients available based on the radii of the spheres bounding the tissue layers and the microwave electrical properties of the material in these layers.

NNN = (NREG - 1)*NMIN + NN, where NN denotes the spherical Bessel function order.

NREG = the number of the layer in which the point at which the temperature is being computed is found.

NOCR = the number of spatial points at which the input data set is to be computed, the maximum value of the index II of the output temperature data for a particular exposure time, and the number of cards in the fourth input data set.

NORG = the number of layers in the model where NORG is 1 if the scatterer is a homogeneous ball and where NORG equals its maximum value of 6 if the body in which the microwave-induced temperature is being predicted is a ball surrounded by five outer layers.

NPOINT(I) = the Ith entry of a 5-element array containing allowable numbers of points that may be used in a Gauss quadrature scheme for evaluating expansion coefficients.

NPUL = the number of pulses in a group, where for example NPUL = 3 if the radar emission pattern being modeled consists of 3 bursts of radiation followed by a quiet period, 3 bursts and a quiet period, et cetera.

NSBF = FORTRAN index equal to one plus the order of the Bessel function being considered in the computation of the microwave-induced temperature.

PAVG = the total absorbed power divided by the total volume of the region in which the temperature increase is being predicted expressed in watts per cubic meter.

PAVG1 = the total absorbed power divided by the total mass in kilograms of the body in which the temperature excursion is being predicted expressed in milliwatts per kilogram.

PCEBF = the relative error in temperature computation associated with using one less order of Bessel function but keeping the same number of eigenvalues for each Bessel function order which, for example, would mean computing the temperature SBFM1 using NMAX-1 Bessel functions and the full XMAX eigenvalues per Bessel function and defining PCEBF = (TRM-SBFM1)/TRM to be this relative error.

PCER = the relative error associated with leaving off the last eigenfunction or, for example, using 24 eigenfunctions instead of 25 eigenfunctions for each Bessel function order.

PD = the value of the divergence of the Poynting vector at the point whose spherical coordinates are (SAVER, THETAD, PHID) which value represents the number of milliwatts of power being deposited per cubic centimeter of tissue.

PHID = the phi coordinate of the point at which the microwave-induced temperature is to be computed, where phi is the spherical coordinate that ranges between zero and 360 degrees.

R = the radial coordinate of the point at which the temperature is being computed.

RHOP(I) = the tissue density of the Ith tissue layer in grams per cubic meter where typically RHOP(I)=1.

SBDP(I) = the radius in centimeters of the smallest sphere containing the Ith tissue layer where I ranges from 1 to NORG.

SBFM1 = the predicted temperature obtained by using KMAX roots per Bessel function order but only NMAX-1 Bessel function orders in approximating the infinite sum of equation (3.4.1).

SIGP(I) = the conductivity in mhos per meter of the Ith tissue layer where I ranges from 1 to NORG.

SRM1 = the estimated temperature using NMAX Bessel function orders and KMAX-1 eigenvalues per Bessel function order.

STOPR = a termination indicator for stopping the generation of Bessel functions based on the fact that STOPR exceeds the maximum absolute value of any of the spherical Bessel functions of the second kind used in describing the dependence of the induced and scattered electromagnetic fields on the radial variable with a typical value being 1.E35.

TBPER = the period of the pulse group envelope, where, for example, if there is a radar emission pattern consisting of a burst of three pulses of duration 3*TPER followed by a quiet period, a burst of three pulses followed by a quiet period, et cetera, then TBPER is equal to 3*TPER plus the major quiet period, where, of course, we define the major quiet period to be total quiet period minus the time between the individual pulses in the group or as the T-SUB-p in Figure 4.3.1.

TCP(I) = the thermal conductivity in calories per centimeter per degree centigrade per second of the Ith tissue layer where I ranges from 1 to NCRG with a typical value being .0012.

TCUT = the time at which the source of pulsed microwave radiation is shut down or the T-SUB-R of Figure 4.4.1.

TDUR = the up time in seconds of an isolated pulse in a pulse group or the value of T-SUB-d in Figure 4.4.1.

THETAD = the theta coordinate of the point at which the temperature is being computed, where this is the spherical coordinate that ranges between zero and 180 degrees.

TIME = the time in seconds at which the microwave-induced temperature is to be computed.

TOTPOW = the total absorbed power in watts determined by carrying out an energy balance on the surface of the scatterer using the Poynting vector for the incident and reflected radiation.

TRM = the microwave-induced temperature obtained by adding up terms in an eigenfunction expansion at the point whose spherical coordinates are specified by the three-tuple, (SAVER, THETAD, PHID).

U(NSBF,M2,K) = the exparsion coefficient which is defined by equation (3.4.16) at the observation time TIME and which is used in equation (3.4.1), where NSBF is one plus the order of the Bessel function, M2 is I or 2 depending on whether the index of the cosine transform defined by equations (3.3.9) and (3.3.10) is 0 or 2, and K is the index of the eigenvalue associated with a given Bessel function order.

VOL = the volume of the body in which the microwave-induced temperature is being predicted in cubic meters.

XLAMDA(K,NSBF) = an element of a KMAX by NMAX array (dimensioned as 25 by 12) which represents the Kth eigenvalue associated with the Bessel function of order NSFF, where each of these numbers is used to define a combination of spherical Bessel functions satisfying the Newton cooling law at the outer boundary with this combination of Ressel functions being the eigenfunction used in the eigenfunction expansion of the microwave-induced temperature.

XMASS = the mass of the scattering body in kilograms.

XNUM(NSBF,M2,NRT) = the transform of the source term with respect to its
spatial variables.

ZLAB(1) = the first element of an alpha array containing the expression
'W/M**3'.

ZLAB(2) = the second element of an alpha array containing the expression 'MW/KG'.

4.4. Input Data Preparation

The purpose of this section is to tell a user how to prepare data to run the computer program to predict the thermal response of a spherically symmetric penetrable body to microwave radiation. The incoming radiation, the precision with which the response to this radiation will be calculated, the temporal envelope of the incoming radiation and the time at which the temperature response is to be computed, and the thermal and electrical properties of the body in which the temperature excursion is being predicted are described in the first three data sets. Data set three is a multi-card set with the number of cards being equal to the number of layers the scattering body. The fourth data set is the collection of points at which one seeks to compute the temperature; each point is on a separate card.

The following paragraphs give details concerning the composition of the four data sets used by the computer program. Figures at the end give some data sets that direct the program to predict the microwave-radiation-induced temperature on the x, y, and z axes of the sphere.

Data set one consists of a single card containing FREQ, EO, STOPR, NORG, NMAX, KMAX, MP, MP1, IEO, and ISAR which is read in via the statements:

READ 5, FREQ, EO, STOPR, NORG, NMAX, KMAX, MP, MP1, IEO, ISAR 5 FORMAT (3D10.0, 715)

In the above

FREQ = the frequency of the incoming radiation in megahertz,

EO = the strength of the incoming E-field in volts per meter (if IEO = 0) and in milliwatts per square centimeter (if IEO = 1),

STOPR = a termination indicator for stopping the generation of Bessel functions based on the fact that STOPR exceeds the absolute value of any of the spherical Bessel functions Y that will be used in describing the dependence of the induced and scattered fields on the radial variable with a typical value being 1.E35.

NORG = the number of layers in the model where NORG is 1 if the scatterer is a homogeneous ball and NORG equals its maximum value of 6 for a ball surrounded by 5 outer layers,

NMAX = the number of orders of spherical Bessel functions that will be used to help describe the microwave radiation-induced temperature with the greatest accuracy being achieved by setting NMAX equal to its maximum value of 12,

KMAX = the number of radial eigenfunctions associated with a given order of Bessel function where the greatest accuracy is achieved by setting KMAX equal to its maximum value of 25,

MP = the number of points used in the Gauss quadrature scheme that carries out the radial transform defined by the formula (3.22) with this number being one of 32, 48, 64, or 80 and with the larger numbers giving the more accurate results,

MP1 = the number of points used in the Gauss quadrature scheme that carries out the Legendre transform defined by equation (3.11) with this number being 32 or 48,

IEO = a parameter for determining the way the input data EO is interpreted with IEO = 0 meaning that EO is a certain number of volts per meter and IEO = 1 meaning that EO is a certain number of milliwatts per square centimeter,

and

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ISAR = a parameter determining the way that the output data is expressed with ISAR = 0 if the predicted power density is to be expressed in milliwatts per kilogram and ISAR = 1 if the predicted power density is to be written out and labeled as a certain number of watts per cubic meter.

Data set two consists also of a single card containing TDUR, TPER, TBPER, TCUT, TIME, NPUL, and NOCR, which is read in through the statements:

10 READ(5,15,END=350)TDUR,TPTR,TBPER,TCUT,TIME,NPUL,NOCR,IPL1,IPL2 15 FORMAT(5D10.0,215)

In the above

TDUR = the duration of the pulse or the value of T-sub-d in Figure 4.4.1,

TPER = the primary pulse group or the value of T-sub-p in Figure 4.4.1,

TBPER = the period of the pulse group envelope or the T-sub-P in Figure 4.4.1, possible time envelope function for incoming radiation. This is similar to some radar emission patterns.

TCUT = the time at which the source is shut down or the T-sub-R in Figure 4.4.1.

TIME = the time at which the microwave-induced temperature is to be computed,

NPUL = the number of pulses per group, where we note that NPUL=2 in Figure 4.4.1 and NPUL=3 in Figure 3.4.1,

 ${\sf NOCR}$ = the number of spatial points at which the temperature is to be computed.

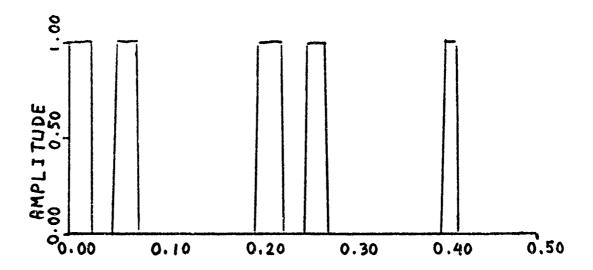
- IPL1 = an integer ranging from 0 to 7, which will indicate which of certain plots of temperature across the sphere diameters coinciding with the coordinate axes will be given. A value of IPL1 equal to
 - O means no axis plots of temperature will be produced,
 - 1 means a plot of temperature across the z-axis will be given,
 - 2 means a plot of temperature across the x-axis will be given,
 - 3 means a plot of temperature across the y-axis will be given,
 - 4 means combined results of 1 and 2 are given,
 - 5 means combined results of 1 and 2 are produced,
 - 6 means combined results of 2 and 3 are produced, and
 - 7 means combined results of 1, 2, and 3 are given,

and

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- IPL2 = an integer ranging from 0 to 7, which will indicate which of certain contour plots of isotherms will be produced on the plotting file FOR008.DAT. In the following description the x-z plane refers to the intersection of the plane containing the x-axis and the z-axis with the interior of the bounding sphere. The y-z plane will mean the plane containing the y and z axes or the plane x = 0. The x-y plane means the plane z = 0. A value of IPL2 equal to
 - O means no axis plots of temperature will be produced,
 - 1 means a contour plot in the x-z plane will be given,
 - 2 means a contour plot in the y-z plane will be given,
 - 3 means a contour plot in the x-y plane will be given,
 - 4 gives the combined results of 1 and 2,
 - 5 gives the combined results of 1 and 3,
 - 6 gives the combined results of 2 and 3, and
 - 7 gives the combined results of 1, 2, and 3.

OVERALL PICTURE



AMPLIFIED PICTURE

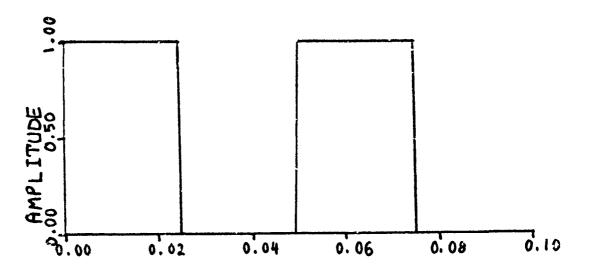


Figure 4.4.1. Typical time envelope function describing some radar emission patterns. In the above figure we have N $_{\rm p}$ = 2 pulses per group, T $_{\rm d}$ = .025 milliseconds (ms), T $_{\rm p}$ = .050 ms, T $_{\rm p}$ = 9 ms. and T $_{\rm R}$ = .4125 ms.

Data set three consists of NORG cards indexed by the parameter I augmented from 1 to NORG in a DO LOOP. The Ith card contains SBDP(I), EPSP(I), SIGP(I), TCP(I), RHOP(I), CP(I), BFRP(I), and ITIS(I) read in by means of the statements:

```
30 FORMAT(7F10.0,15)
    D0 6E I = 1,NORG
    READ 30, SBDP(I), EPSP(I), SFGP(I), TCP(I), RHOP(I),
    1CP(I), BFRP(I), ITIS(I)

...
65 PRINT 70, I, SBDP(I), EPSP(I), SIGP(I),
    1TCP(I), RHOP(I), LP(I), BFRP(I),
    2TISSUE(ITIS(I)).
70 FORMAT(I4,F12.2,F12.2,F13.3,F15.6,F13.4,
    1F10.3,F12.5.3X,A8)
```

In the above, the properties of the Ith layer are specified by letting

SBDP(I) = its outer radius in centimeters,

EPSP(I) = its relative permittivity,

SIGP(I) = its conductivity in mhos per meter,

TCP(I) = its thermal conductivity in calories per centimeter per degree centigrade per second(typically TCP(I) = .0012),

RHOP(I) = tissue density in grams per cubic centimeter(typically RHOP(I) = 1),

CP(I) = tissue specific heat in calories per gram degree centigrade(typically CP(I) = .84),

BFRP(I) = the blood flow term that is equal to the product of the number of grams of blood per gram of tissue per second, the tissue density in grams of tissue per cubic centimeter of tissue, and the specfic heat of the blood (typically b = .0122),

and

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ITIS(I) = the tissue type indicated by a positive integer where ITIS(I) = 1,2,3,4,5,6, or 7 denotes cerebrospinal fluid, blood, muscle, skin or dura, brain, fat or bone, or yellow bone marrow, respectively.

If EPSP(I) or SIGP(I) are read in as 0.D0, then the values of EPSP(I) or SIGP(I) or both are replaced by values determined from values stored in data tables by means of the commands:

```
55 IF(EPSP(I).NE.O.DO.AND.SIGP(I).NE.O.DO)
1GO TO 60
CALL EPROP(FREQ,ITIS(I),EP,SIG)
IF(EPSP(I).EQ.O.DO) EPSP(I) = EP
IF(SIGP(I).EQ.O.DO) SIGP(I) = SIG
60 FAC2 = EPSP(I)/2.DO
```

The fourth data set contains NOCR cards each containing the spherical coordinates (R,THETAD,PHID) of a point whose cartesian coordinates are (X,Y,Z) = (R*SIN(THETAD)*COS(PHID),R*SIN(THETAD)*SIN(PHID),R*COS(PHID)) at which the microwave-induced temperature rise is to be computed. The cards are read in via the statements:

30 FORMAT(7F1G.0)
DO 345 II=1,NOCR
READ 30,R,THETAD,PHID
345 CONTINUE

Finally a typical problem is presented as it would be given to the user and the proper response is indicated. The user directions are to compute the thermal response of a one-layer spherically symmetric ball of brain tissue with a 2.804-cm radius, a permittivity of 31.09, a microwave conductivity of .0012, a density of 1.0, a specific heat of .84, and a blood flow perviousness term of 0.0 to a steady 30-s exposure to 2450-MHz radiation with a power of 70 mW/cm². The user is to compute the temperature along the x, y, and z-axes with x, y, and z-values being taken from the collection, -2.8, -2.45, -2.10,

-1.75, -1.40, -1.15, -.8, -.45, -.1, -1.E-4, +1.E-4, +.1, +.45, +.8, +1.15, +1.40, +1.75, +2.10, +2.45, and +2.8. The user is to obtain these results with maximum accuracy. The proper response is indicated in Figures 4.4.2 - 4.4.5.

2804.D-3	3109.D-2	1414.D-3	13	2.D-4		1.DO	.8	34D+0		0.D0
30.00	30.D0	30.DO	3	0.00	30	0.D0	1	60		
2450.DO	70.DO	1.035	1	12	25	80	48	1	0	

Figure 4.4.2. The first three data sets for the computation of the thermal response of a one-layer brain tissue structure exposed to 70 mW/cm² and 2450-MHz radiation for 30 s at 60 s; 1 points.

280.E-2	180.E0	0.E0
245.E-2	180.E0	0.E0
210.E-2	180.E0	0.E0
175.E-2	180.E0	0.E0
140.E-2	180.E0	0.E0
115.E-2	180.E0	0.E0
60.E-2	2 7 2 7 7 7	0.E0
45.E-2		
10.E-2		0.E0
1.E-4	180.E0	0.E0
1.E-4	0.E0	0.E0
10.E-2	0.E0	0.EC
		1771
45.E-2	0.EQ	0.E0
80.E-2	0.E0	0.E0
115.E-2	0.E0	0.E0
140.E-2	0.E0	0.E0
175.E-2	0.E0	0.E0
210.E-2	0.E0	0.E0
245.E-2	0.E0	0.E0
280.E-2	0.E0	0.E0

Figure 4.4.3. Data set describing points on the z-axis in spherical coordinates. The points on the z-axis at which the temperature is to be computed are shown. The columns in which the data entries end are respectively 10, 20, and 30.

280.E-2	90.E0	0.E0
245.E-2	90.E0	0.E0
210.E-2	90.E0	0.E0
175.E-2	90.E0	0.E0
140.E-2	90.E0	0.E0
115.E-2	90.E0	0.E0
80.E-2	90.E0	0.E0
45.E-2	90.E0	0.E0
10.E-2	90.E0	0.E0
1.E-4	90.E0	0.E0
1.E-4	90.E0	180.E0
10.E-2	90.E0	180.E0
45.E-2	90.E0	180.E0
80.E-2	90.E0	180.E0
115.E-2	90.E0	180.E0
140.E-2	90.E0	180.E0
175.E-2	90.E0	180.E0
210.E-2	90.E0	180.E0
245.E-2	90.E0	180.E0
280.E-2	90.E0	180.E0

Figure 4.4.4. Data set describing points on the x-axis in spherical coordinates. The points on the x-axis at which the data entries end are shown. The columns in which the data entries end are respectively 10, 20, and 30.

280.E-2	90.E0	270.E0
245.E-2	90.E0	270.E0
210.E-2	90,E0	270.E0
175.E-2	90.E0	270.E0
140.E-2	90.E0	270.E0
115.E-2	90.E0	270.E0
80.E-2	90.E0	270.E0
45.E-2	90.E0	270.F0
10.E-2	90.E0	270.t0
1.E-4	90.E0	270.E0
1.E-4	90.E0	90.E0
10.E-2	90.E0	90.E0
45.E-2	90.E0	90.E0
80.E-2	90.E0	90.E0
115.E-2	90.E0	90.E0
140.E-2	90.E0	90.E0
175.E-2	90.E0	90.E0
210.E-2	90.E0	90.E0
245.E-2	90.E0	90.E0
280.E-2	90.E0	90.E0
80.E-2 45.E-2 10.E-2 1.E-4 10.E-2 45.E-2 80.E-2 115.E-2 140.E-2 175.E-2 210.E-2 245.E-2	90.E0 90.E0 90.E0 90.E0 90.E0 90.E0 90.E0 90.E0 90.E0	270.E0 270.E0 270.E0 90.E0 90.E0 90.E0 90.E0 90.E0 90.E0

Figure 4.4.5. Data set describing points on the y-axis in spherical coordinates. The points on the y-axis at which the temperature is to be computed are shown. The columns in which the data entries end are respectively 10, 20, and 30.

4.5. The Output and its Meaning

The output of our program to predict the thermal response of a spherically symmetric body to microwave radiation includes (i) the printing of the input data defining the scattering problem, (ii) the weight and volume of the scatterer, (iii) the average and total absorbed power, (iv) the eigenvalues associated with radial eigenfunctions, (v) the expansion coefficients used in expanding the temperature in spherical harmonics, and finally (vi) the predicted microwave-induced temperature increases and estimates of the theoretical error in our predictions.

The input data which defines the input radiation is printed out and is identified by labels. This data includes the frequency, the field strength, STOPR which is defined in Section 4.3, the up time of a single pulse or TDUR, its period or TPER, the number NPUL of pulses in a single pulse train, the time TBPER that a single pulse train lasts which includes the quiet period after the initial burst of NPUL pulses, the time TCUT after which the incident wave is cut off and the TIME at which one observes the temperature; this output data set is printed by the commands:

PRINT 20, FREQ,E01,UNIT(IEO+1),STOPR,TDUR,TPER,
1NPUL,TBPER,TCUT,TIME
20 FORMAT('1THERMAL RESPONSE OF CONCENTRIC SPHERICAL',
1'HEAD MODEL TO RFR'/'-FREQUENCY =',F9.2,
1'MHZ------FIELD STRENGTH =',F9.2,1X,A8,
16X,'STOPR ='1PD12.4/
1'O FOR ONE PULSE, UP TIME IS',D12.4,'SEC'
1' AND PERIOD IS',D12.4,'SEC.'/
1'O ONE PULSE TRAIN CONTAINS',I4,'PULSES AND LASTS',
1D12.4,'SEC.'/'O THE INCIDENT WAVE IS CUT OFF AFTER',
1'IS OBSERVED AFTER',D12.4,'SEC.')

The next set of output data defines the body in which the microwave-induced temperature is to be predicted. We print out NORG lines of data, each of which defines the outermost bounding sphere of radius SBDP(I), the relative permittivity EPSP(I), the microwave conductivity SIGP(I), the thermal conductivity TCP(I), the density RHOP(I), the specific heat CP(I), the blood flow radial perviousness term BFRP(I), and the tissue type ITIS(I) for the Ith tissue layer. This output data set is defined by the following lines:

```
PRINT 25
25 FORMAT('-REGION', 3X, 'SURFACE', 4X, 'RELATIVE', 5X, 1'ELECTRIC', 7X, 'THERMAL', 6X, 'DENSITY', 3X, 1'SPECIFIC', 3X, 'BLOOD FLOW', 4X, 'TISSUE'/9X, 1'BOUNDARY', 3X, 'DIELECTRIC', 2X, 'CONDUCTIVITY', 12X, 'CONDUCTIVITY', 16X, 'HEAT', 8X, 'RATE', 7X, 1'TYPE'/21X, 'CONSTANT'/11X, '(CM)', 20X, '(MHO/M)', 3X, 1'(CAL/CM-SEC-C)', 3X, '(G/CM3)', 2X, '(CAL/G/S)', 4X, 1'(CC/SEC)'/)

...

DO 65 I = 1, NORG
65 PRINT 70, I, SBDP(I), EPSP(I), SIGP(I), TCP(I), RHOP(I), 1CP(I), BFRP(I), TISSUE(ITIS(I))
70 FORMAT(I4, F12.2, F13.3, F15.6, F13.4, F10.3, 1F12.5, 3X, A8)
```

The next set of output data describes intermediate cuipui resulting from defining the microwave heat source term for the heat transfer equation. The data printed out includes the mass XMASS, in kilograms, of the scattering body, its volume VOL, in cubic meters, the average absorbed power PAVG per unit volume expressed in watts per cubic meter, and the average absorbed power PAVG1 per unit mass expressed in milliwatts per kilogram. This mode by which output is printed is described by the statements:

```
PRINT 80, XMASS, VOL, PAVG, ZLAB(2), PAVG1, ZLAB(1), TOTPOW 80 FORMAT('-WEIGHT=', 1PD12.4, 'KG'/'O VOLUME=', D12.4, 1'M**3'/'OFOR A CONTINUOUS WAVE THE AVERAGE', 1'ABSORBED POWER IS', D13.5, A7, 'OR', D13.5, A7/ 1'OTOTAL ABSORBED POWER=', D13.5, 'WATTS'/ 1'-ROGTS OF THE EIGENFUNCTION'/)
```

The last phrase '-ROOTS OF THE EIGENFUNCTION' is a heading for the next output data set which is the set of eigenvalues needed to define the eigenfunctions used in expressing the microwave-induced temperature excursion.

The next set of output data provide us with the array XLAMDA of eigenvalues defined by equations (3.3.42) and (3.3.44), and which are used to define the radial eigenfunctions used in expanding the microwave-induced temperature excursion. The eigenvalues are printed using the statements:

```
DO 90 NSBF = 1,NMAX

N1 = NSBF - 1

90 PRINT 95,N1,(XLAMDA(K,NSBF),K = 1,KMAX)

95 FORMAT(1H ,I5,1PD12.4,9PD12.4/(7X,10D12.4))
```

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Each row of printing in this output data set displays the sequence defined by equation (3.3.43) where the row index N1 denotes the actual Bessel function order and K is the index of the sequence in equation (3.3.43).

Once the eigenvalues defined as the solution of equation (3.3.44) are determined, we can compute the radial transform, defined by equation (3.3.22), of the source term and subsequently obtain the expansion coefficients U(NSBF,M2,K), defined by equation (3.4.2), that are used in representing the microwave-induced temperature TRM. The expansion coefficients are indexed by

NSBF, which is one plus the order of the Bessel function under consideration, M2 which is 1 if the order of the cosine transform is 0 and is 2 if this is the order of the associated cosine transform, and finally K which is the index of the eigenvalue associated with a given Bessel function order. The expansion coefficients are printed out through the instructions:

```
D0 270 NSBF = 1,NMAX

D0 270 M = 1,NSBF

D0 260 NRT = 1,KMAX

C0 U(NSBF,M2,NRT) = ETIME(NRT)*F*XNUM(NSBF,M2,NRT)/
1DEN(NSBF,M2,NRT)
PRINT 265,N1,M1,(U(NSBF,M2,K),K = 1,KMAX)
265 FORMAT(213,1P10D12.4/(8X,1CD12.4))
270 CONTINUE
```

The final and most important output describes the location of the point at which the temperature is sought, the predicted microwave-induced power density, the temperature excursion, and an estimate of the error associated with approximation of the infinite sum, defined by equation (3.4.1), by only a finite sum. This output is described by the statements:

```
PRINT 275, ZLAB(ISAR+1)

275 FURMAT('-',29X'INTERNAL POINT',11X, 'ABSCRBED',
1'POWER',7X, 'TEMPERATURE',8X, 'APPROXIMATE',
1/11X/'POINT',2X, 'REGION',2X, 'RADIUS',3X,
1'THETA',4X, 'PHI',12X, 'DENSITY',14X,
1'RISE',14X, 'ERROR'/28X, 'CM',6X, 'DEG',12X,
1A7,13X, 'DEG C',13X, 'PER CENT'/)
```

```
DO 345 II = 1,NOCR

PRINT 340, T MMEG, SAVR, THETAD, PHID, PD,

1TRM, PCEBF, PC. ...
340 FORMAI (114,18,F10.3,2F8.2,F19.8,1PD20.4,2P2F12.),
345 CONTINUE
```

In the above ZLAB(ISAR+1) is an alpha array costaining the label 'MW/KG' which stands for milliwatts per kilogram or 'W/M**3' which stands for watts per . mic meter. The parameters II and NREG denote, respectively, the index, resing from 3 to NOCR, of the point at which the temperature is to be computed and the layer number, ranging from 1 to NORG, of the layer in which the point is found. The three-tuple (SAVER, THETAD, PHID) is the spherical coording to representation of the point at which the temperature is to be computed. The variables PD and TRM denote, respectively, the microwave power per unit volume, and the microwave-induced temperature excursion at the point (SAVER, THETAD, PHID). The error estimation parameter PCEBF denotes the relative error in temperature prediction associated with using, NMAX - 1 orders of Bessel functions and KMAX eigenvalues per Bessel function instead of using NMAX and KMAX to get a temperature estimate SBFM1. On the other hand, we see whether or not we have used enough eigenvalues per Sessel function order by using NMAX orders of Bessel furctions and KMAX - 1 eigenvalues per Bessel functions order obtaining a temperature estimate SRM1 and computing the relative error PCER by the statement,

PCER = (TRM - SRM1)/TRM

4.6. Program Size and kunning Time

The program requires 252K on the 'GO' step for an IBM 360 and has a running time that is dependent on the accuracy demanded and the number of layers in the model. For a one-layer model demanding maximum accuracy and computing the temperature at 60 points for one exposure time, the time on the 'GO' step was 2.93 minutes.

Gaussian quadrature it used to compute cosine, Legendre, and radial transforms of the source taken divided by the product of the density and specific heat. We do these computations in an optimal way by precomputing needed values and taking care not to compute any complex function more than once at the same argument.

4.7. Error Messages

In this section we explain the error messages that the program provides to the user when he has inadvertently provided unsuitable input data. Some of the errors are fatal and some merely provide a warning to the user regarding the accuracy of their results.

An example of the latter occurs often when one attempts to compute the thermal response at points on the positive z-axis in that the series expansion of the electric field vector may not have enough terms in it to guarantee eight significant digits of accuracy in the answer. The coding which prints out this error message is given by the statements:

```
PRINT 30, NMIN, NC, STOPR, EPS
30 FORMAT(15X, 'NMIN =', I3, 'NC =', I3, 2X, 1'STOPR =', 1PD14.4, 'IS TGO SMALL', 1'FOR ACCURACY OF', D14.4)
```

where NC is the number of spherical Bessel functions available to estimate the field at a given point, NMIN is the number of expansion coefficients available based on the location of the layer electrical properties, and EPS is the relative error demanded in the solution.

The error messages are described next in the order in which they are found in the main program. The first message in the main program gives an obvious constraint on the parameters defining the time profile of the beam. This is printed out when appropriate by the statements:

```
IF (NPUL.GT.O.AND.TDUR.GT.O.DO.
1AND.TCUT.GT.O.DO.AND.TIME.GT.O.DO)GO TO 24
21 PRINT 22
22 FORMAT('****ERROR IN TIMES****')
```

STOP
24 IF(TPER.LT.TDUR.OR.TBPER.LT.NPUL*TPER)GO TO 21

The next fatal error messages deal with the fact that the radii of the layers should be in ascending order and that there are only 7 possible tissue types, recognized by the program, assignable to a layer. These messages, when appropriate, are printed by the commands:

```
IF(I.EQ.1.OR.SBDP(I).GT.SBDP(I-1))GO TO 45
PRINT 40
40 FORMAT('****LAYER RADII MUST BE',
    1' IN ASCENDING ORDER****)
STOP
45 IF(ITIS(I).GT.O.AND.ITIS(I).LT.8)GO TO 55
PRINT 50,I,ITIS(I)
```

The next control on the input is based on the fact that the number of points used in the Gauss guadrature integration scheme for determining the expansion coefficients can only assume certain discrete values contained in a five-element array NPOINT. These error messages controlling the number of points requested to be used in evaluating the radial transform are, when appropriate, printed by means of the commands:

```
DO 100 I = 1,5
IF(MP.EQ.NPOINT(I))GO TO 110
100 CONTINUE
PRINT 105,MP
105 FORMAT('OINTEGRATION CONTROL =',I9,2X,
1'IS NOT AVAILABLE')
STOP
```

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The error message controlling the number of points requested to be used in evaluating the Legendre transform is, when appropriate, printed by means of the commands:

```
DO 115 I = 1,5
IF(MP1.EQ.NPOINT(I))GO TO 120
115 CONTINUE
PRINT 105,MP1
STOP
```

The above errors are fatal in the sense that the program stops execution as soon as the errors are recognized.

The next error message is another check on the accuracy with which the electric vectors are computed. This check deals with the computation of fields at the Gauss quadrature points for the purpose of eliminating the temperature excursion induced by the microwave radiation. The message described at the beginning of this section dealt with the computation of power density at the points at which the temperature is to be computed or, said differently, with the accuracy of column 6 in the last output data table.

These error messages are described by the following statements:

```
IR = 0
D0 165 N = 1,NC
FAC1 = 2*N + 1
IF(IR.EQ.1)GO TO 155
T = P(N)*TR(N)
ERAD = ERAD + T
IF(CDABS(T).LT.CDABS(ERAD)*EPS) IR = 1
155 IF(ITP.EQ.1)GO TO 160
```

```
NP1 = N + 1
     RATIO = FAC1/(N*NP1)
     A = RATIO*P(N)/SINTH
     B = -RATIO*DP(N)
     C = A*TEI(N) + B*TE(N)
     ETHETA = ETHETA + C
     T = A*TEI(N) + B*TE(N)
     EPHI = EPHI + T
     IF (CABS(C).LT.CDABS(ETHETA)*EPS.
    1AND.CDABS(T).LT.CDABS(EPHI)*EPS) ITP = 1
160 IF(IR + ITP.E0.2)GO TO 175
165 CONTINUE
     PRINT 170, NMIN, NC, THETA, R, STOPR, EPS
170 FORMAT(15X, 'NMIN='I3, 'NC=',I3,
1'THETA=',F9.6, 'R=',2PF9.6,
1'STOPR='1PD9.2, 'ISTOO SMALL FOR',1X,
    1'ACCURACY OF', D9.2)
175 \text{ ERAD} = \text{ERAD/O}
```

We note that in the above code C represents an amount to be added to the series representation of ETHETA. Thus, if CDABS(C) is small in comparison to CDABS(ETHETA)*EPS, then we say that adding the term C affected the value of ETHETA in the decimal place equal to the integer value of 1/EPS or, said differently, that EPS is the relative error associated with using one less term in the series representation of ETHETA. It is also clear from the above coding that the term T is used in the same way to describe the accuracy with which ERAD, the component of the electric field vector in the radial direction, and EPHI, the component of the electric field vector in phi direction, are computed.

The final error message of the control program is a nonfatal error message that warns the user when he attempts to predict the microwave heating in the free space outside the body that is being irradiated. This message, when appropriate, is printed by means of the commands:

DO 285 NREG = 1,NORG
 IF(R.LE.SBDP(NREG))GO TO 300
285 CONTINUE
290 NREG = 1000000000
 PRINT 295,U,NREG,SAVR,THETAD,PHID
295 FORMAT(114,18,F10.3,3X,'**THE RADIUS',1X,
 1'IS OUTSIDE THE SPHERE***')
 GO TO 345
300 IREG = NREG

The statement

GO TO 345

directs the program around the temperature computation part of the program when this error message is printed. In other words, the computer program will not let the user waste his time by attempting to compute microwave-induced temperature excursions at points outside the body being irradiated.

4.8. Program and Subprogram Description

In this section we give an executive description of the overall program, list the subroutines called, and give their purpose.

The main program is divided into five parts. These parts carry out (1) the scattering problem definition by reading in the data and using subroutine EPROP, (ii) the electromagnetic field expansion coefficient determination and surface energy balance from the results of the COEF subroutine, (iii) the determination of the eigenvalues of the elliptic part of the heat transfer operator using the RFNDR subroutine, (iv) the microwave heat source expansion and thermal expansion coefficient using the subroutines BJYH, TERM, PL, ALP, and SRBF, and finally (v) the power density, temperature and error estimation portion using only the subroutines SRBF and ALP. The beginning and ending of the above five sections are marked by comment cards in the listing of the program in Appendix A.

In the next part of this section we describe all of these subroutines in the order in which they occur in the main program.

The subroutine EPROP determines, by interpolating tabulated data, the relative permittivity or microwave conductivity of any of the seven tissue types from tabulated data. The subroutine is called by the statement,

CALL EPROP(FREQ, ITIS(I), EP, SIG)

The user must supply FREQ, the frequency of the incoming radiation in megahertz, and the tissue type ITIS(I) of the Ith layer of the scatterer, where ITIS(I) = 1, 2, 3, 4, 5, 6, or 7 depending on whether the tissue type is cerebrospinal fluid, blood, muscle, skin or dura, brain, fat or bone, or yellow bone marrow, respectively.

The subroutine COEF generates expansion coefficients ANP, BNP, ALPNP, and BETNP used in expanding the electromagnetic field. It is called by the statement,

CALL COEF

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The subroutine RFNDR is used to determine the eigenvalues of the elliptic part of the heat transfer operator by a shooting method. Basically we start out with a trial value of the eigenvalue, an assumption about the asymptotic behavior of the radial eigenvalue at the origin so that with this assumption the solution of the singular ordinary differential equation with which the eigenvalue is associated is unique. We then check and see if the Newton cooling condition on the boundary is satisfied. If it is, we know that we have an eigenvalue. If the Newton cooling condition or equation (3.3.44) is not satisfied, we increase the trial value slightly and try again.

When we find two trial values at which the Newton cooling function, the output of the function subroutine FNCAL, differ in sign, we then use a bisection routine DRTMI to get the value of the eigenvalue to as many decimal places as is desired.

The subroutine BJYH generates arrays BJNP and BHNP of spherical Bessel functions and Hankel functions, respectively, used in the determination of the functions defined in equations (3.2.2) - (3.2.6). It is called by the statement,

CAL BJYH(BJNP, BHNP, Q, NC, STOPR, MAX)

where Q is equal to a sphere radius multiplied by the complex propagation constant FKP(NREG) defined by equation (3.2.7). We compute up to MAX values limited by the size constraint STOPR, but we fill the arrays with only NC values since we have the same number of spherical Bessel functions in all regions.

The subroutine TERM computes the product of the square root of (-1) raised to the power NCK and the factor of I**L appearing in equation (3.2.2) where here "I" denotes the square root of -1.

The subroutine PL computes an array P of associated Legendre polynomials of the first kind and order 1 and an array DP of their derivatives.

The function subroutine ALP computes the associated Legendre function of the first kind, degree N and order M with M and N being nonnegative integers and with M not exceeding N. It is a function subroutine returning a single value at a single point.

The function subroutine SRBF computes the spherical Bessel functions XJ and XY of the first and second kind, respectively, and their respective derivatives DJ and DY at the value equal to the square root of S1 multiplied by SAVR or the arguments appearing in the discussion in Section 3.3.

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APPENDIX A LISTING OF THE PROGRAM

```
PROGRAM TRP
      THERMAL RESPONSE OF CONCENTRIC SPHERICAL
                   HEAD MODEL TO RFR
IMPLICIT REAL*8 (A-H,0-Z)
COMPLEX*16 FKP, ANP, BNP, ALPNP, BETNP, BJNP, BHNP, ERAD, ETHETA, EPHI, T, C,
1W,X,Y1,Z,Q,TE(50),TE1(50),TR(50)
COMMON FKP(7), ANP(300), BNP(300), ALPNP(300), BETNP(300), BJNP(100), BH
                                                                          8
1NP(100),BDP(6),P(51),DP(50),R,THETA,COSTH,PHI,SINTH,STOPR,E0
                                                                          9
COMMON /A/NORG, NREG, NRT, NSBF, NMIN, NC, ICODE
                                                                         10
COMMON /B/FACT(6,25,18),AJ(6,25,18),BY(6,25,18),XLAMDA(25,18),SBDP
                                                                         11
1(6),RHOP(6),CP(6),BP(6),TCP(6),H
                                                                         12
COMMON /C/AJ1,S1,F,R1,IREG
                                                                         13
                                                                         14
INTEGER*2 IFL(102,102)
REAL*4 R3(304), TR3(304), X2(102), DAR(102,102), CLAB(3,3), ANG, AX1, AY
                                                                         15
DIMENSION U(18, 2,25), EPSP(6), SIGP(6), BFRP(6),
                                                                         16
                                                                         17
           S(80,64,2), XNUM(18,2,25), DEN(18,2,25), RR(80), ETIME(25)
                                                    THET1(64),COSTH1(
                                                                         18
164).SINTH1(64).WTTH(64).ALPOL(64)
                                                                         19
                                                                         20
           NPOINT(5), KEY(6), Y(116),
                                           WT(116).
                                                             ARG3(2)
                                                                         21
1,UNIT(2),ZLAB(2),
                                                                         22
           SUM2(80,2)
                                                                         23
           TISSUE(7), ITIS(6)
      ,BLAB(3),AX(3).
                                                                         24
                                                DLAB(4)
DATA TISSUE/'CS FLUID', 'BLOOD', 'MUSCLE', 'SKIN-DUR', 'BRAIN', 'FAT-BO
                                                                         25
1NE', 'Y.B.M.'/
                                                                         26
DATA
                                                              UNIT/'V/
                                                                         27
        'MW/CM**2'/,ZLAB/' MW/KG',' W/M**3'/
                                                                         28
1M'
                                                                         29
     ,EPS/1.D-8/
DATA CLAB/'E PL', 'ANE', ' ', 'H PL', ANE', ' ', 'X-Y', 'PLAN', 'E'/
                                                                         30
1, BLAB/'Z-AXIS C', 'OORDINAT'
                                                                          31
      ,'E (CM)'/,AX/'Z-AXIS C','X-AXIS C','Y-AXIS C'/
                                                                          32
                                     DLAB/'TEMPERAT', 'URE RISE',' (D
                                                                         33
1EG. C','.)'/
                                                                          34
                                                                          35
DATA NPOINT/32,48,64,80,8/,KEY/1,17,41,73,113,117/
DATA Y/.048307665688D0,.14447196158D0,.23928736225D0,.33186860228D
                                                                          36
                                                                          37
10,.42135127613D0,.50689990893D0,.58771575724D0,.66304426693D0,.732
118211874D0,.79448379597D0,.84936761373D0,.89632115577D0,.934906075
                                                                          38
                                                                          39
194D0..96476225559D0..98561151155D0..99726386185D0..032380170963D0,
                                                                          40
1.09700469920900,.1612223560700,.2247637903900,.2873624873600,.3487
15588629D0,.40868648199D0,.46690290475D0,.52316097472D0,.5772247260
                                                                          41
18D0,.62886739678D0,.67787237963D0,.72403413092D0,.76715903252D0,.8
                                                                         42
                                                                          43
10706620403D0,.84358826162D0,.87657202027D0,.90587913672D0,.9313866
19071D0,.95298770316D0,.97059159255D0,.98412458372D0,.99353017227D0
                                                                         44
1,.99877100725D0,.024350292663D0,.072993121788D0,.1214628193D0,.169
                                                                          45
164442042D0,.21742364374D0,.26468716221D0,.31132287199D0,.357220158
                                                                          46
13400,.4022701579600,.4463660172500,.4894031457100,.5312794640200,.
                                                                          47
15718956462D0,.61115535517D0,.64896547125D0,.68523631305D0,.7198818
                                                                          48
                                                                          49
15017D0,.75281990726D0,.78397235894D0,.81326531512D0,.84062929625D0
1,.8659993981500,.88931544600,.9105221370800,.9295691721300,.946411
                                                                          50
137486D0,.96100879965D0,.97332682779D0,.98333625388D0,.99101337148D
                                                                          51
10..99634011677D0..99930504174D0.
                                                                          52
         .019511383257D0,.058504437152D0,.097408398442D0,.136164022
                                                                          53
```

```
54
 1809D0..17471229183D0..21299450286D0..25095235839D0..28852805488D0.
 1.32566437075D0..3623047535D0..39839340588D0..43387537083D0..468696
                                                                        55
 161517D0,.50280411189D0,.5361459209D0,.56867126812D0,.60033062283D0
                                                                        56
 1,.63107577305D0,.66085989899D0,.68963764434D0,.71736518536D0,.744U
                                                                        57
 10029758D0,.76950242014D0,.7938327175D0,.81695413868D0,.83883147358
                                                                        58
 1D0,.85943140666D0,.87872256768D0,.89667557944D0,.91326310257D0,.92
                                                                        59
 1845987717D0,.94224276131D0,.95459076634D0,.96548508904D0,.97490914
                                                                        60
 1059D0..98284857274D0,.9892913025D0,.99422754097D0,.9976498644D0,.9
                                                                        61
 19955382265D0,.1834346425D0,.52553240992D0,.79666647741D0,.96028985
                                                                        62
                                                                        63
 DATA WT/.096540088515D0,.095638720079D0,.093844399081D0,.091173878
                                                                        64
 1696D0,.087652093004D0,.083311924227D0,.078193895787D0,.07234579410
                                                                        65
 19D0,.065822222776D0,.058684093479D0,.050998059262D0,.042835898022D
                                                                        66
 10,.034273862913D0,.025392065309D0,.016274394731D0,.0070186100095D0
                                                                        67
 1,.064737696813D0,.064466164436D0,.063924238585D0,.063114192286D0,.
                                                                        68
 106203942316D0,.060704439166D0,.059114829698D0,.0572772921D0,.05519
                                                                        69
 195037D0,.052890189485D0,.050359035554D0,.047616658492D0,.044674560
                                                                        70
 1857D0,.041545082943D0,.038241351066D0,.034777222565D0,.03116722783
                                                                        71
 13D0..027426509708D0..023570760839D0..019616160457D0..015579315723D
                                                                        72
 10,.011477234579D0,.0073275539013D0,.6031533460523D0,.048690957009D
                                                                        73
                                                                         74
 ,.048575467442D0,.048344762235D0,.047999388596D0,.047540165715D0
 1.046968182816D0..046284796581D0..045491627927D0..044590558164D0..0
                                                                        75
 143583724529D0,.042473515124D0,.041262563243D0,.039953741133D0,.038
                                                                         76
 1550153179D0,.03705512854D0,.035472213257D0,.033805161837D0,.032057
                                                                         77
 1928355D0,.030234657072D0,.028339672614D0,.026377469715D0,.02435270
                                                                         78
 12569D0,.022270173808D0,.020134823154D0,.017951715776D0,.0157260304
                                                                         79
 176D0,.013463047897D0,.01116813946D0,.0088467598264D0,.006504457969
                                                                         80
 1D0,.0041470332606D0,.0017832807217D0,
                                                                        81
           .039017813656D0,.038958395963D0,.038839651059D0,.03866175
                                                                        82
 19774D0,.038424993007D0,.038129711314D0,.037776364362D0,.0373654902
                                                                        83
 139D0,.036897714638U0,.036373749906D0,.035794393953D0,.035160529045
                                                                        84
 1D0,.034473120452D0, 033733214985D0,.032941939398D0,.032100498673D0
                                                                        85
 1,.03121017418858,.0302723_176D0,.029288369583D0,.028259816057D0,.0
                                                                         86
 127188227500,.02607523576800,.02492253576400,.02373188286600,.02250
                                                                         87
 15090246D0,.021244026116D0,.019950610878D0,.018626814208D0,.0172746
                                                                         88
 152056D0,.015896183584D0,.014493508041D0,.013068761592D0,.011624114
                                                                         89
 1121D0,.010161766041D0,.00CJ339452693D0,.0071929047681D0,.005690922
                                                                         90
 14514D0,.0041803131247D0,.0026635335895D0,.0011449500032D0,.3626837
                                                                         91
 18338D0,.31370664588D0,.22238103445D0,.10122853629D0/
                                                                         92
                                                                         93
  IPLSW=0
                                                                         94
  PIE=3.141592653589793D0
 RAD=180.DO/PIE
                                                                         95
 EPS0=8.85416D-12
                                                                         96
  VEL=2.997924562D8
                                                                         97
 RHOBP=1.06D0
                                                                         98
 CBP=0.98D0
                                                                         99
 H=5.72D-5
                                                                        100
  ITME=0
                                                                        101
*******FIRST DATA CARD - CONTROL PARAMETERS
                                                                        102
  READ (5,5)FREQ.EO.STOPR.NORG.NMAX.KMAX.MP.MP1.IEO.ISAR
                                                                        103
5 FORMAT (3D10.0,715)
                                                                        104
               FREOUFNCY IN MEGAHERTZ
        FREO
                                                                        105
               STRE : H OF INCIDENT E-FIELD
                                                                        106
        STOPR
               CUTO: FOR SBF COMPUTATIONS
                                                                        107
        NORG
               NUMBER OF LAYERS IN SPHERE
                                                                        108
               IS DESIRED. A CARD WILL BE READ FOR EACH POINT.
                                                                        109
               NUMBER OF ORDERS OF BESSEL FUNCTIONS USED. MAX=12
        NMAX
                                                                        110
```

```
NUMBER OF ROOTS FOR EACH ORDER. MAX=25
                                                                              111
         KMAX
                 NUMBER OF POINTS FOR INTEGRATION FOR RADIUS. 32, 48,
                                                                              112
         MP
                                                                              113
                    64 OR 80. (, IS AVAILABLE FOR TEST RUNS)
         MP1
                 NUMBER OF POINTS FOR INTEGRATION FOR THETA.
                                                                              114
                 INPUT EO UNITS
                                                                              115
          I EO
                    0 - VOLTS/METER
                                                                              116
                    1 - MILLIWATTS/SQUARE CENTIMETER
                                                                              117
                 OUTPUT POWER DENSITY UNITS
                                                                              118
          ISAR
                                                                               119
                    0 - MILLIWATTS/KG
                                                                               120
                    1 - WATTS/CUBIC METER
 · E01=E0
                                                                               121
   IF (JEO.EQ.0) GO TO 10
                                                                               122
                                                                               123
   IE0=1
                                                                               124
   E0-9SORT(3767.D0*E0)
                                                                               125
*********SECOND DATA CARD. TIMES IN SECONDS FOR INCIDENT WAVE PULSES.
          FIRST PULSE TURNS ON AT ZERO SECONDS.
                                                                               126
10 READ (5,15,END=495) TDUR, TPER, TBPER, TCUT, TIME, NPUL, NOCR, IPL1, IPL2,
                                                                               127
  1NTP
                                                                               128
15 FORMAT (5D19.0,515)
                                                                               129
                                                                               130
          TOTA
                 TIME DURATION OF A PULSE
                                                                               131
          TPER
                 PERIOD FROM START OF A PULSE TO START OF NEXT PULSE.
          TREER
                 PERIOD FOR A GROUP OF PULSES.
                                                                               132
                                                                               133
                 TIME AT WHICH WAVE IS CUT OFF
          TCUT
          TIME
                 TIME WHEN TEMPERATURE RISE IS OBSERVED.
                                                                               134
                 NUMBER OF PULSES IN A GROUP
                                                                               135
          NPUL
                 NUMBER OF POINTS IN SPHERE AT WHICH TEMPERATURE RISE
                                                                               136
          NOCR
          PRINT OUT TITLE AND BASIC INPUT DATA
                                                                               137
                                                                               138
   PRINT 20, FREQ, E01, UNIT (IEO+1), STOPR, TDUR, TPER, NPUL, TBPER, TCUT, TIME
20 FORMAT ('1THERMAL RESPONSE OF CONCENTRIC SPHERICAL HEAD MODEL TO R
                                                                               139
  1FR'/'-FREQUENCY =',F9.2,' MHZ
                                         FIELD STRENGTH = '.F9.2.1X.A8.6
                                                                               140
  1X.'STOPR =',1PD12.4/
                                                                               141
  1'OFOR ONE PULSE, UP TIME IS',D12.4,' SEC. AND PERIOD IS',D12.4,' S 2EC. '/'OONE PULSE TRAIN CONTAINS',I4,' PULSES AND LASTS',D12.4,' SE
                                                                               142
                                                                               143
  3C. /'UTHE INCIDENT WAVE IS CUT OFF AFTER',D12.4,' SEC. AND THE TEM APERATURE IS OBSERVED AFTER',D12.4,' SEC.')
                                                                               144
                                                                               145
   IF (NPUL.GT.O.AND.TDUR.GT.O.DO.AND.TCUT.GT.O.DO.AND.T1ME.GT.O.DO)
                                                                               146
                                                                               147
  1G0 TO 24
                                                                               148
21 PRINT 22
22 FORMAT ('**** ERROR IN TIMES ****')
                                                                               149
                                                                               150
   STOP
24 IF (TPER.LT.TDUR.OR.TBPER.LT.NPUL*TPER) GO TO 21
                                                                               151
   ITME=ITME+1
                                                                               152
   IF (ITME.GT.1) GO TO 215
                                                                               153
                                                                               154
   PRINT 25
25 FORMAT ('OREGION
                        SURFACE
                                                                    THERMAL
                                                                               155
                                    RELATIVE
                                                   ELECTRIC
  1
        DENSITY
                    SPECIFIC
                                BLOOD FLOW
                                                TISSUE'/
                                                                               156
                                              9X, 'BOUNDARY
                                                              DIELECTRIC C
                                                                               157
  10NDUCTIVITY CONDUCTIVITY', 16X, 'HEAT', 8X, 'RATE
                                                              TYPE'/
                                                                               158
                                                         21X, 'CONSTANT'/11X
                                                                               159
  1,'(CM)',20X,'(MHO/N)
                             (CAL/CM-SEC-C)
                                               (G/CM3)
                                                         (CAL/G/S)
                                                                               160
                                                                        (CC/
  1SEC)'/)
                                                                               161
   OMEGA=2.D6*PIE*FREO
                                                                               162
   FAC1=OMEGA/VEL
                                                                               163
   START=1.D38
                                                                               164
   XMASS=0.DO
                                                                               165
   GLDVOL=0.DO
                                                                               166
 ******READ LAYER PROPERTIES AND COMPUTE PROPAGATION CONSTANTS
                                                                               167
```

```
DO 65 I=1.NORG
                                                                           168
   READ (5,30)SBDP(I),EPSP(I),SIGP(I),TCP(I),RHOP(I),CP(I),BFRP(I),
                                                                           169
  1 \text{ ITIS}(I)
                                                                           170
30 FORMAT (7F10.0.I5)
                                                                           171
         SBDP
                 OUTER RADIUS OF LAYER IN CENTIMETERS
                                                                           172
         BDP
                 LAYER OUTER RADIUS IN METERS
                                                                           173
         EPSP
                 PERMITTIVITY (RELATIVE)
                                                                           174
                 CONDUCTIVITY (MHOS PER METER)
         SIGP
                                                                           175
                 THERMAL CONDUCTIVITY
         TCP
                                                                           176
         RHOP
                 DENSITY
                                                                           177
         CP
                 SPECIFIC HEAT
                                                                           178
         BFRP
                 BLOOD FLOW RADIAL PERVICIVITY
                                                                           179
         ITIS
                 CODE FOR LAYER TISSUE TYPE
                                                                           180
           1 DENOTES CEREBROSPINAL FLUID
                                                                           181
           2 DENOTES BLOOD
                                                                           182
           3 DENOTES MUSCLE
                                                                           183
            4 DENOTES SKIN OR DURA
                                                                           184
           5 DENOTES BRAIN
                                                                           185
           6 DENOTES FAT OR BONE
                                                                           186
            7 DENOTES YELLOW BONE MARROW
                                                                           187
   BDP(I)=SBDP(I)/1.D2
                                                                           188
   VOL=4.D0*PIE*BDP(I)**3/3.D0
                                                                           189
   RVOL=VOL-OLDVOL
                                                                           190
   XMASS=XMASS+RVOL*RHOP(I)*1.D3
                                                                           191
   OLDVOL=VOL
                                                                           192
   BP(I)=RHOBP*CBP*BFRP(I)
                                                                           193
   A=BP(I)/(RHOP(I)*CP(I))
                                                                           194
   IF (A.LT.START) START=A
                                                                           195
   IF (I.EQ.1.OR.SBDP(I).GT.SBDP(I-1)) GO TO 45
                                                                           196
   PRINT 40
                                                                           197
40 FORMAT ('0**** LAYER RADII MUST BE IN ASCENDING ORDER ****')
                                                                           198
   STOP
                                                                           199
45 IF (ITIS(I).GT.O.AND.ITIS(I).LT.8) GO TO 55
                                                                           200
   PRINT 50, I, ITIS(I)
                                                                           201
50 FORMAT ('0****TISSUL TYPE CODE FOR LAYER', 12, ' IS', 15, ', OUTSIDE T 202
  1HE RANGE 1-7****)
                                                                           203
   STOP
                                                                           204
55 IF (EPSP(I).NE.O.DO.AND.SIGP(I).NE.O.DO) GO TO 60
                                                                           205
   CALL EPROP (FREQ, ITIS(I), EP, SIG)
                                                                           206
   IF (EPSP(I).EQ.0.DO) EPSP(I)=EP
                                                                           207
   IF (SIGP(I).EQ.O.DO) SIGP(I)=SIG
                                                                           208
60 FAC2=EPSP(I)/2.DO
                                                                           209
   FAC3=DSORT(1.D0+(1.D0/(EPSO*OMEGA)**2)*(SIGP(I)/EPSP(I))**2)
                                                                           210
   FKP(I)=DCMPLX(FAC1*DSQRT(FAC2*(FAC3+1.DO)),FAC1*DSQRT(FAC2*(FAC3-1
                                                                           211
  1.D0)))
                                                                           212
65 PRINT 70, I, SBDP(I), EPSP(I), SIGP(I), TCP(I), RHOP(I), CP(I), BFRP(I), TI
                                                                           213
  1SSUE(ITIS(I))
                                                                           214
70 FORMAT (14, F12.2, F12.2, F13.3, F15.6, F13.4, F10.3, F12.5, 3X, A8)
                                                                           215
   FKP(NORG+1)=DCMPLX(FAC1,0.D0)
                                                                           216
   IF (START.EQ.O.DO) START=1.D-9
                                                                           217
         COMPUTE EXPANSION COEFFICIENTS AND TOTAL ABSORBED POWER
                                                                           218
   CALL COEF
                                                                           219
   NN=NORG*NMIN
                                                                           220
   QS=0.D0
                                                                           221
   OT=0.00
                                                                           222
   DO 75 N=1.NMIN
                                                                           223
   FACN=2*N+1
                                                                           224
```

```
225
    NNN=NN+N
    X3=FACN*DREAL (ALPNP(NNN)+BETNP(NNN))
                                                                            226
    Y3=FACN*(CDABS(ALPNP(NNN))**2+CDABS(BETNP(NNN))**2)
                                                                            227
                                                                            228
    OT=QT~X3
                                                                            229
    QS=QS+Y3
    IF (DABS(X3).LT.DABS(QT)*1.D-6.AND.Y3.LT.QS*1.D-6) GO TO 242
                                                                            230
75 CONTINUE
                                                                            231
                                                                            232
    PRINT 241
241 FORMAT('0**** TOO FEW EXPANSION COSFFICIENTS ****')
                                                                            233
242 TOTPOW=2.65441D-3*E0**2*2.D0*PIE*(QT-QS)/(2.D0*FAC1*FAC1)
                                                                            234
                                                                            235
    PAVG=TOTPOW/VOL
    PAVG1=1.D3*TOTPOW/XMASS
                                                                            236
***
         PRINT OUT AVERAGE ABSORBED POWER DENSITY AND TOTAL ABSORBED
                                                                            237
                                                                            238
         POWER
    PRINT 80, XMASS, VOL, PAVG, ZLAB(2), PAVG1, ZLAB(1), TOTPOW
                                                                            239
80 FORMAT ('OWEIGHT =',1PD12.4,' KG'/'OVOLUME =',D12.4,' M**3'/
                                                                            240
   1'OFOR A CONTINUOUS WAVE THE AVERAGE ABSORBED POWER IS', D13.5, A7, '
                                                                            241
   10R',D13.5,A7/
                                                                            242
   1'OTOTAL ABSORBED POWER =',D13.5,' WATTS'/
                                                                            243
             'OROOTS OF THE EIGENFUNCTION'/)
                                                                            244
                                                                            245
          GET ROOTS OF EQUATION
    STEP=1.D-8
                                                                            246
    ICODE=0
                                                                            247
    AJ1=1.D0
                                                                            248
      PRINT 543, START, STEP
                                                                            249
      FORMAT ('OSTART =',1PD15.7,' STEP =',D15.7)
                                                                            250
    DO 90 NSBF=1.NMAX
                                                                            251
    AJ1=AJ1*(2*NSBF-1)
                                                                            252
    CALL RENDR (START, STEP, 1.D-6, KMAX, 1000, 10000)
                                                                            253
    START=XLAMDA(1,NSBF)
                                                                            254
    STEP=(XLAMDA(2, NSBF)-XLAMDA(1, NSBF))/10.DO
                                                                            255
    N1=NSBF-1
                                                                            256
    PRINT 95,N1,(XLAMDA(K,NSBF),K=1,KMAX)
                                                                            257
 95 FORMAT(1H , I5, 1PD12.4, 9D12.4/(7X, 10D12.4))
                                                                            258
    IF (NSBF.EQ.1) GO TO 90
                                                                            259
                                                                            260
    DO 89 K=1.KMAX
    IF (XLAMDA(K,NSBF).LE.XLAMDA(K,NSBF-1))GO TO 500
                                                                            261
 89 CONTINUE
                                                                            262
 90 CONTINUE
                                                                            263
                                                                            264
    ICODE=1
          DEVELOP U(N,M,K) ARRAY
                                                                            265
    DO 100 I=1.5
                                                                            266
    IF (MP.EQ.NPOINT(I)) GO TO 110
                                                                            267
100 CONTINUE
                                                                            268
    PRINT 105.MP
                                                                            269
105 FORMAT ('OINTEGRATION CONTROL =',19,' IS NOT AVAILABLE')
                                                                            270
    STOP
                                                                            271
110 JF=KEY(I)
                                                                            272
                                                                            273
    JL=KEY(I+1)-1
                                                                            274
    DO 115 J=1.5
    IF (MP1.EQ.NPOINT(I)) GO TO 120
                                                                            275
115 CONTINUE
                                                                            276
                                                                            277
    PRINT 105,MP1
    STOP
                                                                            278
                                                                            279
120 JF1=KEY(I)
    JL1=KEY(I+1)-1
                                                                            280
    PD2=PIE/2.DO
                                                                            281
```

K=1	282
DO 130 J=JF1,JL1	283
IF (Y(J).NE.O.DO) GO TO 125	284
THET1(K)=PD2	285
WTTH(K)=WT(J)	286
SINTH1(K)=1.00	287
COSTH1(K)=0.DO	288
GO TO 130	289
125 PDY=PD2*Y(3)	290
THET1(K)=P·)2+PDY	291
WTTH(K)=WT(J)	292
SINTH1(K)=DSIN(THET1(K))	293
COSTH1(K)=DCOS(THET1(K))	294
	295
K=K+1	
THET1(K)=PD2~PDY	296
WTTH(K)=WT(J)	297
SINTH1(K)=DSIN(THET1(K))	298
COSTH1(K)=DCOS(THET1(K))	299
130 K=K+1	300
E0S0=E0*E0	301
MAX=NMI N+15	302
	303
IF (MAX.GT.100) MAX=100	
CLEAR STORAGE FOR INTEGRALS	304
DO 135 NSBF=1,NMAX	305
DO 135 M=1,2	306
DO 135 NRT=1,KMAX	307
DEN(NSBF,M,NRT)=0.DO	308
135 XNUM(NSBF,M,NRT)≈0.DO	309
SUM OVER REGIONS	310
	311
DO 210 NREG=1,NORG	
IREG=NREG	312
PRECALCULATE THE POWER DENSITY TIMES PHI INTEGRAL	313
FIRST CALCULATE RADIUS DEPENDENT PART OF SOURCE TERM	314
NN=(NREG-1)*NMIN	315
R1=ŠBDP(NRĖG)	316
R2=0.DC	317
IF (MREG.GT.1) R2=SBDP(NREG-1)	318
R11=R1+R2	319
R13=R1-R2	320
RAVG=R13/2.D0	321
RCP=RHOP(NREG)*CP(NREG)	322
FAC=EOSQ*.5DO*SIGP(NREG)/4186.D3	323
J=0	324
DO 180 J3=JF,JL	325
IF (Y(J3).NE.O.DO) GG TO 140	326
13=1	327
ARG3(1)=R11	328
GO TO 145	329
140 I3=2	330
R12=R13*Y(J3)	331
ARG3(1)=RÌ1+Ŕ12	332
ARG3(2)=R11-R12	333
145 DO 180 L=1,I3	334
R=ARG3(L)/2.D0	335
	336
J=J+1 pp(1)-p	330 337
RR(J)=R	
R=R/100.D0	338

```
339
    ()=R*FKP(NREG)
    CALL BJYH (BJNP, BHNP, Q, NC, STOPR, NMIN+2)
                                                                                340
    NC=MINO(NC-2,NMIN)
                                                                                341
                                                                                342
    NCK=0
    DO 150 N=1.NC
                                                                                343
    FAC1=2*N+1
                                                                                344
    NNN=NN+N
                                                                                345
    W=BNP(NNN)
                                                                                346
    X=BJNP(N+1)
                                                                                347
    Y1=BETNP(NNN)
                                                                                348
    Z=BHNP(N+1)
                                                                                349
    NCK=NCK+1
                                                                                350
    T=FAC1*(W*X+Y1*Z)
                                                                                351
    CALL TERM(NCK,T,1)
                                                                                352
    TR(N)=T
                                                                                353
    T=ANP(NNN)*X+ALPNP(NNN)*Z
                                                                                354
    CALL TERM(NCK,T,0)
                                                                                355
    TE(N)=\Gamma
                                                                                356
    A=N+1
                                                                                357
    B=N
                                                                                358
    T=(W*(A*RJNP(N)-B*BJNP(N+2))+Y1*(A*BHNP(N)-B*BHNP(N+2)))/FAC1
                                                                                359
    CALL TERM(NUK,T,1)
                                                                                360
    TER(N)=T
                                                                                361
150 IF (NCK.EQ.4)NCK=0
                                                                                362
           THEN CALCULATE THETA DEPENDENT PART OF SOURCE TERM
                                                                                363
    DO 180 J2=1.MP1
                                                                                364
    THETA=THET1(J2)
                                                                                365
    SINTH=SINTH1(J2)
                                                                                366
    COSTH=COSTH1(J2)
                                                                                367
    CALL PL
                                                                                368
    ERAD=DCMPLX(0.D0,0.D0)
                                                                                369
    ETHETA=DCMPLX(0.D0,0.D0)
                                                                                370
    EPHI=DCMPLX(0.D0,0.D0)
                                                                                371
    ITP=0
                                                                                372
    IR=0
                                                                                373
    DO 165 N=1.NC
                                                                                374
    FAC1=2*N+1
                                                                                375
    IF (IR.EQ.1) GO TO 155
                                                                                376
    T=P(N)*TR(N)
                                                                                377
    ERAD=ERAD+T
                                                                                378
    IF (CDABS(T).LT.CDABS(ERAD)*EPS)IR=1
                                                                                379
155 IF (ITP.EQ.1) GO TO 160
                                                                                380
    NP1=N+1
                                                                                381
    RATIO=FAC1/(N*NP1)
                                                                                382
    A=RATIO*P(N)/SINTH
                                                                                383
    B=-RATIO*DP(N)
                                                                                384
    C=A*TE(N)+B*TE1(N)
                                                                                385
    ETHETA=ETHETA+C
                                                                                386
    T=A*TE1(N)+B*TE(N)
                                                                                387
    EPHI=EPHI+T
                                                                                388
    IF (CDABS(C).LT.CDABS(ETHETA)*EPS.AND.CDABS(T).LT.CDABS(EPHI)*EPS)
                                                                                389
   1ITP=1
                                                                                390
160 IF (IR+ITP.EQ.2) GO TO 175
                                                                                391
165 CONTINUE
                                                                                392
PRINT 170, NMIN, NC, THETA, R, STOPR, EPS

170 FORMAT (15X, 'NMIN =', 13, 'NC =', 13, 'THETA =', F9.6, 'R =', 2PF9.6, '
                                                                                393
                                                                                394
   1 STOPR =',1PD9.2,' IS TOO SMALL FOR ACCURACY OF', D9.2)
                                                                                395
```

```
396
175 ERAD=ERAD/O
          STORE SOURCE TERM TIMES PHI INTEGRAL
                                                                             397
    ERT=DREAL(ERAD*DCONJG(FRAD)+ETHETA*DCONJG(ETHETA))
                                                                             398
    EP1=DREAL (EPHI*DCONJG (EPHI))
                                                                             399
    S(J.J2.1
                 )=FAC*PIE*(ERT+EP1)
                                                                             400
                 )=FAC*PD2*(ERT-EP1)
180 S( J,J2,2
                                                                             401
          CALCULATE NUMERATOR AND DENOMINATOR INTEGRALS
                                                                             402
    DO 210 NSBF=1.NMAX
                                                                             403
    N1=NSBF-1
                                                                             404
    DO 210 M=1,NSBF
                                                                             405
    IF (M.NE.1.AND.M.NE.3) GO TO 210
                                                                             406
    M2=M/2+1
                                                                             407
    M1 = M - 1
                                                                             408
    DO 185 J=1.MP1
                                                                             409
185 ALPOL(J)=ALP(N1,M1,COSTH1(J))*SINTH1(J)
                                                                             410
    D0 195 J3 = 1,MP
                                                                             411
    SUMJ2= 0.D0
                                                                             412
    DO 190 J2 = 1,MP1
                                                                             413
190 SUMJ2 = SUMJ2 + WTTH(J2)*S(J3,J2,M2)*ALPOL(J2)
                                                                             414
195 \text{ SUM2}(J3,M2) = \text{SUMJ2}
                                                                             415
          SUM2 IS THE INTEGRAL OF THE SOURCE TERM TIMES ALPOL
                                                                             416
          ALPOL IS THE PRODUCT OF THE LEGENDRE POLYNOMIAL TIMES THE
                                                                             417
             SINE OF THETA
                                                                             418
          J2 IS AN INDEX FOR THE THETA COORDINATE ASSOCIATED WITH
                                                                             419
             GAUSSIAN INTEGRATION
                                                                             420
    DO 205 NRT=1,KMAX
                                                                             421
          INTEGRATE OVER RADIUS
                                                                             422
    F=FACT(IREG,NRT,NSBF)
                                                                             423
    S1=XLAMDA(NRT, NSBF) *RCP-BP(IREG)
                                                                             424
    SUM=0.DO
                                                                             425
    CUM3=0.D0
                                                                             426
    DO 200 J3=1,MP
                                                                             427
    R=RR(J3)
                                                                             428
                                                                             429
    R1=R
    CALL SRBF(XJ.XY.DJ.DY)
                                                                             430
    ZZ=AJ(NREG,NRT,NSBF)*XJ +BY(NREG,NRT,NSBF)*XY
                                                                             431
    IF (DABS(XY).GT.1.D34) PRINT 666, NSBF, M, NRT, AJ (NREG, NRT, NSBF),
                                                                             432
   1 XJ, BY (NREG, NRT, NSBF), XY, ZZ
                                                                             433
666 FORMAT (315,1P7D15.7)
                                                                             434
    RSO=R*R
                                                                             435
          INTEGRATE OVER THETA
                                                                             436
    J=JF+(J3-1)/2
                                                                             437
    WTJ=WT(J)*ZZ*RSQ
                                                                             438
    SUM=SUM+WTJ*ZZ
                                                                             439
(200 \text{ SUM3} = \text{SUM3} + \text{WTJ*SUM2}(J3,M2))
                                                                             440
    DEN(NSBF,M2,NRT)=DEN(NSBF,M2,NRT)+RCP*SUM*RAVG
                                                                             441
205 XNUM(NSBF,M2,NRT)=XNUM(NSBF,M2,NRT)+SUM3*RAVG
                                                                             442
210 CONTINUE
                                                                             443
          CALCULATE COEFFICIENTS U(N,M,K)
                                                                             444
215 IF (TCUT.GT.TIME) TCUT=TIME
                                                                             445
    IA=TCUT/TBPER
                                                                             446
    IC=(TCUT-IA*TBPER)/TPER
                                                                             447
    IB=MINO(NPUL,IC)
                                                                             448
    XL=IA*TBPER+IB*TPER
                                                                             449
    D=0.D0
                                                                             450
    IF (IC.LT.NPUL) D=1.
                                                                             451
    XU=DMIN1 (TCUT, XL+D*TDUR)
                                                                             452
```

	TA=TIME-TDUR-(IA-1)*TBPER-(NPUL-1)*TPER	453
	TB=TIME-TDUR-IA*TBPER-(IB-1)*TPER	454
	PRINT 220	455
220	FORMAT ('OU COEFFICIENTS')	456
	DO 270 NSBF=1,NMAX	457
	PRINT 225	458
		-
225	FORMAT (' ')	459
	N1=NSBF-1	460
	DO 270 M=1,NSBF	461
		462
	IF (M.NE.1.AND.M.NE.3) GO TO 270	
	M1=M-1	463
	M2=M/2+1	464
	NMM=N1-M1	465
	NPM=N1+M1	466
		-
	F=1.D0	467
	IF (M1.EQ.O) GO TO 255	468
	IF (N1.NE.M1) GO TO 240	469
	DO 235 I=2,NPM	470
025		
235	F=F*I	471
	GO TO 250	472
240	I I=2*M1	473
	F1=NMM+1	474
		475
	DO 245 I=1,II	
	F=F*F1	476
245	F1=F1+1.D0	477
	F=1.D0/F	478
		479
200	F=(2.D0*N1+1.D0)/(2.D0*PIE)*F*PD2	_
	DO 260 NRT=1,KMAX	480
	IF (M.NE.1) GO TO 260	481
	XR=XLAMDA(NRT,NSBF)	482
	D=0.D0	483
	IF (IA+IB.EQ.0) GO TO 258	484
	X1=XR*TPER	485
	X3=1.00	486
	IF (X1.LE.40.DO) X3=1.DO-DEXP(-X1)	487
		488
	IF (IA.LE.0) GO TO 256	
	X4=XR*TA	489
	IF (X4.GT.87.DO) GO TO 256	490
	X1=XR*NPUL*TPER	491
		492
	X5=1.00	
	IF (X1.LE.40.DO) X5=1.DO-DEXP(-X1)	493
	X1=XR*TBPER	494
	X6=1.D0	495
	X7=1.00	496
	IF (X1.GT.40.DO) GO TO 261	497
	X6=1.D0-DEXP(-X1)	498
	X1=X1*IA	499
	IF (X1.LE.40.DO) X7=1.DO-DEXP(-X1)	500
261		501
	D=D+DEXP(-X4)*X5*X7/(X3*X6)	
256	IF (IB.LE.O) GO TO 257	502
	X4=XR*TB	503
	IF (X4.GT.87.DO) GO TO 257	504
	X1=XR*IB*TPER	505
	X5=1.D0	506
	IF (X1.LE.40.D0) X5=1.D0-DEXP(-X1)	507
	D=D+DEXP(-X4)*X5/X3	508
クヒフ	X1=XR*TDUR	509
43/	VIVE IDAV	703

```
510
    X4=1.D0
                                                                            511
    IF (X1.LE.40.D0) X4=1.D0-DEXP(-X1)
                                                                             512
    D=D*X4
                                                                             513
258 IF (XU.LE.XL) GO TO 259
                                                                             514
    X1=XR*(TIME-XU)
    IF (X1.GE.87.D0) GO TO 259
                                                                            515
    X3=XR*(XU-XL)
                                                                             516
                                                                             517
    X4=1.D0
    IF (X3.LE.40.D0) X4=1.D0-DEXP(-X3)
                                                                             518
    D=D+DEXP(-X1)*X4
                                                                             519
                                                                             520
259 ETIME(NRT)=D/XR
260 U(NSBF, M2, NRT)=ETIME(NRT)*F*XNUM(NSBF, M2, NRT)/DEN(NSBF, M2, NRT)
                                                                             521
                                                                             522
    PRINT 265,N1,M1, (U(NSBF,M2,K),K=1,KMAX)
265 FORMAT (213,1P10D12.4/(8X,10D12.4))
                                                                             523
270 CONTINUE
                                                                             524
***
         ABSORBED-POWER DENSITY AND TEMPERATURE RISE AT
                                                                             525
         GIVEN POINTS INTERIOR TO P-TH REGION
                                                                             526
    IF (ISAR.NE.O) ISAR=1
                                                                             527
    PRINT 275, ZLAB (ISAR+1)
                                                                             528
275 FORMAT ('0',29X,'INTERNAL POINT',11X,'ABSORBED POWER',7X,'TEMPERAT
                                                                             529
   1URE',8X,'APPROXIMATE'
                                                                             530
        /11X, 'POINT REGION RADIUS THETA
                                                  PHI'.12X, 'DENSITY'.14X,
                                                                             531
   1'RISE',14X,'ERROR'
1/28X,'CM DEG
                                                                             532
                           DEG',12X,A7,13X,'DEG C',13X,'PER CENT'/)
                                                                             533
                                                                             534
    DO 345 II=1,NOCR
    READ (5,30) R, THETAD, PHID
                                                                             535
                                                                             536
                    R-COORDINATE OF PT
          THETAD
                    THETA COORDINATE (DEGREES)
                                                                             537
                    PHI-COORDINATE(IN EQUATORIAL PLANE)(DEGREES)
                                                                             538
          PHID
    IF (R.LE.O.DO) GO TO 290
                                                                             539
    DO 285 NEEG=1, NORG
                                                                             540
    IF (R.LE.SBDP(NREG)) GO TO 300
                                                                             541
285 CONTINUE
                                                                             542
290 NREG=1000000000
                                                                             543
    PRINT 295, II, NREG, R, THETAD, PHID
                                                                             544
295 FORMAT (114,18,3F10.3,' ** THE RADIUS IS OUTSIDE THE SPHERE **')
                                                                             545
                                                                             546
           NREG = NUMBER OF THE REGION IN WHICH TEMP IS TO BE COMPUTED
                                                                             547
300 IREG=NREG
                                                                             548
                                                                             549
    R1=R
    R=R/1.D2
                                                                             550
    THETA=THETAD/RAD
                                                                             551
    PHI=PHID/RAD
                                                                             552
    CALL BJYH(BJNP, BHNP, FKP(NREG) *R, NC, STOPR, NMIN+2)
                                                                             553
    NC=MINO(NC-2,NMIN)
                                                                             554
    SINTH=DSIN(THETA)
                                                                             555
    COSTH=DCOS(THETA)
                                                                             556
    CALL PL
                                                                             557
    CALL EVEC(PD)
                                                                             558
    PD=.5DO*SIGP(NREG)*PD
                                                                             559
    KMAX1=KMAX
                                                                             560
    K1=KMAX-1
                                                                             561
    DO 315 KMAX=K1,KMAX1
                                                                             562
    TRM=0.D0
                                                                             563
    DO 315 NSBF=1,NMAX
                                                                             564
    N1=NSBF-1
                                                                             565
    DO 315 M=1,NSBF
                                                                             566
```

```
567
    IF (M.NE.1.AND.M.NE.3) GC TO 315
                                                                           568
    M1 = M - 1
                                                                           569
    M2=M/2+1
                                                                           570
    ALPNM=ALP(N1,M1,COSTH)*DCOS(M1*PHI)
                                                                           571
    IF (ALPNM.EQ.O.DO) GO TO 310
                                                                           572
    SUM=0.DO
    DO 305 NRT=1,KMAX
                                                                           573
    S1=XLAMDA(NRT,NSBF)*RHOP(IREG)*CP(IREG)-BP(IREG)
                                                                           574
                                                                           575
    F=FACT(IREG,NRT,NSBF)
                                                                           576
    CALL SRBF(XJ, XY, DJ, DY)
305 SUM=SUM+U(NSBF.M2,NRT)*(AJ(NREG,NRT,NSBF)*XJ+BY(NREG,NRT,NSBF)*XY)
                                                                           577
                                                                           578
310 TRM=TRM+SUM*ALPNM
                                                                           579
    IF (M.NE.3) GO TO 315
       (KMAX.EO.K1.AND.NSBF.EQ.NMAX) SRM1=TRM
                                                                           580
                                                                           58.1
    IF (KMAX.EQ.KMAX1.AND.NSBF.EQ.NMAX-1) SBFM1=TRM
                                                                           582
315 CONTINUE
                                                                           583
    KMAX=KMAX1
    PCER=(TRM-SRM1)/TRM
                                                                           584
                                                                           585
    PCEBF=(TRM-SBFM1)/TRM
    IF (ISAR.EQ.O)PD=PD/RHOP(NREG)
                                                                           586
         PRINT PARTICULARS OF INTERIOR POINT OF REGION P
                                                                           587
    PRINT 340.II.NREG.R1.THETAD.PHID.PD.TRM.PCEBF.PCER
                                                                           588
                                                                           589
340 FORMAT (114,18,F10.3,2F8.2,F19.8,1PD20.4,2P2F14.7)
345 CONTINUE
                                                                           590
    IF (IPL1.EQ.O.AND.IPL2.EQ.O) GO TO 10
                                                                           591
    IF (IPLSW.EQ.1) GO TO 350
                                                                           592
    IPLSW=1
                                                                           593
    CALL PLOTS(0,0,8)
                                                                           594
                                                                           595
    CALL PLOT(0.,-11.,-3)
    CALL PLOT(G.,2.,-3)
                                                                           596
    NTR=MAXO(NTR,1)
                                                                           597
                                                                           598
    NTR=MINO(NTR,5)
                                                                           599
350 IF (IPL1.EQ.0) GO TO 405
                                                                           600
*** PLOT POWER DENSITIES ALONG Z, X AND/OR Y AXIS
    NPTS=300
                                                                           601
                                                                           602
    NPTD2=NPTS/2
                                                                           603
    NP2=NPTD2+1
                                                                           604
    DX=SBDP(NORG)/NPTD2
                                                                           605
    DO 400 KJI=1,3
    IF (KJI.EQ.1.AND.(IPL1.EQ.2.OR.IPL1.EQ.3.OR.IPL1.EQ.6)) GO TO 400
                                                                           606
    IF (KJI.EQ.2.AND.(IPL1.EQ.1.OR.IPL1.EQ.3.OR.IPL1.EQ.5)) GO TO 400
                                                                           607
                                                                           608
    IF (KJI.EQ.3.AND.(IPL1.EQ.1.OR.IPL1.EQ.2.OR.IPL1.EQ.4)) GO TO 400
                                                                           609
    PRINT 355
355 FORMAT ('0')
                                                                           610
    TRMAX=0.
                                                                           611
    COSTH=0.DO
                                                                           612
                                                                           613
    IF (KJI.EQ.1) COSTH=1.DO
                                                                           614
    IREG=NORG
                                                                            615
    R1=SBDP(NORG)
*** CALCULATE POWER DENSITIES ALONG SPHERE DIAMETER
                                                                           616
    DO 370 I=1.NP2
                                                                            617
                                                                           618
    RC=RHOP(IREG)*CP(IREG)
    BP1=BP(IREG)
                                                                            619
                                                                            620
    TRM=0.DO
                                                                            621
    TRM1=0.D0
                                                                            622
    DO 365 NSBF=1.NMAX
                                                                            623
    N1=NSBF-1
```

```
624
    COSMP=1.DO
    DO 365 M=1.NSBF
                                                                            625
    IF (M.NE.1.AND.M.NE.3) GO TO 365
                                                                            626
    IF (KJI.EQ.3.AND.M.EQ.3) COSMP=-1.DO
                                                                            627
    M1 = M - 1
                                                                            628
    M2=M/2+1
                                                                            629
    SUM=0.DO
                                                                            630
    DO 360 NRT=1,KMAX
                                                                            631
    S1=XLAMDA(NRT, NSBF)*RC-BP1
                                                                            632
    F=FACT(IREG,NRT,NSBF)
                                                                            633
    CALL SRBF(XJ.XY.DJ.DY)
                                                                            634
360 SUM=SUM+U(NSBF, M2, NRT)*(AJ(IREG, NRT, NSBF)*XJ+BY(IREG, NRT, NSBF)*XY)
                                                                            635
    TRM=TRM+SUM*ALP(N1.M1.COSTH)*COSMP
                                                                            636
    TRM1=TRM1+SUM*ALP(N1,M1,-COSTH)*COSMP
                                                                            637
365 CONTINUE
                                                                            638
    R3(I)=R1
                                                                            639
    TR3(I)=TRM
                                                                            640
    R3(NPTS-I+3)=-R1
                                                                            641
    TR3(NPTS-I+3)=TRM1
                                                                            642
    TRMAX=DMAX1(TRM,TRM1,TRMAX)
                                                                            643
                                                                            644
    R1=R1-DX
    IF (IREG.GT.1.AND.R1.LT.SBDP(IREG-1))IREG=IREG-1
                                                                            645
370 IF (R1.LT..0001)R1=.0001
                                                                            646
*** DETERMINE PLOT SCALE FOR POWER DENSITIES
                                                                            647
    PD3=.0001
                                                                            648
    DO 375 I=1,10
                                                                            649
    PD3=5.*PD3
                                                                            650
    IF (TRMAX.LT.PD3) GO TO 380
                                                                            651
    PD3=PD3*2.
                                                                            652
    IF (TRMAX.LT.PD3) GO TO 380
                                                                            653
375 CONTINUE
                                                                            654
380 TRMAX=PD3
                                                                            655
*** PLOT POWER DENSITY ALONG DIAMETER ON Z. X OR Y AXIS
                                                                            656
    BLAB(1)=AX(KJI)
                                                                            657
    DO 390 I=1,NTR
                                                                            658
    ANG=2*(I-1)*PIE/NTR
                                                                            659
    AX1=.01*COS(ANG)
                                                                            660
    AY=.01*SIN(ANG)
                                                                            661
    IF (NTR.EQ.1) AX1=0.
                                                                            662
    CALL PLOT(AX1.AY.-3)
                                                                            663
390 CALL PLTCV1(R3,TR3,5.,6.,BLAB,DLAB,22,26,NPTS+2,0,1,1,-R3(1),
                                                                            664
   1R3(1), 0., TRMAX, 0, 0, .14, R3(1)/3., TRMAX/5., 1
                                                                            665
    CALL PLOT(7.,0.,-3)
                                                                            666
400 CONTINUE
                                                                            667
405 IF (IPL2.EQ.0) GO TO 10
                                                                            668
*** PLOT POWER DENSITY CONTOURS IN E PLANE. H PLANE AND/OR X-Y PLANE
                                                                            669
    NPTS=100
                                                                            670
    NPTD2=NPTS/2
                                                                            671
    NPTP2=NPTS+2
                                                                            672
    X1=SBDP(NORG)
                                                                            673
    XF=10./(2.*X1)
                                                                            674
    DX=X1/NPTD2
                                                                            675
    X3=X1
                                                                            676
    DO 410 I=1,NPTD2
                                                                            677
    X2(I)=X3
                                                                            678
    X2(NPTS+3-I)=-X3
                                                                             679
410 X3=X3-DX
                                                                             680
```

```
681
    X2(NPTD2+1)=.0001
                                                                            682
    X2(NPTD2+2)=-.0001
                                                                            683
*** CALCULATE POWER DENSITIES AT POINTS IN PLANE
                                                                            684
    N12=NPTP2/2
                                                                            685
    00.465 \text{ KJI}=1.3
    IF (KJI.EQ.1.AND.(IPL2.EQ.2.OR.IPL2.EQ.3.OR.IPL2.EQ.6)) GO TO 465
                                                                             686
                                                                             687
    IF (KJI.EQ.2.AND.(IPL2.EQ.1.OR.IPL2.EQ.3.OR.IPL2.EQ.5)) GO TO 465
                                                                             688
    IF (KJI.EQ.3.AND.(1PL2.EQ.1.OR.IPL2.EQ.2.OR.IPL2.EQ.4)) GO TO 465
                                                                             689
    Y3=0.
                                                                             690
    X3=0.
                                                                             691
    Z3=0.
                                                                             692
   DO 455 I=1.N12
                                                                             693
    I1=NPTS+3-I
                                                                             694
   DO 455 J=1.N12
                                                                             695
    J1=NPTS+3-J
                                                                             696
    IF (KJI.GT.1) GO TO 415
                                                                             697
    X3=X2(I)
                                                                             698
    Z3=X2(J)
                                                                             699
    GO TO 425
                                                                             700
415 IF (KJI.GT.2) GO TO 420
                                                                             701
    Y3=X2(I)
                                                                             702
    Z3=X2(J)
                                                                             703
    GO TO 425
                                                                             704
420 X3=X2(I)
                                                                             705
    Y3=X2(J)
                                                                             706
425 R1=DSQRT(X3*X3+Y3*Y3+Z3*Z3)
                                                                             707
    IF (R1.LE.X1) GO TO 430
                                                                             708
    DAR(I,J)=-1.
                                                                             709
    DAR(I,J1)=-1.
                                                                             710
    GO TO 453
                                                                             711
430 DO 435 IREG=1.NORG
                                                                             712
    IF (R1.LE.SBDP(IREG)) GO TO 440
                                                                             713
435 CONTINUE
*** CALCULATE TEMPERATURE RISE AT POINTS IN PLANE
                                                                             714
                                                                             715
440 COSTH=Z3/R1
                                                                             716
    PHI=DATAN2(Y3,X3)
                                                                             717
    RC=RHOP(IREG)*CP(IREG)
                                                                             718
    BP1=BP(IREG)
                                                                             719
    TRM=0.DO
                                                                             720
    TRM1=0.D0
                                                                             721
    DO 450 NSBF=1,NMAX
                                                                             722
    N1=NSBF-1
                                                                             723
    DO 450 M=1,NSBF
                                                                             724
    IF (M.NE.1.AND.M.NE.3) GO TO 450
                                                                             725
    M1=M-1
                                                                             726
    M2=M/2+1
                                                                             727
    SUM=0.DO
                                                                             728
    DO 445 NRT=1,KMAX
                                                                             729
    S1=XLAMDA(NRT, NSBF)*RC-BP1
                                                                             730
    F=FACT(IREG.NRT.NSBF)
                                                                             731
    CALL SRBF(XJ, XY, DJ, DY)
445 SUM=SUM+U(NSBF, M2, NRT)*(AJ(IREG, NRT, NSBF)*XJ+BY(IREG, NRT, NSBF)*XY)
                                                                             732
                                                                             733
    TRM=TRM+SUM*ALP(N1,M1,COSTH)*DCOS(M1*PHI)
                                                                             734
    TRM1=TRM1+SUH*ALP(N1,M1,-COSTH)*DCOS(M1*PHI)
                                                                             735
450 CONTINUE
                                                                             736
    DAR(I,J)=TRM
                                                                             737
    DAR(I,J1)=TRM1
```

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```
738
453 DAR(I1,J)=DAR(I,J)
                                                                             739
455 DAR(I1,J1)=DAR(I,J1)
                                                                              740
*** PLOT CONTOURS
                                                                              741
    DO 460 I=1.NTR
    ANG=2*(I-1)*PIE/NTR
                                                                              742
                                                                             743
    AX1=.01*COS(ANG)
                                                                              744
    AY=.01*SIN(ANG)
    IF (NTR.EQ.1) AX1=0.
                                                                              745
                                                                              116
    CALL PLOT(AX1,AY,-3)
    CALL SYMBOL (-.5,6.,.21,CLAB(1,KJI),0..9)
                                                                              747
                                                                              748
460 CALL CNTRP1(X2,NPTP2,X2,NPTP2,DAR,10,0,IFL)
                                                                              749
    CALL PLOT(10..0..-3)
                                                                              750
465 CONTINUE
    GO TO 10
                                                                              751
495 IF (IPLSW.NE.O) CALL PLOT(0..0..999)
                                                                              752
                                                                              753
500 STOP
                                                                              754
    END
                                                                              755
                                                                              756
    SUBROUTINE COEF
                                                                              757
    IMPLICIT REAL*8 (A-H.O-Z)
                                                                              758
         GENERATES EXPANSION COEFFICIENTS
                                                                              759
                                                                              760
    COMPLEX*16 FKP.ANP.BNP.ALPNP.BETNP.BJNP.BHNP.BJHP1(500).BJHP2(500)
   1,SJNP1(100),SHNP1(100),DELNP,SNT11,SNT12,SNT21,SNT22,TNT11,TNT12,T
                                                                              761
   1NT21.TNT22.ETAP1.ETAP2.ZEP1.ZEP2.SNP11.SNP12.SNP21.SNP22.TNP11.TNP
                                                                              762
   112, TNP21, TNP22, DEL1, DEL2, RATIO, Z
                                                                              763
    COMMON FKP(7), ANP(300), BNP(300), ALPNP(300), BETNP(300), BJNP(100), BH
                                                                              764
   1NP(100), BDP(6), P(51), DP(50), R, THETA, COSTH, PHI, SINTH, STOPR, EO
                                                                              765
    COMMON /A/NORG, NREG, NRT, NSBF, NMIN, NC, ICODE
                                                                              766
                                                                              767
    DIMENSION NTER(6)
         COMPUTE EXPANSION COEFFICIENTS ANI, BN1, ANN, BNN, ALPN1, BETN1,
                                                                              768
         ALPNN, BETNN
                                                                              769
    N^1 = 1
                                                                              770
                                                                              771
    NMIN=100
    DO 10 NR=1.NORG
                                                                              772
    CALL BJYH (SJNP1, SHNP1, FKP (NR) *BDP (NR), N, STOPR, NMIN)
                                                                              773
    CALL BJYH (BJNP. BHNP. FKP (NR+1) *BDP (NR), NN, STOPR, NMIN)
                                                                              774
                                                                              775
    NMIN=MINO(N,NN,NMIN)
                                                                              776
    N2=N1+NMIN
                                                                              777
    DO 5 I=1.NMIN
    BJHP1(N1)=SJNP1(I)
                                                                              778
                                                                              779
    BJHP1(N2)=SHNP1(I)
                                                                              780
    BJHP2(N1)=BJNP(I)
    BJHP2(N2)=BHNP(I)
                                                                              781
                                                                              782
    N1=N1+1
  5 N2=N2+1
                                                                              783
                                                                              784
    N1=N1+NMTN
 10 NTER(NR)=NMIN
                                                                              785
    NMIN=NMIN-2
                                                                              786
                                                                              787
    IF (NMIN.LE.50.AND.N2.LE.301) GO TO 20
    PRINT 15,N2,NMIN
                                                                              788
 15 FORMAT ('OCOEF ERROR: N2 ='.I3.' NMIN ='.I3.' DIMENSIONS ARE TOO
                                                                              789
   1 SMALL')
                                                                              790
                                                                              791
    STOP
                                                                              792
 20 DO 25 I=1,NMIN
    ALPNP(I)=DCMPLX(0.D0,0.D0)
                                                                              793
                                                                              794
 25 RETNP(I)=DCMPLX(0.D0.0.D0)
```

	NSUM=NORG*NMIN	795
	DO 35 I=1,NMIN	796
		797
	JJ=0	
	KK=0	798
	XI=I	799
	XI1=I+1	800
	XI2=2*I+1	801
	SNT11=DCMPLX(1.D0,0.D0)	802
	SNT12=DCMPLX(0.D0,0.D0)	803
	SNT21=SNT12	804
	• • • • • • • • • • • • • • • • • • • •	805
	SNT22=SNT11	
	TNT11=SNT11	806
	TNT12=SNT12	807
	TNT21=SNT12	808
	TNT22=SNT11	809
	DO 30 J=1,NORG	810
	KK=KK+NTER(J)	811
	KKI=KK+I	812
	JJI=JJ+I	813
		814
	ETAP1=(XI1*BJHP1(JJI)-XI*BJHP1(JJI+2))/XI2	
	ETAP2=(XI1*BJHP2(JJI)-XI*BJHP2(JJI+2))/XI2	815
	ZEP1=(XI1*BJHP1(KKI)-XI*BJHP1(KKI+2))/XI2	816
	ZEP2=(XI1*BJHP2(KKI)-XI*BJHP2(KKI+2))/XI2	817
	DELNP=BJHP1(JJI+1)*ZEP1-BJHP1(KKI+1)*ETAP1	818
	RATIO=FKP(J+1)/FKP(J)	819
	Z=RATIO*ETAP2	820
	SNP11=(ZEP1*BJHP2(JJI+1)-Z*BJHP1(KKI+1))/DELNP	821
	SNP21=(Z*BJHP1(JJI+1)-ETAP1*BJHP2(JJI+1))/DELNP	822
		823
	Z=RATIO*ZEP2	
	SNP12=(ZEP1*BJHP2(KKI+1)-Z*BJHP1(KKI+1))/DELNP	824
	SNP22=(Z*BJHP1(JJI+1)-ETAP1*BJHP2(KKI+1))/DELNP	825
	Z=SNT11	826
	SNT11=SNT11*SNP11+SNT12*SNP21	827
	-	
	SNT12=Z*SNP12+SNT12*SNP22	828
	Z=SNT21	829
	SNT21=SNT21*SNP11+SNT22*SNP21	830
	SNT22=Z*SNP12+SNT22*SNP22	831
	Z=RATIO*ZEP1	832
	TNP11=(Z*BJHP2(JJI+1)-BJHP1(KKI+1)*ETAP2)/DELNP	833
	TNP12=(Z*BJHP2(KKI+1)-BJHP1(KKI+1)*ZEP2)/DELNP	834
	Z=RATIO*ETAP1	835
	TNP21=(BJHP1(JJI+1)*ETAP2-Z*BJHP2(JJI+1))/DELNP	836
	TNP22=(BJHP1(JJI+1)*ZEP2-Z*BJHP2(KKI+1))/DELNP	837
	Z=TNT11	838
	TNT11=TNT11*TNP11+TNT12*TNP21	839
	TNT12=Z*TNP12+TNT12*TNP22	840
	Z=TNT21	841
		842
	TNT21=TNT21*TNP11+TNT22*TNP21	
	TNT22=Z*TNP12+TNT22*TNP22	843
	JJ=JJ+2*NTER(J)	844
30	KK=KK+NTER(J)	845
	ANP(I)=SNT11-(SNT12*SNT21)/SNT22	846
	BNP(I)=TNT11-(TNT12*TNT21)/TNT22	847
	LL=NSUM+I	848
	ANP(LL)=DCMPLX(1.D0,0.D0)	849
	BNP(LL)=DCMPLX(1.D0,0.D0)	850
	ALPNP(LL)=-SNT21/SNT22	851
	MELIAL (FE) 30151/30155	031

```
35 BETNP(LL)=-TNT21/TNT22
                                                                           852
                                                                           853
   IF (NORG.EQ.1) RETURN
        COMPUTE EXPANSION COEFFICIENTS AN2,...,AN(N-1);BN2,...,BN(N-1
                                                                           854
                                                                           855
        );ALPN2...,ALPN(N-1);BETN2....BETN(N-1)
                                                                           856
   JJ=0
  KK=0
                                                                           857
                                                                           858
  MM1=0
                                                                           859
  MM2=NMIN
   NRGM1=NORG-1
                                                                           860
                                                                           861
  DO 45 J=1.NRGM1
   KK=KK+NTER(J)
                                                                           862
  DO 40 I=1,NMIN
                                                                           863
                                                                           864
   KKI=KK+I
                                                                           865
   JJI=JJ+I
                                                                           866
   XI = I
                                                                           867
   XI1=I+1
                                                                           868
   X12=2*1+1
   ETAP1=(XI1*BJHP1(JJI)-XI*BJHP1(JJI+2))/XI2
                                                                           869
   ETAP2=(XI1*BJHP2(JJI)-XI*BJHP2(JJI+2))/XI2
                                                                           870
   ZEP1=(XI1*BJHP1(KKI)-XI*BJHP1(KKI+2))/XI2
ZEP2=(XI1*BJHP2(KKI)-XI*BJHP2(KKI+2))/XI2
                                                                           871
                                                                           872
                                                                           873
   DELNP=BJHP1(JJI+1)*ZEP1-BJHP1(KKI+1)*ETAP1
   RATIO=FKP(J+1)/FKP(J)
                                                                           874
                                                                           875
   Z=RATIO*ETAP2
   SNP11=(ZEP1*BJHP2(JJI+1)-Z*BJHP1(KKI+1))/DELNP
                                                                           876
   SNP21=(Z*BJHP1(JJI+1)-ETAP1*BJHP2(JJI+1))/DELNP
                                                                           877
                                                                           878
   Z=RATIO*ZEP2
   SNP12=(ZEP1*BJHP2(KKI+1)-Z*BJHP1(KKI+1))/DELNP
                                                                           879
                                                                            880
   SNP22=(Z*BJHP1(JJI+1)-ETAP1*BJHP2(KKI+1))/DELNP
   DEL1=SNP11*SNP22-SNP12*SNP21
                                                                           881
                                                                            882
   Z=RATIO*ZEP1
   TNP11=(Z*BJHP2(JJI+1)-BJHP1(KKI+1)*ETAP2)/DELNP
                                                                            883
   TNP12=(Z*BJHP2(KKI+1)-BJHP1(KKI+1)*ZEP2)/DELNP
                                                                            884
                                                                            885
   Z=RATIO*ETAP1
                                                                            886
   TNP21=(BJHP1(JJI+1)*ETAP2-Z*BJKP2(JJI+1))/DELNP
   TNP22=(BJHP1(JJI+1)*ZEP2-Z*BJHP2(KKI+1))/DELNP
                                                                            887
                                                                            888
   DEL2=TNP11*TNP22-TNP12*TNP21
                                                                            889
   NN1=MM1+I
                                                                            890
   NN2=MM2+I
                                                                            891
   ANP(NN2)=(ANP(NN1)*SNP22-ALPNP(NN1)*SNP12)/DEL1
   BNP(NN2)=(BNP(NN1)*TNP22-BETNP(NN1)*TNP12)/DEL2
                                                                            892
                                                                            893
   ALPNP(NN2)=(-ANP(NN1)*SNP21+ALPNP(NN1)*SNP11)/DEL1
                                                                            894
40 BETNP(NN2)=(-BNP(NN1)*TNP21+BETNP(NN1)*TNP11)/DEL2
   JJ=JJ+2*NTER(J)
                                                                            895
                                                                            896
   KK=KK+NTER(J)
                                                                            897
   MM1=MM1+NMIN
                                                                            898
45 MM2=MM2+NMIN
                                                                            899
   RETURN
                                                                            900
   END
                                                                            901
                                                                            902
   SUBROUTINE EVEC(PD)
                                                                            903
                                                                            904
   IMPLICIT REAL*8 (A-H,0-Z)
         COMPUTES THE RADIAL, COLATITUDE, AND AZIMUTHAL
                                                                            905
                                                                            906
         COMPONENTS OF ELECTRIC FIELD VECTOR E FOR
                                                                            907
   REGION P AND SCALAR PRODUCT E.E*
   COMPLEX*16 FKP.ANP.BNP.ALPNP.BETNP.BJNP.BHNP.ERAD.ETHETA.EPHI.T.T1
                                                                            908
```

```
909
  1,C,W,X,Y,Z
   COMMON FKP(7), ANP(300), BNP(300), ALPNP(300), BETNP(300), BJNP(100), BH
                                                                            910
  1NP(100), BDP(6), P(51), DP(50), R, THETA, COSTH, PHI, SINTH, STOPR, EO
                                                                            911
                                                                            912
   COMMON /A/NORG, NREG, NRT, NSBF, NMIN, NC, ICODE
   DATA EPS/1.D-8/
                                                                            913
                                                                            914
   ERAD=DCMPLX(0.D0,0.D0)
   ETHETA=DCMPLX(0.D0,0.DC)
                                                                            915
                                                                            916
   EPHI=DCMPLX(0.D0,0.D0)
   NCK=0
                                                                            917
   NN=(NREG-1)*NMIN
                                                                            918
                                                                            919
   IF (THETA.EQ.O.DO) IR=1
                                                                            920
   ITP=0
                                                                            921
   DO 25 N=1,NC
                                                                            922
                                                                            923
   FAC1=2*N+1
   NNN=NN+N
                                                                            924
   W=BNP(NNN)
                                                                            925
   X=BJNP(N+1)
                                                                            926
                                                                            927
   Y=BETNP(NNN)
                                                                            928
   Z=BHNP(N+1)
   NCK≈NCK+1
                                                                            929
                                                                            930
   IF (IR.EQ.1) GO TO 5
   T=FAC1*P(N)*(W*X+Y*Z)
                                                                            931
                                                                            932
   CALL TERM(NCK,T,1)
                                                                            933
   ERAD=ERAD+T
                                                                            934
   IF (CDABS(T).LT.CDABS(ERAD)*EPS)IR=1
 5 IF (ITP.EQ.1) GO TO 20
                                                                            935
                                                                            936
   T=ANP(NNN)*X+ALPNP(NNN)*Z
                                                                            937
   CALL TERM(NCK,T,0)
                                                                            938
   NP1=N+1
                                                                            939
   RATIO=FAC1/(N*NP1)
                                                                            940
   A=NP1
                                                                            941
   B=N
                                                                            942
   T1=(\forall * (A*BJNP(N)-B*BJNP(N+2))+Y*(A*BHNP(N)-B*BHNP(N+2)))/FAC1
                                                                            943
   CALL TERM(NCK,T1,1)
                                                                            944
   IF (SINTH.GT.1.D-6) GO TO 10
                                                                            945
   A-FAC1/2.DO
   IF (THETA.GE.3.141591D0)A=A*(-1.D0)**MP1
                                                                            946
   GO TO 15
                                                                            947
10 A=RATIO*P(N)/SINTH
                                                                            948
15 = RATIO*DP(N)
                                                                            949
                                                                            950
   C*A*T+B*T1
                                                                            951
   ETHETA=ETHETA+C
   T=A*T1+B*1
                                                                            952
                                                                            953
   EPHI=EPHI+T
   IF (CDABS(C).LT.CDABS(ETHETA)*EPS.AND.CDABS(T).LT.CDABS(EPHI)*EPS)
                                                                            954
                                                                            955
  1ITP=1
                                                                            956
20 IF (IR+ITP.EQ.2) GO TO 35
25 IF (NCK.EQ.4)NCK=0
                                                                            957
   PRINT 30, NMIN, NC, STOPR, EPS
                                                                            958
30 FORMAT (15X, 'NMIN =', I3, 'NC =', I3, 'STOPR =', 1PD14.4, 'IS TOO SM
                                                                            959
  1ALL FOR ACCURACY OF ',D14.4)
                                                                            960
                                                                            961
35 ECOSPH=EO*DCOS(PHI)
   ERAD=-ECOSPH/(FKP(NREG)*R)*ERAD
                                                                            962
   ETHETA=ECOSPH*ETHETA
                                                                            963
                                                                            964
   EPHI=EO*DSIN(PHI)*EPHI
   PD=DREAL(ERAD*DCONJG(ERAD))+DREAL(ETHETA*DCONJG(ETHETA))+DREAL(EPH
```

```
966
  1I*DCONJG(EPHI))
                                                                           967
  RETURN
                                                                           968
   FND
                                                                           969
                                                                           970
   SUBROUTINE TERM(NCK,T,KEY)
                                                                           971
                                                                           972
   IMPLICIT REAL*8 (A-H,O-Z)
        COMPUTES I**NCK*(N-TH TERM IN SERIES)
                                                                           973
                                                                           974
   COMPLEX*16 T
   IF (KEY.EQ.1) GO TO 5
                                                                           975
                                                                           976
   GO TO (10,15,20,25),NCK
5 GO TO (15,20,25,10),NCK
                                                                           977
                                                                           978
10 T=DCMPLX(-DIMAG(T), DREAL(T))
   GO TO 25
                                                                           979
                                                                           980
15 T=-T
                                                                           981
   GO TO 25
                                                                           982
20 T=DCMPLX(DIMAG(T),-DREAL(T))
                                                                           983
25 RETURN
   END
                                                                           984
                                                                           985
                                                                           985
                                                                           987
   SUBROUTINE PL
                                                                           988
   IMPLICIT REAL*8 (A-H,O-Z)
        ASSOCIATED LEGENDRE FUNCTIONS OF THE FIRST
                                                                           989
                                                                           990
        KIND, DEGREE K AND ORDER 1 AND THEIR FIRST
                                                                           991
        DERIVATIVES
                                                                           992
   COMPLEX*16 FKP, ANP, BNP, ALPNP, BETNP, BJNP, BHNP
                                                                           993
   COMMON FKP(7), ANP(300), BNP(300), ALPNP(300), BETNP(300), BJNP(100), BH
  1NP(100), BDP(6), P(51), DP(50), R, THETA, COSTH, PHI, SINTH, STOPR, EO
                                                                           994
                                                                           995
   COMMON /A/NORG, NREG, NRT, NSBF, NMIN, NC, ICCDE
                                                                            996
   P(1)=SINTH
                                                                            997
   P(2)=3.DO*SINTH*COSTH
                                                                            998
   DP(1)=COSTH
                                                                           999
   DO 10 M=2.NC
                                                                           1000
   A=M
                                                                           1001
   MP1=M+1
                                                                           1002
   P(MP1)=(2.D0*A+1.D0)/A*COSTH*P(M)-(A+1.D0)/A*P(M-1)
                                                                          1003
   IF (SINTH.GT.1.D-6) GO TO 5
                                                                           1004
   DP(M)=M*MP1/2
   IF (THETA.GE.3.141591D0)DP(M)=(-1.D0)**M*DP(M)
                                                                           1005
                                                                           1006
   GO TO 10
 5 DP(M)=(A*COSTH*P(M)-(A+1.DO)*P(M-1))/SINTH
                                                                           1007
                                                                           1008
10 CONTINUE
                                                                           1009
   RETURN
                                                                           1010
   END
                                                                           1011
                                                                           1012
   FUNCTION ALP(N.M.X)
                                                                           1013
                                                                           1014
   IMPLICIT REAL*8 (A-H,0-Z)
          ASSOCIATED LEGENDRE FUNCTIONS OF THE FIRST KIND,
                                                                           1015
                                                                           1016
         DEGREE N AND ORDER M. N AND M GTE O. N GTE M
                                                                           1017
   FM=M
                                                                           1018
   IF (M.GT.0) GO TO 5
                                                                           1019
   P1=1.00
                                                                           1020
   GO TO 25
                                                                           1021
 5 IF (M.GT.1) GO TO 10
                                                                           1022
   SUM=2.DO
```

```
GO TO 20
                                                                            1023
10 J=2*M
                                                                            1024
   SUM=J
                                                                            1025
   IS=M-1
                                                                            1026
                                                                            1027
   DO 15 I=1.IS
15 SUM=SUM*(J-I)
                                                                            1028
20 P1=SUM*((1.D0-X*X)**(FM/2.D0))/(2.D0**M)
                                                                            1029
25 IF (N.NE.M) GO TO 30
                                                                            <sup>3</sup> 030
   ALP=P1
                                                                            1031
                                                                            1032
   GO TO 40
30 ALP=(2.D0*FM+1.DC)*X*P1
                                                                            1033
                                                                            1034
   IF (N.EQ.M+1) GO TO 40
                                                                            1035
   IS=N-M
   DO 35 I=2.IS
                                                                            1036
                                                                            1037
   P2=ALP
   C1=2*(M+I)-1
                                                                            1038
   ALP=(C1*X*P2-(C1-I)*P1)/I
                                                                            1039
                                                                            1040
35 P1=P2
40 RETURN
                                                                            1041
   END
                                                                            1042
                                                                            1043
                                                                            1044
                                                                            1045
   SUBROUTINE RFNDR (RSTART, STEP1, E, NRTS, M1, NITR)
   IMPLICIT REAL*8 (A-H,0-Z)
                                                                            1046
         ROOT FINDER
                                                                            1047
   COMMON /A/NORG, NREG, NRT, NSBF, NMIN, NC, ICODE
                                                                            1048
   COMMON /B/FACT(6,25,18),AJ(6,25,18),[(6,25,18),XLAMDA(25,18),SBDP 1049
                                                                            1050
  1(6),RHOP(6),CP(6),BP(6),TCP(6),H
                                                                            1051
   EXTERNAL FNCAL
   STEP=STEP1
                                                                            1052
   M = M1 - 3
                                                                            1053
                                                                            1054
   I=1
   SL=RSTART
                                                                            1055
 5 X=SL
                                                                            1056
                                                                            1057
   NRT=I
                                                                            1058
   W=FNCAL(X)
10 IF (W) 15,55,25
                                                                            1059
15 DO 20 J=1.M
                                                                            1060
   X=X+STEP
                                                                            1061
   V=FNCAL(X)
                                                                            1062
                                                                            1063
   IF (V) 20,55,50
20 W=V
                                                                            1064
   GO TO 35
                                                                            1065
25 DO 30 J=1.M
                                                                            1066
                                                                            1067
   X=X+STEP
   V=FNCAL(X)
                                                                            1068
   IF (V) 50,55,30
                                                                            1069
30 W=V
                                                                            1070
35 IF(M.GT.1000) GO TO 40
                                                                            1071
   M=M+1
                                                                            1072
   STEP=STEP*1.D1
                                                                            1073
   GO TO 10
                                                                            1074
40 PRINT 45,SL,X
                                                                            1075
45 FORMAT ('ORFNDR ERROR: NO ROOTS FROM', 1PE14.4, 'TO', E14.4)
                                                                            1076
   STOP
                                                                            1077
50 SL=X-STEP
                                                                            1078
   SR=X
                                                                            1079
```

	CALL DOTMINY C ENCAL CL CD II IV C NITTO	
5	CALL DRTMI(X,F,FNCAL,SL,SR,W,V,E,NITR) 5 XLAMDA(I,NSBF)=X	1080
•	SL=X+STEP	1081 1082
	IF(I+NSRF.EQ.2) STEP =DMAX1(X/10.D0,STEP)	1082
	IF (I.GT.1)STEP=(X-XLAMDA(I-1,NSBF))/10.DO	1084
	I=I+1	1085
	IF (I.LE.NRTS) GO TO 5 RETURN	1086
	END	1087
		1088
		1089 1090
	SUBROUTINE DRTMI(X,F,FCT,XLI,XRI,FLI,FRI,EPS,IEND)	1090
	IMPLICIT REAL*8 (A-H,O-Z)	1092
	BISECTION METHOD XL=XLI	1093
	XR=XRI	1094
	FL=FLI	1095
	FR=FRI	1096 1097
	I=0	1098
	TOLF=100.DO*EPS	1099
5	5 I=I+1 DO 30 K=1,IEND	1100
	X=.5DO*(XL+XR)	1101
	F=FCT(X)	1102 1103
	IF (F.EQ.O.DO) GO TO 45	1103
	IF (DSIGN(1.DO,F)+DSIGN(1.DO,FR).NE.O.DO) GO TO 10	1105
	TOL=XL XL=XR	1106
	XR=TOL	1107
	TOL=FL	1108
	FL=FR	1109 1110
	FR=TCL	1111
10) TOL=F-FL	1112
	A=F*TOL A=A+A	1113
	IF (A.GE.FR*(FR-FL)) GO TO 25	1114
	IF (I.GT.IEND) GO TO 25	1115 1116
	A=FR-F	1117
	DX=(X-XL)*FL*(1.D0+F*(A-TOL)/(A*(FR-FL)))/TOL	1118
	XM=X	1119
	FM=F X=XL-DX	1120
	F=FCT(X)	1121
	IF (F.EQ.0.D0) GO TO 45	1122 1123
	TOL=EPS	1124
	A=DABS(X)	1125
	IF (A.GT.1.DO)TOL=TOL*A IF (DABS(DX).GT.TOL) GO TO 15	1126
	IF (DABS(F).LE.TOLF) GO TO 45	1127
15	IF (DSIGN(1.D0,F)+DSIGN(1.D0,FL).NE.0.D0) GO TO 20	1128 1129
	XK=X	1130
	FR=F	1131
20	GO TO 5 XL=X	1132
۷.	FL=F	1133
	XR=XM	1134 1135
	FR=FM	1136

```
GO TO 5
                                                                           1137
25 XR=X
                                                                           1138
   FR=F
                                                                           1139
   TOL=EPS
                                                                           1140
   A=DABS(XR)
                                                                           1141
                                                                           1142
   IF (A.GT.1.DO)TOL=TOL*A
      (DABS(XL-XR).GT.TOL) GO TO 30
                                                                           1143
   IF (DABS(FR-FL).LE.TOLF) GO TO 40
                                                                           1144
30 CONTINUE
                                                                           1145
   PRINT 35, XL, XR
                                                                           1146
35 FORMAT ('ODRTMI ERROR: ROOT BETWEEN', 1PD15.7, 'AND', D15.7, 'MAY BE 1147
  1 INACCURATE')
                                                                           1148
40 IF (DABS(FR).LE.DABS(FL)) GO TO 45
                                                                           1149
   X=XL
                                                                           1150
   F=FL
                                                                           1151
45 RETURN
                                                                           1152
   END
                                                                           1153
                                                                           1154
                                                                           1155
   FUNCTION FNCAL (EIGV)
                                                                           1156
         FUNCTION EVALUATOR USED IN THE DETERMINATION
                                                                           1157
         OF THE EIGENVALUES LAMBDANK
                                                                           1158
   IMPLICIT REAL*8 (A-H,0-Z)
                                                                           1159
   COMMON /B/FACT(6,25,18), AJ(6,25,18), BY(6,25,18), XLAMDA(25,18), SBDP 1160
  1(6),RHOP(6),CP(6),BP(6),TCP(6),H
                                                                           1161
   COMMON /C/AJ1,S,F,R,I
                                                                           1162
   COMMON /A/NORG, NREG, NRT, NSBF, NMIN, NC, ICODE
                                                                           1163
   BY(1,NRT,NSBF) = 0.D0
                                                                           1164
   DO 35 I = 1, NORG
                                                                           1165
      =(EIGV*RHOP(I)*CP(I)-BP(I))/TCP(I)
                                                                           1166
   F=DSQRT(DABS(S))
                                                                           1167
   FACT(I,NRT,NSBF)=F
                                                                           1168
   IF (I.NE.1) GO TO 27
                                                                           1169
   IF (F.NE.O.DO) GO TO 5
                                                                           1170
   AJ(1,NRT,NSBF)=AJ1
                                                                           1171
   GO TO 30
                                                                           1172
 5 AJ(1,NRT,NSBF)=AJ1/F**(NSBF-1)
                                                                           1173
   IF (S.LT.0.D0) AJ(1,NRT,NSBF)=AJ(1,NRT,NSBF)/((-1)**((NSBF-1)/2))
                                                                          1174
   GO TO 30
                                                                           1175
27 R=SBDP(I-1)
                                                                           1176
   CALL SRBF (AM, BM, ATM, BTM)
                                                                           1177
   DELTA = AM*BTM-ATM*BM
                                                                           1178
   T1 = AJ(I-1,NRT,NSBF)*A + BY(I-1,NRT,NSBF)*BE
                                                                           1179
   T2 = AJ(I-1,NRT,NSBF)*AT + BY(I-1,NRT,NSBF)*BT
                                                                           1180
   AJ(I,NRT,NSBF) = (?1*BTM-T2*BM)/DELTA
                                                                           1181
   BY(I,NRT,NSBF) = (T2*AM-T1*ATM)/DELTA
                                                                           1182
30 R = SBDP(I)
                                                                           1183
35 CALL SRBF(A,BE,AT,BT)
                                                                           1184
   FNCAL=AJ (NORG, NRT, NSBF) *AT+BY (NORG, NRT, NSBF) *BT
                                                                           1185
  1 +H*(AJ(NORG, NRT, NSBF)*A+BY(NORG, NRT, NSBF)*BE)
                                                                           1186
   RETURN
                                                                           1187
   END
                                                                           1188
                                                                           1189
                                                                           1190
   SUBROUTINE BJYH(BJNP,BHNP,Z,N,STOPR,NBF)
                                                                           1191
   IMPLICIT COMPLEX*16(A-H,O-Z)
                                                                           1192
   DIMENSION BJNP(62), BHNP(62)
                                                                           1193
```

```
1194
   REAL*8 STOPR, X, XNPH, DREAL, DIMAG
   BJNP(1)=CDSIN(Z)/Z
                                                                          1195
   BJNP(2)=(BJNP(1)-CDCOS(Z))/Z
                                                                          1196
                                                                          1197
   ZTI=DCMPLX(-DIMAG(Z), DREAL(Z))
                                                                          1198
   T1=CDEXP(ZTī)/Z
                                                                          1199
   T1=DCMPLX(DIMAG(T1),-DREAL(T1))
                                                                          1200
   BHNP(1)=T1
   BHNP(2)=DCMPLX(DIMAG(T1),-DREAL(T1))*(1.DO-1.DO/ZTI)
                                                                          1201
                                                                          1202
   ZSQ=Z*2
                                                                          1203
   TCZ=2.DO/Z
   X=1.DO/STOPR
                                                                          1204
                                                                          1205
   DO 15 N=3.NBF
   XNPH=DFLOAT(N)-.5DO
                                                                          1206
                                                                          1207
   XNU=-(XNPH+1.DO)*TDZ
                                                                          1208
   A1=XNPH*TDZ
                                                                          1209
   DEN=XNU+1.DO/A1
                                                                          1210
   F=XNU/(DEN*A1)
                                                                          1211
   CF=-TDZ
                                                                          1212
   D0 5 I=2,200
                                                                          1213
   CF=-CF
                                                                          1214
   A1=CF*(XNPH+I)
                                                                          1215
   XNU=A1+1.DO/XNU
                                                                          1216
   DEN=A1+1.DO/DEN
   F1=XNU/DEN
                                                                          1217
   F=F*F1
                                                                          1218
   IF (DABS(CDABS(F1)-1.D0).LT.1.D-14) GO TO 10
                                                                          1219
 5 CONTINUE
                                                                          1220
10 BJNP(N)=F*BJNP(N-1)
                                                                          1221
                                                                          1222
   0=1.D0/(ZSO*BJNP(N-1))
   BHNP(N)=F*BHNP(N-1)-DCMPLX(-DIMAG(Q),DREAL(Q))
                                                                          1223
   IF (CDABS(BJNP(N)).LT.X.OR.CDABS(BHNP(N)).GT.STOPR) GO TO 20
                                                                          1224
                                                                          1225
15 CONTINUE
                                                                          1226
   N=N-1
20 IF (N.LT.5) PRINT 25,N,Z
                                                                          1227
25 FORMAT (25X, 'ONLY', I3, 'BESSEL FUNCTIONS FOR Z =', 1P2D12.4)
                                                                          1223
                                                                          1229
   END
                                                                          1230
                                                                          1231
                                                                          1232
   SUBROUTINE SRBF (A,Y,AD,YD)
                                                                          1233
         GET J, J', Y AND Y' FOR NEWTON'S COOLING FUNCTION AND RETURN 1234
         THE APPROPRIATE PART OF COMPLEX VALUES ADJUSTED FOR REAL
                                                                          1235
         VALUE CALCULATIONS
                                                                          1236
   IMPLICIT REAL*8 (A-H,0-Z)
                                                                          1237
                                                                          1238
   COMMOM /A/NORG, NREG, NRT, NSBF, NMIN, NC, ICODE
   COMMON /B/FACT(6,25,18),AJ(6,25,18),BY(6,25,18),XLAMDA(25,18),SBDP 1239
  1(6),RHOP(6),CP(6),BP(6),TCP(6),H
                                                                          1240
   COMMON /C/AJ1,S,F,R,I
                                                                          1241
                                                                          1242
   COMPLEX*16 BJ.YF.BJD.BYD
   COMMON /BES/BJ, YF, BJD, BYD, RJ, RY, RJD, RYD
                                                                          1243
   IF (S) 5,15,20
                                                                          1244
 5 CALL CSBFD (DCMPLX(0.DG,R*F))
                                                                          1245
                                                                          1246
         FOR S<0.
                                                                          1247
   IF (NSBF.EQ.2*(NSBF/2)) GO TO 10
                                                                          1248
         FOR SCO. AND EVEN ORDER BESSEL FUNCTIONS
                                                                           1249
   A=DREAL(BJ)
                                                                           1250
   Y=DIMAG(YF)
```

```
1251
   IF (ICODE.EQ.1) GO TO 25
                                                                          1252
   C=TCP(I)*F
                                                                          1253
   AD=-C*DIMAG(BJD)
   YD=C*DREAL (BYD)
                                                                          1254
   GO TO 25
                                                                           1255
         FOR SKO. AND ODD ORDER BESSEL FUNCTIONS
                                                                          1256
10 A=DIMAG(BJ)
                                                                           1257
   Y=DREAL (YF)
                                                                           1258
                                                                           1259
   IF (ICODE.EQ.1) GO TO 25
                                                                           1260
   C=TCP(I)*F
   AD=C*DREAL (BJD)
                                                                           1261
   YD=-C*DIMAG(BYD)
                                                                           1262
                                                                           1263
   GC TO 25
         FOR S=0.
                                                                           1264
15 A=R**(NSBF-1)
                                                                           1265
                                                                           1266
   Y=1.DO/R**(NSBF)
                                                                           1267
   IF (ICODE.EQ.1) GO TO 25
   AD=TCP(I)*(NSBF-1)*R**(NSBF-2)
                                                                           1268
   YD=-TCP(1)*(NSBF)/R**(NSBF+1)
                                                                           1269
   GO TO 25
                                                                           1270
         FOR S>O.
                                                                           1271
20 CALL SBFAD(R*F)
                                                                           1272
                                                                           1273
   A=RJ
                                                                           1274
   Y=RY
   IF (ICODE.EO.1) GO TO 25
                                                                           1275
                                                                           1276
   C=TCP(I)*F
                                                                           1277
   AD=C*RJD
                                                                           1278
   YD=C*RYD
25 RETURN
                                                                           1279
                                                                           1280
   END
                                                                           1281
                                                                           1282
   SUBROUTINE SBFAD(Z)
                                                                           1283
          SPHERICAL BESSEL FUNCTIONS OF THE FIRST
                                                                           1284
                                                                           1285
         AND SECOND KINDS AND THEIR FIRST DERIVATIVES
                                                                           1286
         FOR REAL ARSUMENT
   IMPLICIT REAL*8 (A-H,0-Z)
                                                                           1287
   COMMON /A/NORG, NREG, NRT, NSBF, NMIN, NC, ICODE
                                                                           1288
                                                                           1289
   COMPLEX*16 BJ.YF.BJD.BYD
   COMMON /BES/BJ,YF,BJD,BYD,RJ,RY,RJD,RYD
                                                                           1290
   COMMON /C/AJI,S,F,R,I
                                                                           1291
   SINZ = DSIN(Z)/Z
                                                                           1292
   COSZ = DCOS(Z)/Z
                                                                           1293
   Y1 = -COSZ
                                                                           1294
   RY = Y1/Z - SINZ
                                                                           1295
   IF(NSBF.GE.3) GO TO 12
                                                                           1296
                                                                           1297
   IF(NSBF.GT.1) GO TO 25
                                                                           1298
   RJ = SINZ
                                                                           1299
   RY=-COSZ
   IF (ICODE.EQ.1) GO TO 55
                                                                           1300
   RJD= COSZ - SINZ/Z
                                                                           1301
   RYD = SINZ + COSZ/Z
                                                                           1302
                                                                           1303
   GO TO 55
                                                                           1304
12 IF (I.EQ.1) GO TO 25
   00.15 M = 3,NS8F
                                                                           1305
                                                                           1306
   Y0=Y1
                                                                           1307
   YI=RY
```

```
IF (DABS(Y1).GT.1.D34) PRINT 500,NRT,M.NSBF,Z,Y1
                                                                              1308
     FORMAT ('SBFAD: ROOT', 13, 'FOR BF', 13, 'OF', 13, 'Z =', 1PD12.4, 1309
  1' Y = ', D12.4
                                                                              1310
                                                                              1311
15 \text{ RY} = (2*M-3)*Y1/Z - Y0
25 C = DABS(Z)
                                                                              1312
   IF(C.GE.3.DO) GO TO 30
                                                                              1313
                                                                              1314
   RJ = BES1(NSBF-1,Z)
                                                                              1315
   GO TO 35
30 \text{ RJ} = \text{SBFJ}(\text{NSBF-1,Z})
                                                                              1316
35 IF(ICODE.EO.1) GO TO 55
                                                                              1317
                                                                              1318
   IF (NSBF.GT.2) GO TO 40
                                                                              1319
   BJ1= SINZ
                                                                              1320
   GO TO 50
                                                                              1321
40 IF(C.GE.3.D0) GO TO 45
                                                                              1322
   BJI = BESI (NSBF-2,Z)
                                                                              1323
   GO TO 50
45 \text{ BJ1} = \text{SBFJ (NSBF-2,Z)}
                                                                              1324
50 \text{ RJD} = \text{BJ1} - \text{NSBF*RJ/Z}
                                                                              1325
                                                                              1326
   RYD = Y1 - NSBF*RY/Z
                                                                              1327
55 RETURN
                                                                              1328
   END
                                                                              1329
                                                                              1330
                                                                              1331
   FUNCTION BES1(N,Z)
   IMPLICIT REAL*8 (A-H,0-Z)
                                                                              1332
   BES1=DSIN(Z)/Z
                                                                              1333
   IF (N.EQ.O) GO TO 15
                                                                              1334
                                                                              1335
   TDZ=2.DO/Z
                                                                              1336
   I1=0
                                                                              1337
   DO 10 M=1,N
                                                                              1338
   XNUPH=DFLOAT(M)+.5D0
                                                                              1339
   AO=XNUPH*TDZ
                                                                              1340
   A1=-(XNUPH+1.D0)*TDZ
                                                                              1341
   RNUM=A1+1.DO/A0
                                                                              1342
   RDEN=A1
   COLD=AO*RNUM/RDEN
                                                                              1343
                                                                              1344
   CFAC=-TDZ
                                                                              1345
   D0 5 I=2,200
                                                                              1346
   CFAC=-CFAC
   A=CFAC*(XNUPH+I)
                                                                              1347
                                                                              1348
   RNUM=A+1.DO/RNUM
                                                                              1349
   RDEN=A+1.DO/RDEN
                                                                              1350
   C=RNUM/RDEN
   COLD=COLD*C
                                                                              1351
   IF (DABS(DABS(C)-1.D0).LT.1.D-8) GO TO 10
                                                                              1352
                                                                              1353
 5 CONTINUE
                                                                              1354
10 BES1=BES1/COLD
15 RETURN
                                                                              1355
                                                                              1356
   END
                                                                              1357
                                                                              1358
                                                                              1359
   FUNCTION SBFJ(N,Z)
                                                                               1360
    IMPLICIT REAL*8 (A-H,0-Z)
                                                                              1361
   0 = 0.00
                                                                               1362
   P=1.00
    IF (N.EQ.O) GO TO 10
                                                                               1363
    XN1=N+1
                                                                               1364
```

	XN2=N	1365
	F=1.D0	1366
	Z2=2.D0*Z	1367
c	T=1.00	1368
Э	T=T*((XN1*XN2)/(F*Z2)) Q=Q+T	1369 1370
	IF (XN2.EQ.1.D0) GO TO 10	1370
	XN1=XN1+1.D0	1371
	XN2=XN2-1.D0	1372
	F=F+1.D0	1374
	T=-T*((XN1*XN2)/(F*Z2))	1375
	P=P+T	1376
	IF (XN2.EQ.1.D0) GO TO 10	1377
	XN1=XN1+1.D0	1378
	XN2=XN2-1.D0	1379
	F=F+1.D0	1380
• •	GO TO 5	1381
10	A=Z-N*1.5707963267948965D0	1382
	SBFJ=(P*DSIN(A)+Q*DCOS(A))/Z	1383
	RETURN END	1384 1385
	END	1386
		1387
	SUBROUTINE CSBFD(Z)	1388
	IMPLICIT COMPLEX*16 (A-H,0-Z)	1389
	COMMON /BES/BJ,YF,BJD,BYD	1390
	COMMON /A/NORG, NREG, NRT, NSBF, NMIN, NC, ICODE	1391
	COMMON /C/AJ1,S,F,R,I	1392
	REAL*8 C,AJ1,S,F,R	1393
	C = CDABS(Z)	1394
	SINZ = CDSIN(Z)/Z $COSZ = CDCOS(Z)/Z$	1395
	COSZ = CDCOS(Z)/Z $Y1 = -COSZ$	1396 1397
	YF = Y1/Z - SINZ	1398
	IF(NSBF.GE.3) GO TO 12	1399
	IF(NSBF.GT.1) GO TO 25	1400
	BJ = SINZ	1401
	YF=-COSZ	1402
	IF(ICODE.EQ.1) GO TO 55	1403
	BJD= COSZ - SINZ/Z	1404
	BYD = SINZ + COSZ/Z	1405
12	GO TO 55 IF (I.EQ.1) GO TO 25	1406
12	DO 15 M = 3,NSBF	1407 1408
	Y0=Y1	1409
	Y1=YF	1410
15	YF = (2*M-3)*Y1/Z - Y0	1411
	IF (C.GE.15.DO) GO TO 30	1412
	BJ = BES1C(NSBF-1,Z)	1413
~~	G0 T0 35	1414
	BJ = SBFJC(NSBF-1,Z)	1415
33	IF(ICODE.EQ.1) GO TO 55	1416
	1F(NSBF.GT.2) GO TO 40 BJ1= SINZ	1417
	GO TO 50	1418 1419
40	IF(C.GE.15.DO) GO TO 45	1420
-	BJ1 = BES1C(NSBF-2,Z)	1421
	•	

	GO TO 50	1422
45	BJ1 = SBFJC(NSBF-2, Z)	1423
	BJD = BJ1 - NSBF*BJ/Z	
50		1424
	BYD = Y1 - NSBF*YF/Z	1425
55	RETURN	1426
	END	1427
		1428
		1429
	FUNCTION BESIC(N,Z)	1430
	IMPLICIT COMPLEX*16 (A-H,O-Z)	1431
	BESIC = CDSIN(Z)/Z	1432
	IF(N.EQ.0) GO TO 15	1433
	BESIC=(BESIC-CDCOS(Z))/Z	1434
	IF (N.EQ.1) GO TO 15	1435
	TDZ = 2.DO/Z	1436
	DO 10 M = 2,N	1437
	CM = DCMPLX (DFLOAT(M), 0.DO)	1438
	XNUPH = CM + .5DO	1439
	AO = XNUPH*TDZ	1440
	A1 = -(XNUPH + 1.D0)*TDZ	1441
	RNUM = A1 + 1.DO/AO	1442
	RDEN = A1	
		1443
	COLD = AO*RNUM/RDEN	1444
	CFAC = -TDZ	1445
	D0 5 I = 2,200	1446
	CI = DCMPLX(DFLOAT(I),0.D0)	1447
	CFAC = -CFAC	
		1448
	A = CFAC*(XNUPH + CI)	1449
	RNUM = A + 1.DO/RNUM	1450
	RDEN = A + 1.DO/RDEN	1451
	C = RNUM/RDEN	1452
	COLD = COLD*C	
		1453
_	IF(DABS(CDABS(C)-1.D0).LT.1.D-8) GO TO 10	1454
5	CONTINUE	1455
10	BESIC = BESIC/COLD	1456
	RETURN	1457
	END	1458
	CHO	
		1459
		1460
	FUNCTION SBFJC(N,Z)	1461
	IMPLICIT COMPLEX*16 (A-H,O-Z)	1462
	REAL*8 XN1, XN2, F, DREAL, DIMAG	1463
	0=0.00	1464
	P=1.D0	1465
	IF (N.EQ.O) GO TO 10	1466
	XN1=N+1	1467
	XN2=N	1468
	F=1.D0	1469
	Z2=2.D0*Z	
		1470
_	T=1.D0	1471
5	T=T*((XN1*XN2)/(F*72))	1472
	Q=Q+T	1473
	IF (XN2.EQ.1.DO) GO TO 10	1474
	XN1=XN1+1.D0	1475
	XN2=XN2-1.D0	1476
	F=F+1.D0	1477
	T=-T*((XN1*XN2)/(F*Z2))	1478

```
1479
  P=P+T
   IF (XN2.EQ.1.D0) GO TO 10
                                                                        1480
                                                                        1481
   XN1=XN1+1.D0
                                                                        1482
   XN2=XN2-1.DO
                                                                        1483
  F=F+1.D0
                                                                        1484
   GO TO 5
10 A = 7 - DCMPLX(DFLOAT(N)*1.5707963267948965D0.0.D0)
                                                                        1485
   T = (P*CDSIN(A)+Q*CDCOS(A))/Z
                                                                        1486
                                                                        1487
   IF (DREAL(Z).EQ.O.DO) GO TO 17
   SBFJC=T
                                                                        1488
                                                                        1489
   GO TO 20
17 IF (N.NE.2*(N/2)) GO TO 15
                                                                        1490
                                                                        1491
   SBFJC=DCMPLX(DREAL(T),0.D0)
                                                                        1492
   GO TO 20
15 SBFJC=DCMPLX(0.DO.DIMAG(T))
                                                                        1493
                                                                        1494
20 RETURN
                                                                        1495
   END
                                                                        1496
                                                                        1497
                                                                        1498
   SUBROUTINE EPROP(F .ITIS.EPS.SIG)
   IMPLICIT REAL*8 (A-H,0-Z)
                                                                        1499
                                                                        1500
         INTERPOLATE EPS AND SIGMA FROM TABLES
                FREQUENCY IN MEGAHERTZ
                                                                        1501
                TISSUE TYPE
                                                                        1502
         ITIS
           1 DENOTES CEREBROSPINAL FLUID
                                                                        1503
                                                                        1504
           2 DENOTES BLOOD
                                                                        1505
           3 DENOTES MUSCLE
           4 DENOTES SKIN OR DURA
                                                                        1506
                                                                        1507
           5 DENOTES BRAIN
           6 DENOTES FAT OR BONE
                                                                        1508
                                                                        1509
           7 DENOTES YELLOW BONE MARROW
                REAL PART OF DIELECTRIC CONSTANT
         EPS
                                                                        1510
                CONDUCTIVITY
                                                                        1511
         SIG
   DIMENSION FR(32), EA(32,7), SA(32,7), SA1(128), SA5(96), EA1(128), EA5(9 1512
                                                                        1513
  16)
   EQUIVALENCE (SA1,SA),(SA5,SA(1,5)),(EA1,EA),(EA5,EA(1,5))
                                                                        1514
   DATA FR/0.108,.125908,.158508,.199508,.251208,.316208,.398108,.501 1515
  12D8..631D8..7943D8..1D9..1259D9..1585D9..1995D9..2512D9..3162D9.,3 1516
  1981D9,.5012D9,.631D9,.7943D9,.1D10,.1259D10,.1585D10,.1995D10,.251 1517
  12D10,.3162D10,.3981D10,.5012D10,.631D10,.7943D10,.8913D10,.1D11/
   DATA SA1/.75D0,.762D0,.78D0,.798D0,.816D0,.84D0,.876D0,.9D0,.96D0, 1519
  1.102D1,.114D1,.1224D1,.1308D1,.1392D1,.1452D1,.1524D1,.1572D1,.160 1520
  18D1,.1644D1,.174D1,.1812D1,.1932D1,.2064D1,.2292D1,.2616D1,.3084D1 1521
  1,.3744D1,.4716D1,.642D1,.918D1,.1076D2,.1236D2,.6875D0,.6985D0,.71 1522
  15D0,.7315D0,.748D0,.77D0,.803D0,.825D0,.88D0,.935D0,.1045D1,.1122D 1523
  11,.1199D1,.1276D1,.1331D1,.1397D1,.1441D1,.1474D1,.1507D1,.1595D1, 1524
  1.1661D1,.1771D1,.1892D1,.2101D1,.2398D1,.2827D1,.3432D1,.4323D1,.5 1525
  1885N1, .8415D1, .9867D1, .1133D2, .625N0, .635DG, .65D0, .665D0, .68N0, .7N 1526
  10..73D0..75D0..8D0..85D0..95D0..102D1..109D1..116D1..121D1..127D1, 1527
  1.13101,.13401,.13701,.14501,.15101,.16101,.17201,.19101,.21801,.25 1528
  17D1,.312D1,.393D1,.535D1,.765D1,.897D1,.103D2,.5313D0,.5393D0,0.55 1529
  12500,.565300,0.57800,.59500,.620500,.637500,.6800,.722500,.807500, 1530
  1.867D0,.9265D0,.986D0,.1029D1,.108D1,.1114D1,.1139D1,.1165D1,.1233 1531
  101..1284D1..1369D1..1462D1..1624D1..1853D1..2185D1..2652D1..3341D1 1532
  1,.4548D1,.6503D1,.7625D1,.8755D1/
   DATA SA5/.4116D0,.4181D0,0.4280D0,.4379D0,.4478D0,.461D0,.4807D0,. 1534
  14939D0..5268D0..5597D0..6256D0..6717D0..7178D0..7639D0..7968D0..83 1535
```

```
163D0..8626D0,.8324D0,.9021D0,.9548D0,.9943D0,.106D1,.1133D1,.1258D 1536
 11,.1436D1,.1692D1,.2055D1,.2598D1,.3523D1,.5038D1,.5907D1,.6783D1, 1537
 1.22D-1,.228D-1,.235D-1,.25D-1,.26D-1,.28D-1,.32D-1,.348D-1,.38D-1, 1538
 1.4D-1,.4.5D-1,.47D-1,.52D-1,.57D-1,.628D-1,.69D-1,.74D-1,.81D-1,.8 1539
 18D-1,.96D-1,.103D0,.113D0,.124D0,.138D0,.154D0,.176D0,.201D0,.236D 1540
 10,.274D0,.342D0,.384D0,.4365D0,.198D-1,.2052D-1,.2115D-1,.225D-1,. 1541
 1234D-1,.252D-1,.288D-1,.3132D-1,.342D-1,.36D-1,.3825D-1,.423D-1,.4 1542
 168D-1,.513D-1,.5652D-1,.621D-1,.666D-1,.729D-1,.792D-1,.864D-1,.92 1543
 17D-1,.1017D0,.1116D0,.1242D0,.1386D0,.1584D0,.1809D0,.2124D0,.2466 1544
 1D0,.3078D0,.3456D0,.3929D0/
  DATA EA1/.192D3,.1782D3,.165D3,.1517D3,.1393D3,.1277D3,.1171D3,.10 1546
 172D3,.9876D2,.9144D2,.8412D2,.7716D2,.7116D2,.6744D2,.6588D2,.648D 1547
 12,.6396D2,.6324D2,.624D2,.6156D2,.6072D2,.5976D2,.5868D2,.576D2,.5 1548
 1652D2,.5532D2,.5412D2,.5268D2,.5136D2,.498D2,.4896D2,.4788D2,.192D 1549
 13,.1782D3,.165D3,.1517D3,.1393D3,.1277D3,.1171D3,.1072D3,.9876D2,. 1550
 19144D2,.8412D2,.7716D2,.7116D2,.6744D2,.6588D2,.648D2,.6396D2,.632 1551
 14D2,.624D2,.6156D2,.6072D2,.5976D2,.5868D2,.576D2,.5652D2,.5532D2, 1552
 1.5412D2,.5268D2,.5136D2,.498D2,.4896D2,.4788D2,.16D3,.1485D3,.1375 1553
 1D3,.1264D3,.1161D3,.1064D3,.976D2,.893D2,.823D2,.762D2,.701D2,.643 1554
 1D2..593D2..562D2..549D2..54D2..533D2..527D2..52D2..513D2..506D2..4 1555
 198D2,.489D2,.48D2,.471D2,.461D2,.451D2,.439D2,.428D2,.415D2,.408D2 1556
 1,.399D2,.1424D3,.1322D3,.1224D3,.1125D3,.1033D3,.947D2,.8686D2,.79 1557
 148D2,.7325D2,.6782D2,.6239D2,.5"23D2,.5278D2,.5002D2,.4886D2,.4806 1558
 1D2, 4744D2, 469D2, 4628D2, 4566D2, 4503D2, 4432D2, 0.4352D2, 4272D2 1559
 1..4192D2..4103D2..4014D2..3907D2..3809D2..3694D2..3631D2..3551D2/ 1560
  DATA EA5/.1054D3,.9779D2,.9054D2,.8323D2,0.7645D2,.7006D2,.6427D2, 1561
 1.588D2,.5419D2,.5018D2,0.4616D2,.4234D2,.3905D2,.3701D2,.3615D2,.3 1562
 1556D2,.351D2,.3470D2,.3424D2,.3378D2,.3332D2,.3279D2,.322D2,.3161D 1563
 12,.3102D2,.3036D2,.297D2,.2891D2,.2818D2,.2733D2,.2687D2,.2627D2,. 1564
 136D2,.318D2,.279D2,.243D2,0.208D2,.178D2,.148D2,.123D2,.10°D2,.86D 1565
 11,.745D1,.68D1,.63D1,.6D1,.58D1,.57D1,.565D1,.563D1,.562D1 561D1, 1566
 1.56D1,.559D1,.557D1,.556D1,.554D1,.552D1,.55D1,.548D1,.52D1,.49D1, 1567
 1.473D1,.45D1,.324D2,.2862D2,.2511D2,.2187D2,.1872D2,.160272,.1332D 1568
 12..1107D2..918D1,.774D1,.6705D1,.612D1,.567D1,.54D1,.522D1,.513D1, 1569
  1.5085D1,.5067D1,.5058D1,.5049D1,.504D1,.5031D1,.5013D1,.5004D1,.49 1570
  186D1,.4968D1,.495D1,.4932D1,.468D1,.441D1,.4257D1,.405D1/
                                                                       1571
  FREQ=F *1.D6
                                                                       1572
  NDX=ITIS
                                                                       1573
   IF (FREQ.GE.FR(1).AND.FREQ.LE.FR(32)) GO TO 10
                                                                       1574
                                                                       1575
 5 FORMAT ('O**** FREQUENCY LIES OUTSIDE THE RANGE 10 - 10000 MHZ *** 1576
                                                                       1577
  1*')
   STOP
                                                                       1578
                                                                       1579
10 DO 15 IJ=1.31
   IF (FREQ.LE.FR(IJ+1)) GO TO 20
                                                                       1580
                                                                       1581
15 CONTINUE
20 X=(FREQ-FR(IJ))/(FR(IJ+1)-FR(IJ))
                                                                       1582
   EPS=EA(IJ,NDX)+(EA(IJ+1,NDX)-EA(IJ,NDX))*X
                                                                       1583
                                                                       1584
   SIG=SA(IJ,NDX)+(SA(IJ+1,NDX)-SA(IJ,NDX))*X
                                                                       1585
  RETURN
                                                                       1586
  END
                                                                       1587
                                                                       1588
   SUBROUTINE PLTCV1(X,Y,XLEN,YLEN,XTL,YTL,NXTL,NYTL,NP,ICRCT,ISYM,
                                                                       1589
                                                                       1590
    IMM, XMIN, XMAX, YMIN, YMAX, INPLT, LINTYP, SOCH, DELX, DELY,
                                                                       1591
    NDEC)
   WE ARE PLOTTING Y AS A FUNCTION OF X
                                                                       1592
```

```
**** THIS IS A VARIATION OF PLTCRV TO PERMIT SPECIFYING THE BLIP
                                                                         1593
     INTERVAL AND THE NUMBER OF DECIMAL PLACES AND CHARACTER SIZE FOR
                                                                         1594
     SCALE NUMBERS AND LABELS.
                                                                         1595
              ARRAY TO PLOT ON X (HORIZONTAL) AXIS - DIMENSION (NP+2)
                                                                         1596
              ARRAY TO PLOT ON Y (VERTICAL) AXIS - DIMENSION (NP+2)
                                                                         1597
              LENGTH IN INCHES OF X AXIS
       XLEN
                                                                         1598
       YLEN
              LENGTH IN INCHES OF Y AXIS
                                                                         1599
       XTTL
              ARRAY CONTAINING X AXIS TITLE
                                                                         1600
       YTTL
              ARRAY CONTAINING Y AXIS TITLE
                                                                         1601
       NX
              NUMBER OF CHARACTERS IN XTTL
                                                                         1602
       NY
              NUMBER OF CHARACTERS IN YTTL
                                                                         1603
       NP
              NUMBER OF POINTS TO PLOT IN ARRAYS X AND Y
                                                                         1604
              0 - PLOT AXES AND LINE PLOT
       ICRCT
                                                                         1605
              1 - PLO; LINE ON EXISTING AXES
                                                                         1606
              CODE (0-13) TO SELECT SYMBOL TO MARK PLOTTED POINTS
       ISYM
                                                                         1607
       IMM
              0 - GET SCALE END VALUES BY SCANNING X AND Y ARRAYS
                                                                         1608
              1 - GET SCALE END VALUES FROM INPUT ARGUMENTS
                                                                         1609
       XMIN
              MINIMUM VALUE ON X AXIS
                                                                         1610
       XMAX
              MAXIMUM VALUE ON X AXIS
                                                                         1611
       YMIN
              MINIMUM VALUE ON Y AXIS
                                                                         1612
       YMAX
              MAXIMUM VALUE ON Y AXIS
                                                                         1613
       INPLT
              O - DRAW SCALES AND LINE
                                                                         1614
              1 - GET MAXIMA AND MINIMA OF X AND Y ARRAYS, NO PLOT
                                                                         1615
      LINTYP MAGNITUDE GIVES FREQUENCY OF SYMBOLS - EVERY LINTYP PTS. 1616
              =0 - LINE PLOT, NO SYMBOLS
                                                                         1617
              >0 - LINE PLOT WITH SYMBOLS
                                                                         1618
              <0 - NO LINE, SYMBOLS ONLY</p>
                                                                         1619
              CHARACTER HEIGHT FOR TITLE AND SCALE (INCHES)
       SOCH
                                                                         1620
              FOR X AXIS, POSITIVE VALUE TO DEFINE UNITS BETWEEN TIC
      DELX
                                                                         1621
                MARKS (USER UNITS). IF DELX = 0., TIC MARKS WILL BE
                                                                         1622
                ONE INCH APART.
                                                                         1623
      DELY
              FOR Y AXIS, POSITIVE VALUE TO DEFINE UNITS BETWEEN TIC
                                                                         1624
                MARKS (USER UNITS).
                                     IF DELY = 0., TIC MARKS WILL BE
                                                                         1625
                ONE INCH APART.
                                                                         1626
      NDEC
              NUMBER OF DECIMAL PLACES IN SCALE NUMBERS
                                                                         1627
                >=0 - SPECIFIES NUMBER OF DECIMAL PLACES AFTER
                                                                         1628
                      DECIMAL POINT
                                                                         1629
                    - ROUNDED INTEGER DRAWN
                                                                         1630
   DIMENSION X(NP), Y(NP), XTL(1), YTL(1)
                                                                         1631
   IF(ICRCT.EQ.1) GO TO 20
                                                                         1632
   IF(IMM.EQ.1) GO TO 10
                                                                         1633
   XMIN = 1.E35
                                                                         1634
   XMAX = -1.E35
                                                                         1635
   YMIN =
           1.E35
                                                                         1636
   YMAX = -1.E35
                                                                         1637
       5 I = 1,NP
                                                                         1638
   XMIN=AMIN1(X(I),XMIN)
                                                                         1639
   YMIN=AMIN1(Y(I), YMIN)
                                                                         1640
   XMAX=AMAX1(X(I),XMAX)
                                                                         1641
 5 YMAX=AMAX1(Y(I),YMAX)
                                                                         1642
   IF (INPLT.EQ.1) RETURN
                                                                         1643
10 DELVX = (XMAX-XMIN)/XLEN
                                                                         1644
   DELVY = (YMAX-YMIN)/YLEN
                                                                         1645
   CALL BAXIS (0.,0.,XTL,-NXTL,XLEN,0.,XMIN,DELVX,DELX,SOCH,NDEC)
                                                                         1646
   CALL BAXIS (0.,0.,YTL,NYTL,YLEN,90.,YMIN,DELVY,DELY,SOCH,NDEC)
                                                                         1647
20 IF(ISYM.LT.O.OR.ISYM.GT.13) ISYM = 1
                                                                         1648
                                                                         1649
   X(NP+1) = XMIN
```

```
1650
  Y(NP+1) = YMIN
                                                                        1651
  X(NP+2) = (XMAX-XMIN)/XLEN
  Y(NP+2) = (YMAX-YMIN)/YLEN
                                                                        1652
                                                                        1653
  CALL LINE(X.Y.NP.1.LINTYP.ISYM)
                                                                        1654
  RETURN
  END
                                                                         1655
                                                                         1656
                                                                         1657
  SUBROUTINE BAXIS (XPAGE, YPAGE, IBCD, NCHAR, AXLEN, ANGLE, FIRSTV, DELTAV 1658
 1,DELTIC,SOCH,NDEC)
                                                                         1659
      THIS SUBROUTINE IS AN EXTENSION OF THE CALCOMP 'AXIS' ROUTINE
                                                                        1660
      TO ALLOW THE USER TO SPECIFY THE SIZE OF CHARACTERS. THE
                                                                         1661
      DISTANCE BETWEEN TIC MARKS AND THE NUMBER OF DECIMAL PLACES IN
                                                                        1662
      THE SCALE NUMBERS.
                                                                         1663
                - X COORDINATE OF AXIS STARTING POINT (INCHES)
                                                                         1664
         XPAGE
                - Y COORDINATE OF AXIS STARTING POINT (INCHES)
                                                                         1665
         YPAGE
                - ARRAY WITH AXIS TITLE
                                                                         1666
         IBCD
               - NUMBER OF CHARACTERS IN AXIS TITLE
                                                                         1667
         NCHAR
                     <0 - ALL NOTATION ON CLOCKWISE SIDE OF AXIS</p>
                                                                         1668
                    >0 - ALL NOTATION ON COUNTERCLOCKWISE SIDE
                                                                         1669
                                                                         1670
                - AXIS LENGTH (INCHES) (MUST BE POSITIVE)
         AXLEN
                - ANGLE (POSITIVE OR NEGATIVE) AT WHICH AXIS IS DRAWN 1671
         ANGLE
                                                                         1672
                     (DEGREES)
         FIRSTY - STARTING VALUE (MAX OR MIN) OF AXIS AT FIRST TIC
                                                                         1673
                     (USER UNITS)
                                                                         1674
         DELTAY - INCREMENT OR DECREMENT VALUE ASSOCIATED WITH ONE
                                                                         1675
                                                                         1676
                     INCH ON AXIS (USER UNITS)
         DELTIC - POSITIVE VALUE TO DEFINE UNITS BETWEEN TIC MARKS
                                                                         1677
                     (USER UNITS) IF DELTIC = 0., TIC MARKS WILL BE
                                                                         1678
                    ONE INCH APART.
                                                                         1679
                                                                         1680
         SOCH
                - CHARACTER HEIGHT FOR TITLE AND SCALE (INCHES)
         NDEC
                - NUMBER OF DECIMAL PLACES IN SCALE NUMBERS
                                                                         1681
                     >=0 - SPECIFIES NUMBER OF DECIMAL PLACES AFTER
                                                                         1682
                           DECIMAL POINT
                                                                         1683
                                                                         1684
                     -1 - ROUNDED INTEGER DRAWN
                                                                         1685
  DIMENSION IBCD(1)
   IF (AXLEN.GT.O..AND.DELTIC.GE.O..AND.NDEC.LE.9) GO TO 10
                                                                         1686
   PRINT 5, AXLEN, DELTIC, NDEC
                                                                         1687
 5 FORMAT ('0**** BAXIS ERROR: AXLEN =',1PD15.7,' DELTIC =',D15.7,' 1688
      NDEC =', 15.' ****!)
                                                                         1689
                                                                         1690
   STOP
10 IF (NDEC.LT.-1)NDEC=-1
                                                                         1691
                                                                         1692
   AIR=3.1415927*ANGLE/180.
                                                                         1693
   CA=COS(AIR)
                                                                         1694
   SA=SIN(AIR)
         DRAW AXIS LINE
                                                                         1695
   CALL PLOT(XPAGE, YPAGE, 3)
                                                                         1696
   CALL PLOT(XPAGE+AXLEN*CA, YPAGE+AXLEN*SA, 2)
                                                                         1697
                                                                         1698
   FSTV=FIRSTV
   DELV=DELTAV
                                                                         1699
                                                                         1700
   A=AMAX1(ABS(FSTV),ABS(FSTV+DELV*AXLEN))
                                                                         1701
   M=ALOG10(A)
   IF (A.LT..1)M=M-1
                                                                         1702
   TM=10.**M
                                                                         1703
   DTIC=ABS(DELTIC/DELV)
                                                                         1704
                                                                         1705
   IF (DELTIC.EQ.0)DTIC=1.0
                                                                         1706
   DELV=DELV/TM
```

	FSTV=FSTV/TM	1707
	X1=SOCH/2.	1708
		1709
	TICH=X1	
	IF (NCHAR.LT.O)TICH=-TICH	1710
	XT=-TICH*SA	1711
	YT=TICH*CA	1712
	COMPUTE POSITION OF AXIS SCALE NUMBERS RELATIVE TO TIC	1713
	MARKS AND ADJUST FOR NUMBER OF DECIMAL POINTS	1714
		1715
	FN=X1	
	IF (NDEC.GE.O)FN=FN*(2+NDEC)	1716
	FN=FN429*X1	1717
	XN=1.4*XT-FN*CA	1718
	YN=1.4*YT-FN*SA	1719
	IF (NCHAR.GT.O) GO TO 20	1720
	FOR TICS ON CLOCKWISE SIDE OF AXIS, NUMBERS MUST BE MOVED	1721
		1722
	AWAY FROM AXIS BY ONE CHARACTER WIDTH	
	XN=XN+2.*XT	1723
	YN=YN+2.*YT	1724
20	XTIC=XPAGE	1725
	YTIC=YPAGE	1705
	DX=DTIC*CA	1727
	DY=DTIC*SA	1728
		729
	FPN=FSTV	
	DTIC=DTIC*DELV	1730
	X=.571*SOCH-FN	1731
	IL=0	1732
	LOOP TO DRAW TICS AND SCALE NUMBERS	1733
25	CALL PLOT(XTIC, YTIC, 3)	1734
	CALL PLOT(XTIC+XT, YTIC+YT, 2)	1735
	IF (IL.EQ.O.AND.NDEC.GE.O) GO TO 30	1736
		1737
	X=0.	
	IF (FPN.LT.O.)X=X1	1738
30	CALL NUMBER(XTIC+XN-X*CA,YTIC+YN-X*SA,SOCH,FPN,ANGLE,NDEC)	1739
	XTIC=XTIC+DX	1740
	YTIC=YTIC+DY	1741
	FPN=FPN+DTIC	1742
	ALEN=(XTIC-XPAGE-DX*.5)/CA	1743
		1744
	IF (ALEN.GT.AXLEN) GO TO 45	
	IL=IL+1	1745
	IF (IL.LE.100) GO TO 25	1746
	PRINT 40	1747
40	FORMAT ('0**** BAXIS ERROR: MORE THAN 100 TIC MARKS ****')	1748
	STOP	1749
	CENTER AXIS TITLE AND PLOT IT	1750
AR	IL=IABS(NCHAR)	1751
43		1752
	IF (M.NE.O) IL=IL+4	
	X=IL*SOCH	1753
	HTL=(AXLEN-X)/2.	1754
	XN=XPAGE+4.6*XT+HTL*CA	1755
	YN=YPAGE+4.6*YT+HTL*SA	1756
	IF (NCHAR.GT.0) GO TO 50	1757
	LEAVE ROOM FOR TITLE CHARACTERS ON CLOCKWISE SIDE OF AXIS	1758
	XN=XN+2.*XT	1759
		1760
	YN=YN+2.*YT	
50	CALL SYMBOL(XN, YN, SOCH, IBCD, ANGLE, IABS(NCHAR))	1761
	IF (M.EQ.0) GO TO 55	1762
	ADD SCALE FACTOR	1763

```
CALL SYMBOL(999.,999.,SOCH, ' *10'.ANGLE.4)
                                                                         1764
                                                                         1765
   XN=XN+X*CA-X1*SA
   YN=YN+X*SA+1.5*X1*CA
                                                                         1766
                                                                         1767
   CALL NUMBER(XN, YN, X1, FLOAT(M), ANGLE, -1)
55 RETURN
                                                                         1768
                                                                         1769
   END
                                                                         1770
                                                                         1771
   SUBROUTINE CNTRP1(X,NROW,Y,NCOL,D,NLEV1,NSYM1,IFL)
                                                                         1772
                                                                         1773
   DIMENSION X(NROW), Y(NCOL), D(NROW, NCOL), FLEV(10), XST(60), YST(60)
   INTEGER*2 IFL(NROW, NCOL), IST(60), JST(60)
                                                                         1774
   NLEV=NLEV1
                                                                         1775
                                                                         1776
   IF (NLEV.LT.1)NLEV=1
   IF (NLEV.GT.10)NLEV=10
                                                                         1777
                                                                         1778
   NSYM=NSYM1
   IF (NSYM.LE.O)NSYM=NROW*NCOL
                                                                         1779
                                                                         1780
   AXLEN=6.
         SCALE THE DATA FOR THE COORDINATE AXES
                                                                         1781
                                                                         1782
   ZMAX=-1.E38
   ZMIN=1.E38
                                                                         1783
   XMAX=-1.E38
                                                                         1784
   XMIN=1.E38
                                                                         1785
   DO 5 I=1, NROW
                                                                         1786
   IF (X(I).GT.XMAX)XMAX=X(I)
                                                                         1787
   IF (X(I).LT.XMIN)XMIN=X(I)
                                                                         1788
   DO 5 J=1.NCOL
                                                                         1789
   IF (D(I,J).GT.ZMAX)ZMAX=D(I,J)
                                                                         1790
                                                                         1791
 5 IF (D(I,J).GT.O..AND.D(I,J).LT.ZMIN)ZMIN=D(I,J)
                                                                         1792
   YMAX=-1.E38
                                                                         1793
   YMIN=1.E+38
                                                                          1794
   DO 10 J=1,NCOL
                                                                          1795
   IF (Y(J),GT,YMAX)YMAX=Y(J)
                                                                          1796
10 IF (Y(J).LT.YMIN)YMIN=Y(J)
   PRINT 15, XMIN, XMAX, YMIN, YMAX, ZMIN, ZMAX
                                                                          1797
15 FORMAT ('OX RANGE', 1P2E12.4,' Y RANGE', 2E12.4,' Z RANGE', 2 1798
                                                                          1799
  1E12.4)
                                                                          1800
   XFAC=AXLEN/(XMAX-XMIN)
                                                                          1801
   YFAC=AXLEN/(YMAX-YMIN)
                                                                          1802
   CDIF1=(ZMAX-ZMIN)/(2*NLEV)
                                                                          1803
   IL=-ALOG10(CDIF1)+1.
                                                                          1804
20 T=10.**IL
   ICD1F=5*((IFIX(CD1F1*T)+2)/5)
                                                                          1805
                                                                          1806
   S=(ZMIN+ZMAX-FLOAT(2*NLEV*ICDIF)/T)/2.
                                                                          1807
   IF (S.NE.O.)IS=5*(IFIX(S*T+2.5*S/ABS(S))/5)
                                                                          1808
                                                                          1809
   T1=FLOAT(IS+ICDIF)/T
                                                                          1810
   CDIF=FLOAT(2*ICDIF)/T
   S=T1+CDIF*(NLEV-1)
                                                                          1811
   S1=CDIF*.1
                                                                          1812
                                                                          1813
   IF (ZMIN.LT.T1-S1.AND.ZMAX.GT.S+S1.AND.ZMAX.LT.S+CDIF) GO TO 25
                                                                          1814
   IL=IL+1
   GO TO 20
                                                                          1815
25 FLEV(1)=T1
                                                                          1816
   IF (NLEV.EQ.1) GO TO 35
                                                                          1817
   DO 30 K=2.NLEV
                                                                          1818
30 FLEV(K)=T1+FLOAT(2*ICDIF*(K-1))/T
                                                                          1819
35 AXLP1=AXLEN+.5
                                                                          1820
```

,这种是一种,我们就是一种,我们是一种,我们是一种,我们是一种,我们也不是一种,我们也是一种,我们也是一种,我们也是一种,我们也是一种,我们们也是一种,我们们就

	AXLP2=AXLEN+.75	1821
		1822
	RSQ=X(1)**2	_
	AX2=AXLEN/2.	1823
	AX2S=(.985*AX2)**2	1824
	NROWM1=NROW-1	1825
		1826
	NCOLM1=NCOL+1	
	DO 40 K=1,NLEV	1827
	S=FLEV(K)+.001*CDIF	1828
	T=FLEV(K)001*CDIF	1829
	DO 40 I=1,NROW	1830
	DO 40 J=1,NCOL	1831
40	IF $(D(I,J).LT.S.AND.D(I,J).GT.T)D(I,J)=S$	1832
	DO 380 K=1,NLEV	1833
	F=FLEV(K)	1834
	IEND=0	1835
	DO 150 I=1,NROWM1	1836
	DO 150 J=1,NCOLM1	1837
	IFL(I,J)=0	1838
	DIJ=D(I,J)	1839
	DIIJ=D(I+1,J)	1840
	DIJ1=D(I,J+1)	1841
	DIIJ1=D(I+1,J+1)	1842
	IF (DIJ.GT.F.OR.DIJ1.LT.F) GO TO 85	1843
	T=DI1J1-F	1844
	A=DIJ	1845
	B=DIIJI	1846
45	IF (I.GT.1) GO TO 60	1847
	IF (A.GT.O.) GO TO 50	1848
	YC=SQRT(RSQ-X(I)**2)	1849
	IF (Y(J+1).LT.0.)YC=-YC	1850
		1851
	GO TO 55	
50	S=(F-DIJ)/(DIJ1-DIJ)	1852
	YC=Y(J)+S*(Y(J+1)-Y(J))	1853
55	IEND=IEND+1	1854
•••	YST(IEND)=YC	1855
	XST(IEND)=X(I)	1856
	IST(IEND)=0	1857
	JST(IEND)=J	1859
60	IF (T.GT.O.) GO TO 80	1859
	IF (J.LT.NCOLM1) GO TO 80	1860
UJ		1861
	IF (B.GT.O.) GO TO 70	
	XC=SQRT(RSQ-Y(J+1)**2)	1862
	IF (X(I+1).LT.O.)XC=-XC	1863
	GO TO 75	1864
70	S=(F-D1J1)/(D11J1-D1J1)	1865
, 0		1866
7.	$XC=X(I)+S^*(X(I+1)-X(I))$	
75	IEND=IEND+1	1867
	XST(IEND)=XC	1868
	YST(IEND)=Y(J+1)	1869
	IST(IEND)=I	1870
		1871
^-	JST(IEND)=NCOL	
80	IFL(I,J)=1	1872
	GO TO 95	1873
85	IF (DIJ.LT.F.OR.DIJ1.GT.F) GO TO 90	1874
	T=F-DI1J1	1875
		1876
	A=0IJ1	
	B=A	1877

```
GO TO 45
                                                                            1878
 90 B=DIJ1
                                                                            1879
    IF (DIJ.LT.F.AND.DI1J1.GT.F) GO TO 65
                                                                            1880
                                                                            1881
    B=DIIJI
    IF (DIJ.GT.F.AND.DIIJ1.LT.F) GO TO 65
                                                                            1882
 95 IF (DIJ.GT.F.OR.DI1J.LT.F) GO TO 140
                                                                            1883
    T=DI1J1-F
                                                                            1884
    A=DIJ
                                                                            1385
    B=DI1J1
                                                                            1086
100 IF (J.GT.1) GO TO 115
                                                                            1887
    IF (A.GT.O.) GO TO 105
                                                                            1888
    XC = SQRT(RSQ - Y(J) **2)
                                                                            1889
    IF (X(I+1).LT.0.)XC=-XC
                                                                            1890
    GO TO 110
                                                                            1891
105 S=(F-DIJ)/(DI1J-DIJ)
                                                                            1892
    XC=X(I)+S*(X(I+1)-X(I))
                                                                            1893
110 IEND=IEND+1
                                                                            1894
    XST(IEND)=XC
                                                                            1895
    YST(IEND)=Y(J)
IST(IEND)=I
                                                                            1896
                                                                            1897
    JST(IEND)=0
                                                                            189.5
115 IF (T.GT.O.) GO TO 135
                                                                            1899
    IFL(I,J)=IFL(I,J)+2
                                                                            1900
120 IF (I.LT.NROWM1) GO TO 135
                                                                            1901
    IF (B.GT.O.) GO TO 125
                                                                            1902
    YC=SQRT(RSQ-X(I+1)**2)
                                                                            1903
    IF (Y(J+1).LT.0.)YC=-YC
                                                                            1904
    GO TO 130
                                                                            1905
                                                                            1906
125 S=(F-DI1J)/(DI1J1-DI1J)
    YC=Y(J)+S*(Y(J+1)-Y(J))
                                                                            1907
130 IEND=IEND+1
                                                                            1908
    YST(IEND)=YC
                                                                            1909
    XST(IEND)=X(I+1)
                                                                            1910
    IST(IEND)=NROW
                                                                            1911
    JST(IEND)=J
                                                                            1912
135 IF (IFL(I,J).EQ.0)IFL(I,J)=1
                                                                            1913
    GO TO 150
                                                                            1914
140 IF (DIJ.LT.F.OR.DIIJ.GT.F) GO TO 145
                                                                            1915
    T=F-DI1J1
                                                                            1916
    A=DI1J
                                                                            1917
    B=A
                                                                            1918
    GO TO 100
                                                                            1919
145 B=DI1J
                                                                            1920
    IF (DIJ.LT.F.AND.DI1J1.GT.F) GO TO 120
                                                                            1921
                                                                            1922
    B=DI1J1
    IF (DIJ.GT.F.AND.DIIJ1.LT.F) GO TO 120
                                                                            1923
150 CONTINUE
                                                                            1924
155 IF (IEND.EQ.O) GO TO 160
                                                                            1925
           SET UP TO PLOT NEXT CONTOUR FROM EDGE OF GRID
                                                                            1926
    I=IST(1)
                                                                            1927
    J=JST(1)
                                                                            1928
    IOLD=I
                                                                            1929
    JOLD=J
                                                                            1930
    CALL PLOT((XST(1)-XMIN)*XFAC,(YST(1)-YMIN)*YFAC,3)
                                                                            1931
    IF (I.EQ.0)I=1
                                                                            1932
    IF (J.EQ.0)J=1
                                                                            1933
    IF (I.EQ.NROW)I=NROWM1
                                                                            1934
```

```
1935
    IF (J.EQ.NCOL)J=NCOLM1
    ISTC=1
                                                                            1936
    GO TO 180
                                                                            1937
                                                                            1938
          ALL CONTOURS THAT LEAVE GRID HAVE BEEN DRAWN
                                                                            1939
          SET UP TO PLOT NEXT CONTOUR THAT DOES NOT LEAVE GRID
160 I1=1
                                                                            1940
165 J1=1
                                                                            1941
170 IF (IFL(I1,J1).NE.O) GO TO 175
                                                                            1942
    J1=J1+1
                                                                            1943
    IF (J1.LT.NCOL) GO TO 170
                                                                            1944
    [1=I1+1]
                                                                            1945
    IF (I1.LT.NROW) GO TO 165
                                                                            1946
                                                                            1947
    GO TO 375
                                                                            1948
175 ISTC=0
                                                                            1949
    I=I1
    J=J1
                                                                            1950
                                                                            1951
180 ISYM=NSYM-1
          FIND ENDS OF LINES IN UPPER LEFT TRIANGLE
                                                                            1952
                                                                            1953
185 DIJ=D(I,J)
    DIIJ=D(I+1,J)
                                                                            1954
    DIJ1=D(I,J+1)
                                                                            1955
                                                                            1956
    DIIJI=D(I+1,J+1)
                                                                            1957
    IF (DIJ.GT.F.OR.DIJ1.LT.F) GO TO 220
                                                                            1958
    T=DIIJI-F
    A≃DIJ
                                                                            1959
    B=DIIJ1
                                                                            1960
190 IF (A.GT.O.) GO TO 195
                                                                            1961
    YC=SORT(RSO-X(I)**2)
                                                                            1962
    IF (Y(J+1).LT.0.)YC=-YC
                                                                            1963
    GO TO 200
                                                                            1964
195 S=(F-DIJ)/(DIJ1-DIJ)
                                                                            1965
    YC=Y(J)+S*(Y(J+1)-Y(J))
                                                                            1966
200 \text{ XC}=\text{X}(I)
                                                                            1967
    IB=I-1
                                                                            1968
    JB=J
                                                                            1969
    IF (T.GT.O.) GO TO 250
                                                                            1970
    IF (IFL(I,J).EQ.2) CO TO 250
                                                                            1971
    IF (B.GT.0) GO TO 205
                                                                            1972
    XC1=SORT(RSQ-Y(J+1)**2)
                                                                            1973
                                                                            1974
    IF (X(I+1).LT.0.)XC1=-XC1
    GO TO 210
                                                                            1975
205 S=(F-DIJ1)/(DI1J1-DIJ1)
                                                                            1976
                                                                            1977
    XC1=X(I)+S*(X(I+1)-X(I))
210 YC1=Y(J+1)
                                                                            1978
    IE=I
                                                                            1979
                                                                            1980
    JE=J+1
    IF (IOLD.EQ.IB.AND.JOLD.EQ.JB) GO TO 215
                                                                            1981
    IF (IOLD.NE.IE.OR.JOLD.NE.JE) GO TO 250
                                                                            1982
215 IFL(I,J)=IFL(I,J)-1
                                                                            1983
    GO TO 310
                                                                            1984
220 IF (DIJ.LT.F.OR.DIJ1.GT.F) GO TO 225
                                                                            1985
    T=F-D1131
                                                                            1986
    A=DIJ1
                                                                            1987
    B=A
                                                                            1988
                                                                            1989
    GO TO 190
225 IF (DIJ.GT.F.OR.DI1J1.LT.F) GO TO 245
                                                                            1990
                                                                            1991
    IF (DIJ1.GT.O.) GO TO 235
```

```
1992
230 XC = SORT(RSQ - Y(J+1)**2)
                                                                           1993
    IF (X(I+1).LT.0.)XC=-XC
                                                                            1994
    GO TO 240
                                                                           1995
235 S=(F-DIJ1)/(DI1J1-DIJ1)
                                                                            1996
    XC=X(I)+S*(X(I+1)-X(I))
                                                                           1997
240 VC = Y(J+1)
                                                                            1998
    IB=I
                                                                            1999
    JB=J+1
                                                                            2000
    GO TO 250
                                                                            2001
245 IF (DIJ.LT.F.OR.DI1J1.GT.F) GO TO 250
                                                                            2002
    IF (DI1J1.GT.O.) GO TO 235
    GO TO 230
                                                                            2003
                                                                            2004
          FIND ENDS OF LINES IN LOWER RIGHT TRIANGLE
                                                                            2005
250 IF (DIJ.GT.F.OR.DI1J.LT.F) GO TO 290
                                                                            2006
    T=DI1J1-F
                                                                            2007
    A=DIJ
                                                                            2008
    B≈DI1J1
                                                                            2009
255 IF (A.GT.O.) GO TO 260
                                                                            2010
    XC1=SQRT(RSQ-Y(J)**2)
                                                                            2011
    IF (X(I+1).LT.0.)XC1=-XC1
                                                                            2012
    GO TO 265
                                                                            2013
260 S=(F-DIJ)/(DIIJ-DIJ)
                                                                            2014
    XC1=X(I)+S*(X(I+1)-X(I))
                                                                            2015
265 IF (T.GT.O) GO TO 285
                                                                            2016
    IF (IFL(I,J).LT.2) GO TO 310
                                                                            2017
    XC=XC1
                                                                            2018
    YC=Y(J)
                                                                            2019
    IB=I
                                                                            2020
    JB=0-1
    IFL(I,J)=IFL(I,J)-2
                                                                            2021
                                                                            2022
270 IF (B.GT.O.) GO TO 275
                                                                            2023
    YC1=SQRT(RSQ-X(I+1)**2)
                                                                            2024
    IF (Y(J+1).LT.0)YC1=-YC1
    GO TO 280
                                                                            2025
                                                                            2026
275 S=(F-DI1J)/(DI1J1-DI1J)
                                                                            2027
    YC1=Y(J)+S*(Y(J+1)-Y(J))
                                                                            2028
280 XC1=X(I+1)
                                                                            2029
    IE=I+1
                                                                            2030
    JE=J
                                                                            2031
    GO TO 310
                                                                            2032
285 YC1=Y(J)
                                                                            2033
    IE=I
                                                                            2034
    JE=J-1
                                                                            2035
    IFL(I,J)=0
                                                                            2036
    GO TO 310
                                                                            2037
290 IF (DIJ.LT.F.OR.DIIJ.GT.F) GO TO 295
                                                                            2038
    T=F-DIIJI
                                                                            2039
    A=DIIJ
                                                                             2040
    B=V
                                                                             2041
    GO TO 255
                                                                             2042
295 IF (UIJ.GT.F.CP.DIIJI.LT.F) GO TO 305
                                                                             2043
    B=CIIJ
                                                                             2044
300 IFL(1,J)=0
                                                                             2045
    GO TO 270
                                                                             2046
305 B=DI1J1
                                                                             2047
     IF (DIJ.GT.F.AND.DIIJ1.LT.F) GO TO 300
310 IF (ISTC.NE.O) GO TO 320
                                                                             2048
```

```
91.07 FIRST SEGMENT OF NEW CONTOUR
                                                                           2049
                                                                           2050
   CALL PLOT ((XC1-XMIN)*XFAC, (YC1-YMIN)*YFAC, 3)
                                                                           2051
    ISTC=1
315 PX=(XC-XMIN)*XFAC
                                                                           2052
    PY=(YC-YMIR)*YFAC
                                                                           2053
                                                                           2054
    IOLD=I
    J0LD=J
                                                                           2055
    I=IB
                                                                           2056
                                                                           2057
    J≃JB
                                                                           2058
    GO TO 340
          MATCH CURRENT PEN POSITION TO ONE END OF NEW LINE SEGMENT
                                                                           2059
                                                                           2060
320 IF (IOLD.EQ.IB.AND.JOLD.EQ.JB) GO TO 335
    IF (IOLD.EQ.IE.AND.JOLD.EQ.JE) GO TO 315
                                                                           2061
    PRINT 330, I, J, IOLD, JOLD, IB, JB, IE, JE, DIJ, DIJI, DIIJ, DIIJ1
                                                                           2062
330 FORMAT ('-LOGIC ERROR: AT'.213.' FROM'.213.' TO'.213.' OR'.213.4 2063
   1F8.4)
                                                                           2064
    STOP
                                                                           2065
335 PX=(XC1-XMIN)*XFAC
                                                                           2056
    PY=(YC1-YMIN)*YFAC
                                                                           2067
                                                                           2068
    IOLD=I
    JOLD=J
                                                                           2069
                                                                           2070
    I=IE
    J=JE
                                                                           2071
          PLOT LINE SEGMENT
                                                                           2072
340 R1SQ=(PX-AX2)**2+(PY-AX2)**2
                                                                           2073
    IF (R1SQ.GT.AX2S) GO TO 345
                                                                           2074
    ISYM=ISYM+1
                                                                           2075
    IF (ISYM.LT.NSYM) GO TO 345
                                                                           2076
                                                                           2077
    CALL SYMBOL(PX,PY,.07,K,0.,-2)
    ISYM=0
                                                                           2078
    GO TO 350
                                                                           2079
345 CALL PLOT(PX,PY,2)
                                                                           2080
          DETERMINE WHETHER CONTOUR HAS ENDED
                                                                           2081
350 IF (I.EQ.O.OR.I.EQ.NROW.OR.J.EQ.O.OR.J.EQ.NCOL) GO TO 355
                                                                           2082
       (IFL(I,J).NE.O) GO TO 185
                                                                           2083
    IF (IEND.EQ.0) GO TO 170
                                                                           2084
          REMOVE END POINTS OF LAST CONTOUR FROM TABLE
                                                                           2085
                                                                           2086
355 I1=0
    IF (IEND.EQ.1) GO TO 370
                                                                           2087
    DO 365 L=2, IEND
                                                                           2088
    IF (I.EQ.IST(L).AND.J.EQ.JST(L)) GO TO 365
                                                                           2089
                                                                           2090
    I1 = I1 + 1
    XST(I1)=XST(L)
                                                                           2091
    YST(I1)=YST(L)
                                                                           2092
    IST(I1)=IST(L)
                                                                           2093
                                                                           2094
    JST(I1)=JST(L)
365 CONTINUE
                                                                           2095
370 IEND=I1
                                                                           2096
    GO TO 155
                                                                           2097
          PUT SYMBOL AND LEVEL ON PLOT
                                                                           2098
          ALL CONTOURS AT THIS LEVEL HAVE BEEN DRAWN
                                                                           2099
375 FLK=FLOAT(K-1)*.6
                                                                           2100
    CALL SYMBOL (AXLP1,FLK+.08,.14,K,0.,-1)
                                                                           2101
    CALL FNUM(AXLP2,FLK,FLEV(K),2,0.,.14)
                                                                           2102
380 CONTINUE
                                                                           2103
*** PLOT AXES
                                                                           2104
    CALL PLOT(AX2, AXLEN, 3)
                                                                            2105
```

```
CALL PLOT(AX2.0..2)
                                                                            2106
    CALL PLOT(0..AX2.3)
                                                                            2107
    CALL PLOT (AXLEN, AX2, 2)
                                                                            2108
*** PLOT CIRCLE AROUND CONTOURS
                                                                            2109
    DTH=2.*3.1415927/288
                                                                            2110
    THETA=DTH
                                                                            2111
    DO 385 K=1,288
                                                                            2112
    R=AX2*(1,+COS(THETA))
                                                                            2113
    P=AX2*(1.+SIN(THETA))
                                                                            2114
    THETA=THETA+DTH
                                                                            2115
385 CALL PLOT(R,P,2)
                                                                            2116
    RETURN
                                                                            2117
    END
                                                                            2118
                                                                            2119
                                                                            2120
    SUBROUTINE FNUM(XPAGE, YPAGE, FPN, ND, ANGLE, HEIGHT)
                                                                            2121
         EDIT A FLOATING POINT NUMBER FOR THE PLOTTER
                                                                            2122
                   X COORDINATE OF STARTING POINT (INCHES)
                                                                            2123
            XPAGE
                   Y COORDINATE OF STARTING POINT (INCHES)
                                                                            2124
            FPN
                    NUMBER TO BE PLOTTED
                                                                            2125
                    IF 10.**-ND <= FPN < 10.**ND, THE NUMBER IS PLOTTED 2126
            ND
                    WITHOUT EXPONENT
                                                                            2127
            ANGLE ANGLE AT WHICH NUMBER IS PLOTTED (DEGREES)
                                                                            2128
            HEIGHT CHARACTER SIZE (INCHES)
                                                                            2129
    DIMENSION B(6)
                                                                            2130
    DATA B/.999999,.9999,.999,.99,.9/
                                                                            2131
    X=ABS(FPN)
                                                                            2132
                                                                            2133
    IF (X.NE.O.) GO TO 5
                                                                            2134
            PLOT ZERO
                                                                            2135
    CALL NUMBER (XPAGE, YPAGE, HEIGHT, X, ANGLE, 1)
                                                                            2136
    RETURN
                                                                            2137
  5 N=ALOG10(X)
                                                                            2138
    IF (X.LT.1.)N=N-1
                                                                            2139
    X=X*10.**(-N)
                                                                            2140
                                                                            2141
    T=X/10.-X*1.E-7
    00 10 J=1,6
                                                                            2142
    T1=T-INT(T)
                                                                            2143
    IF (T1.LE.O) GO TO 15
IF (T1.GE.B(J)) GO TO 15
                                                                            2144
                                                                            2145
 10 T=T*10.
                                                                            2146
 15 J=J-1
                                                                            2147
    T=ABS(FPN)
                                                                            2148
    IF (T.GE.10.**M) GO TO 20
                                                                            2149
    IF (T+.5*10.**(N-6).LT.10.**(-M)) GO TO 20
                                                                            2150
           PLOT NUMBERS WHICH DO NOT NEED EXPONENTS
                                                                            2151
    M=J-N-1
                                                                            2152
    IF (M.LT.1)M=1
                                                                            2153
    IF (M.GT.9)M=9
                                                                            2154
    CALL NUMBER (XPAGE, YPAGE, HEIGHT, FPN, ANGLE, M)
                                                                            2155
    RETURN
                                                                            2156
           PLOT NUMBERS WITH EXPONENTS
                                                                            2157
 20 IF (J.GT.1) GO TO 25
                                                                            2158
    X=1.
                                                                            2159
    N=N+1
                                                                            2160
    J=2
                                                                            2161
 25 IF (FPN.LT.O.)X=-X
                                                                            2162
```

CALL NUMBER(XPAGE, YPAGE, HEIGHT, X, ANGLE, J-1)	2163
CALL SYMBOL (999.,999., HEIGHT, 3H*10, ANGLE, 3)	2164
X1=HEIGHT/2	2165
A=3.1415927*ANGLE/180.	2166
SA=SIN(A)	2167
CA=COS(A)	2168
NC=J+4	2169
IF (FPN.LT.O.)NC=NC+1	2170
S=NC*HEIGHT	2171
PX=XPAGE+S*CA-X1*SA	2172
PY=YPAGE+S*SA+1.5*X1*CA	2173
CALL NUMBER(PX,PY,X1,FLOAT(N),ANGLE,-1)	2174
RETURN	2175
END	2176



DEPARTMENT OF THE AIR FORCE AIR FORCE INSTITUTE FOR OPERATIONAL HEALTH (APMC) BROOKS CITY-BASE TEXAS

31 August 2007

MEMORANDUM FOR DTIC-OCO

ATTN: LARRY DOWNING

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FORT BELVOIR, VA 22060-6218

FROM: AFIOH/DOBP (STINFO)

2513 Kennedy Circle

Brooks City-Base TX 78235-5116

SUBJECT: Changing the Distribution Statement on a Technical Report

This letter documents the requirement for DTIC to change the distribution statement from "B" to "A" (Approved for public release; distribution is unlimited.) on the following technical report: AD Number ADB071126, SAM-TR-82-22, A Computer Model Predicting the Thermal Response to Microwave Radiation.

If additional information or a corrected cover page and SF Form 298 are required please let me know. You can reach me at DSN 240-6019 or my e-mail address is sherry mathews@brooks.af.mil.

Thank you for your assistance in making this change.

SHERRY Y. MATHEWS AFIOH STINFO Officer